

# *Adventures in the microlensing cloud*

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*Christopher Fluke, Nick Bate, Darren Croton*

*Centre for Astrophysics and Supercomputing  
Swinburne University of Technology*

# Quasars and Supermassive black holes

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Quasars → feedback → galaxy formation and evolution

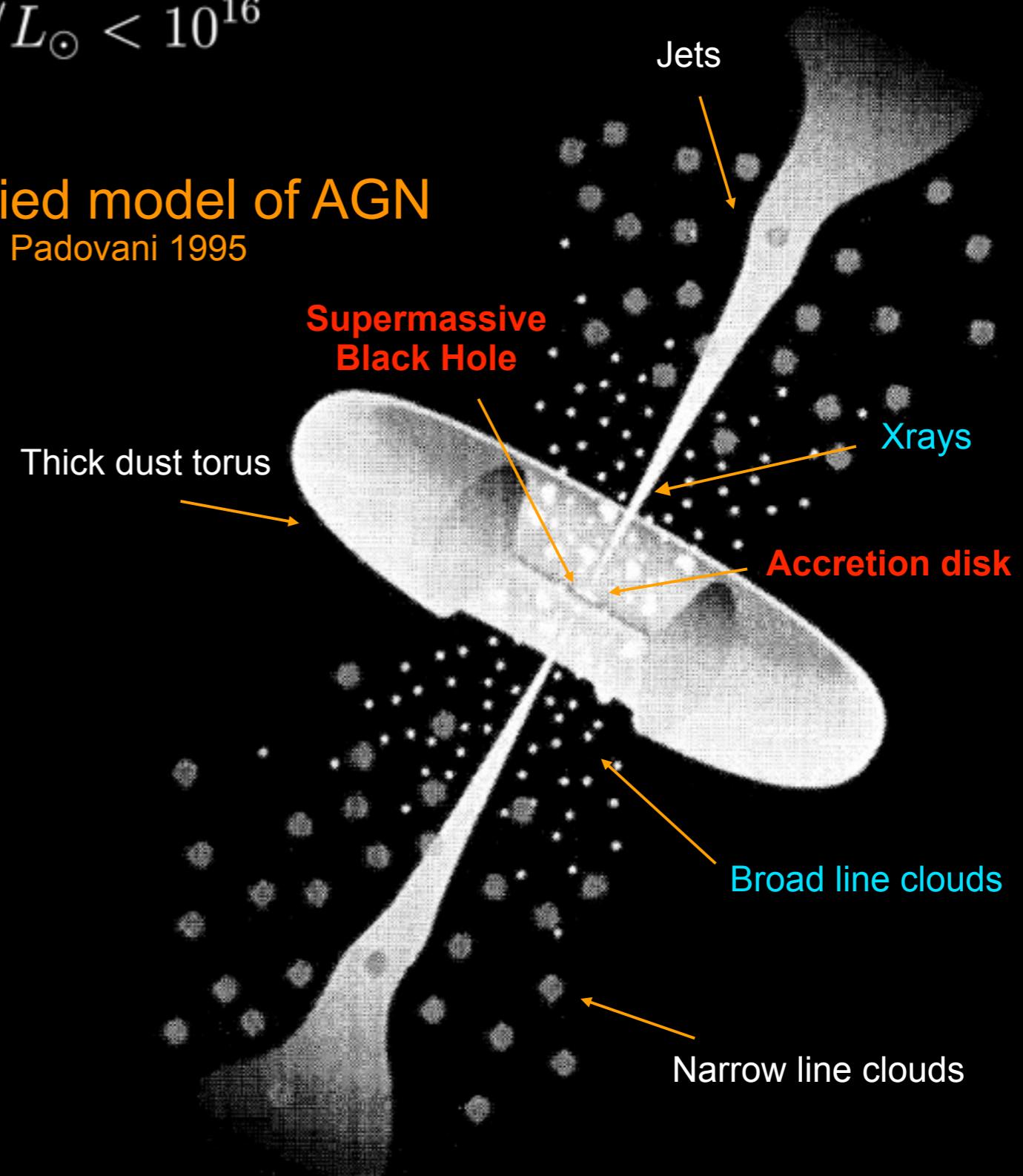
Quasar luminosities :  $10^{11} < L/L_{\odot} < 10^{16}$

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Unified model of AGN  
Urry & Padovani 1995



# Quasars and Supermassive black holes

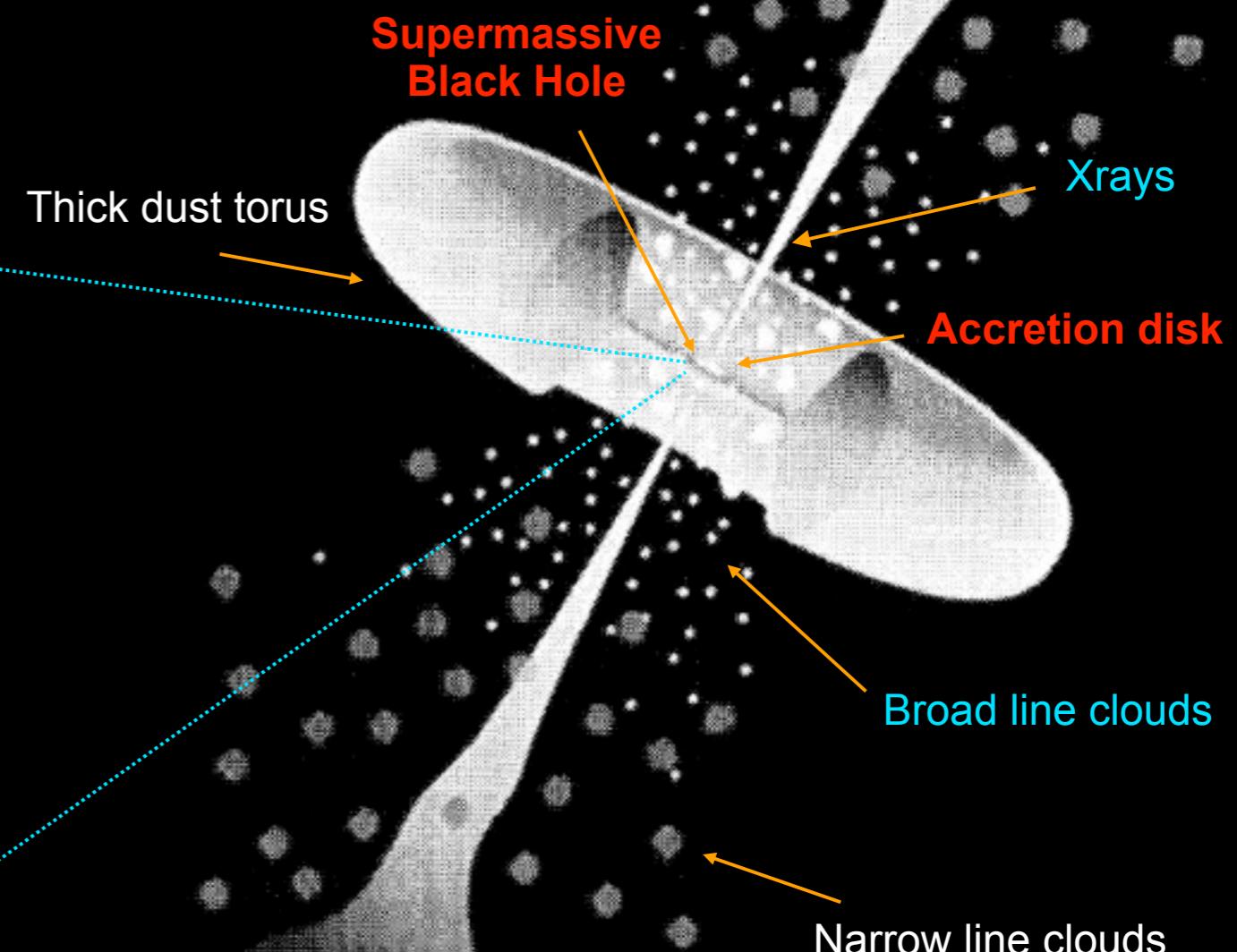
Quasars → feedback → galaxy formation and evolution

Quasar luminosities :  $10^{11} < L/L_{\odot} < 10^{16}$

*Accretion disc + Black hole = Energy*



Unified model of AGN  
Urry & Padovani 1995



B

You are here



B

You are here





B

You are here



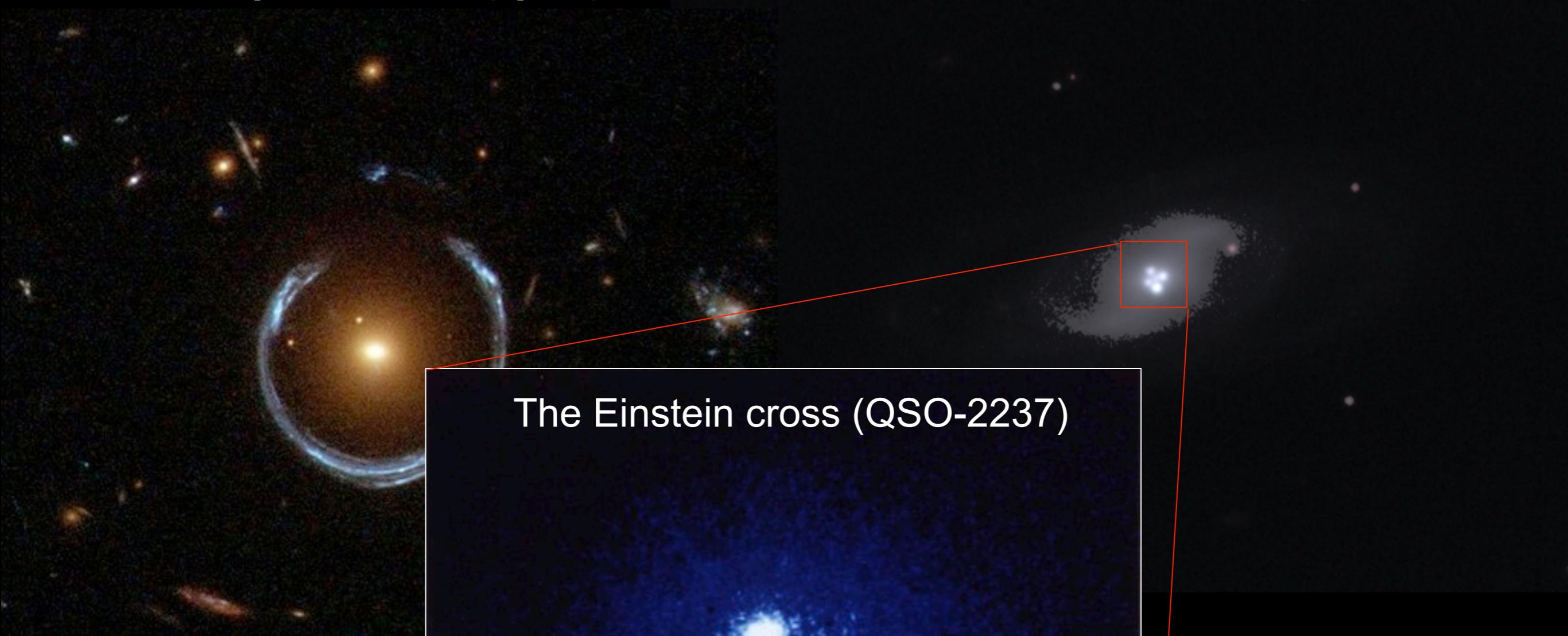
# *(Strong) gravitational lensing*



Images : HST NASA/ESA

*Einstein rings, arcs, multiple images, magnifications...*

# (Strong) gravitational lensing



The Einstein cross (QSO-2237)

Images : HST NASA/ESA

$z_{\text{source}} = 1.69$   
 $z_{\text{lens}} = 0.04$

# *lensing models part 1 (macro)*

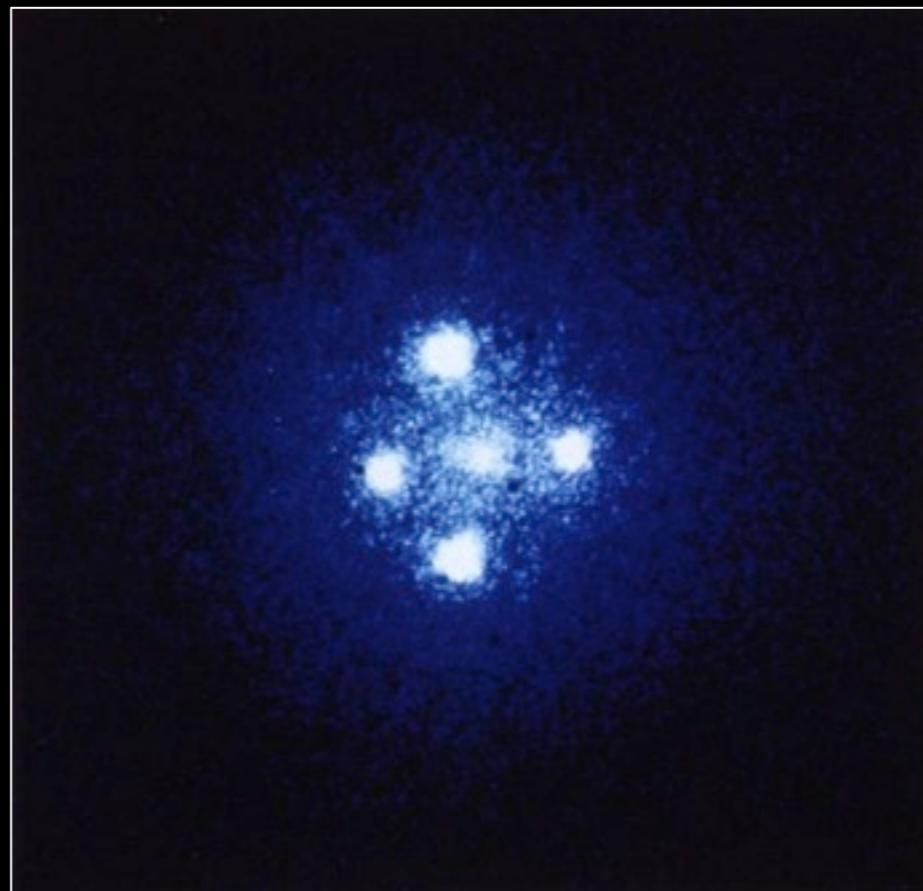
**Input**

(Observables)

Position of images  
Image fluxes  
(Time delays)  
...



Solve lens equation  
for ***mass distribution***



**Output**

*magnifications*  
 $\kappa$  : convergence  
 $\gamma$  : shear  
...

...

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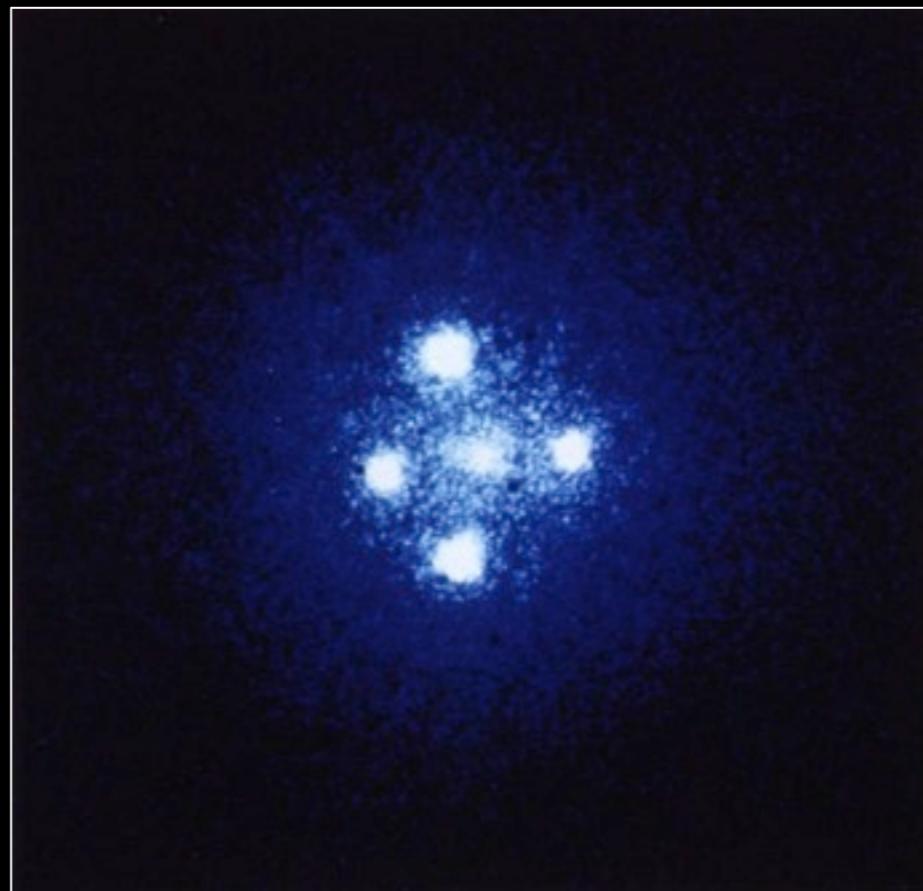
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study structure and substructure of the lens galaxy  
study high redshift sources  
perform cosmological measurements  
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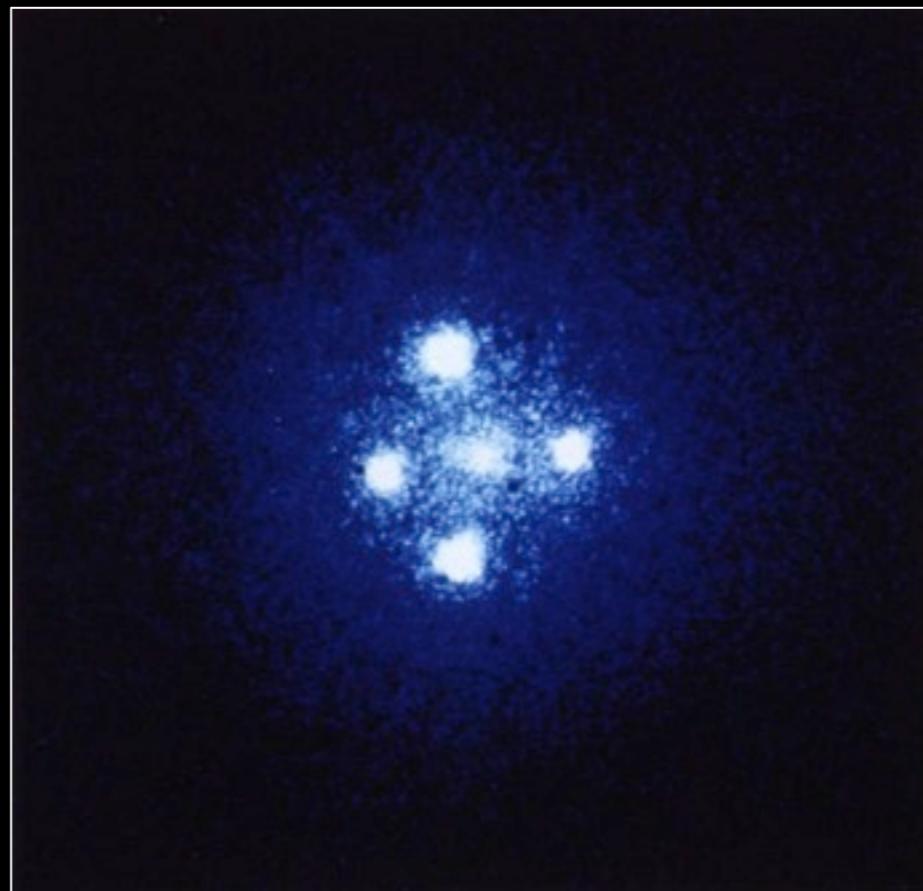
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*Ready to :*

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...

*But not the accretion disc yet!*

image WHT, Lewis G.

# QSO 2237

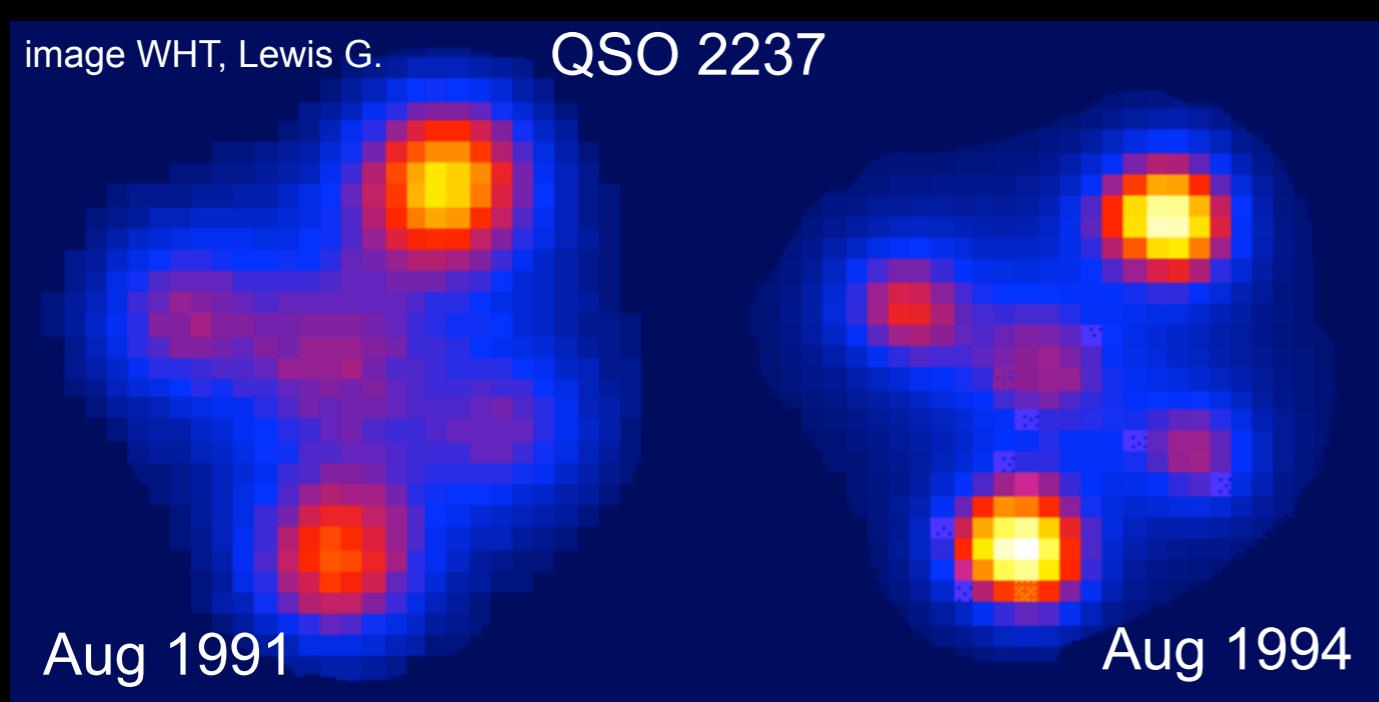


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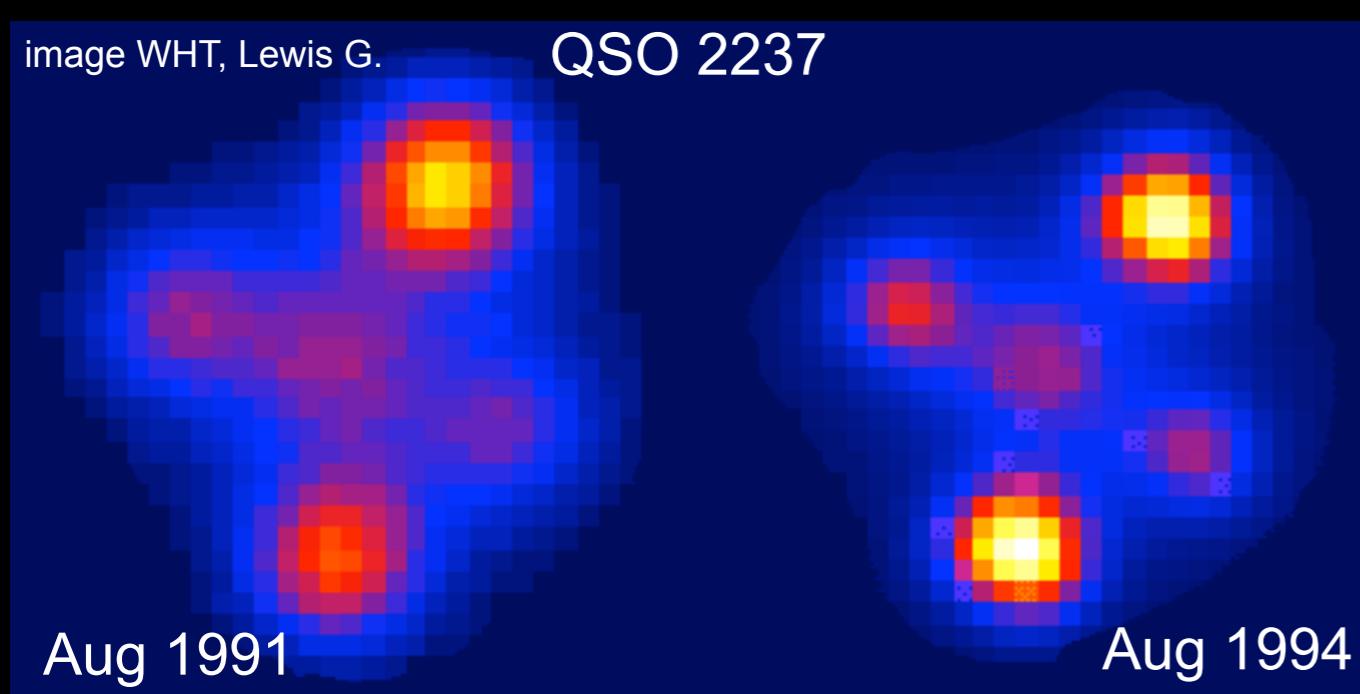


Figure: OGLE database

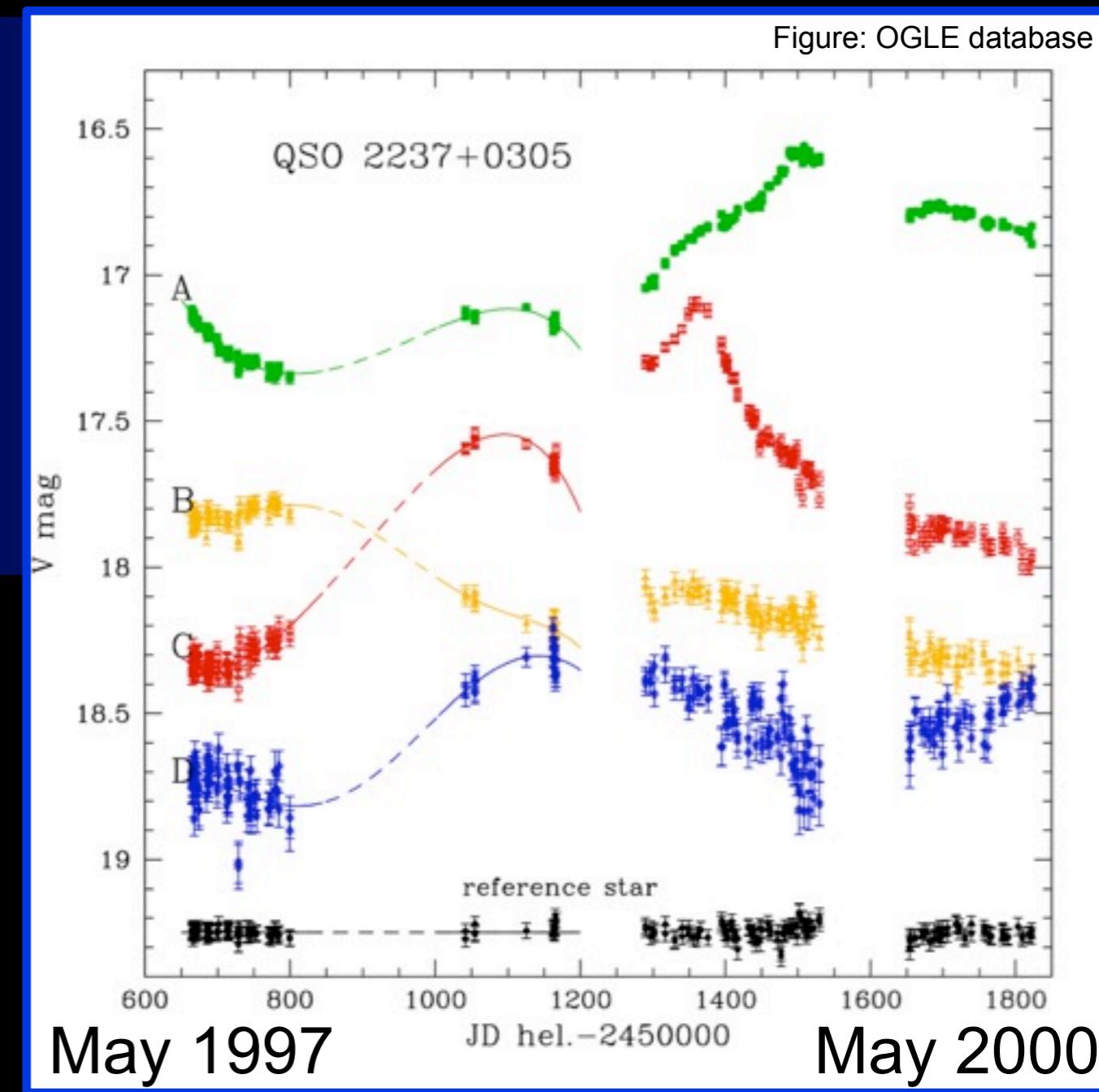


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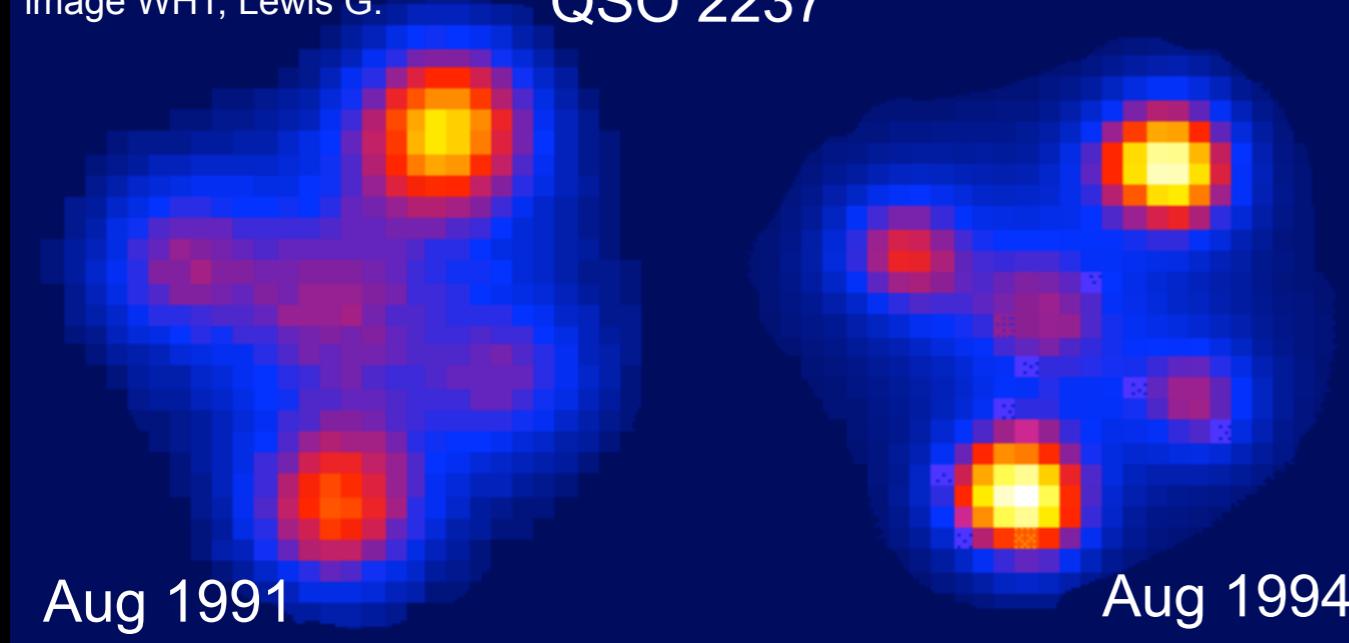
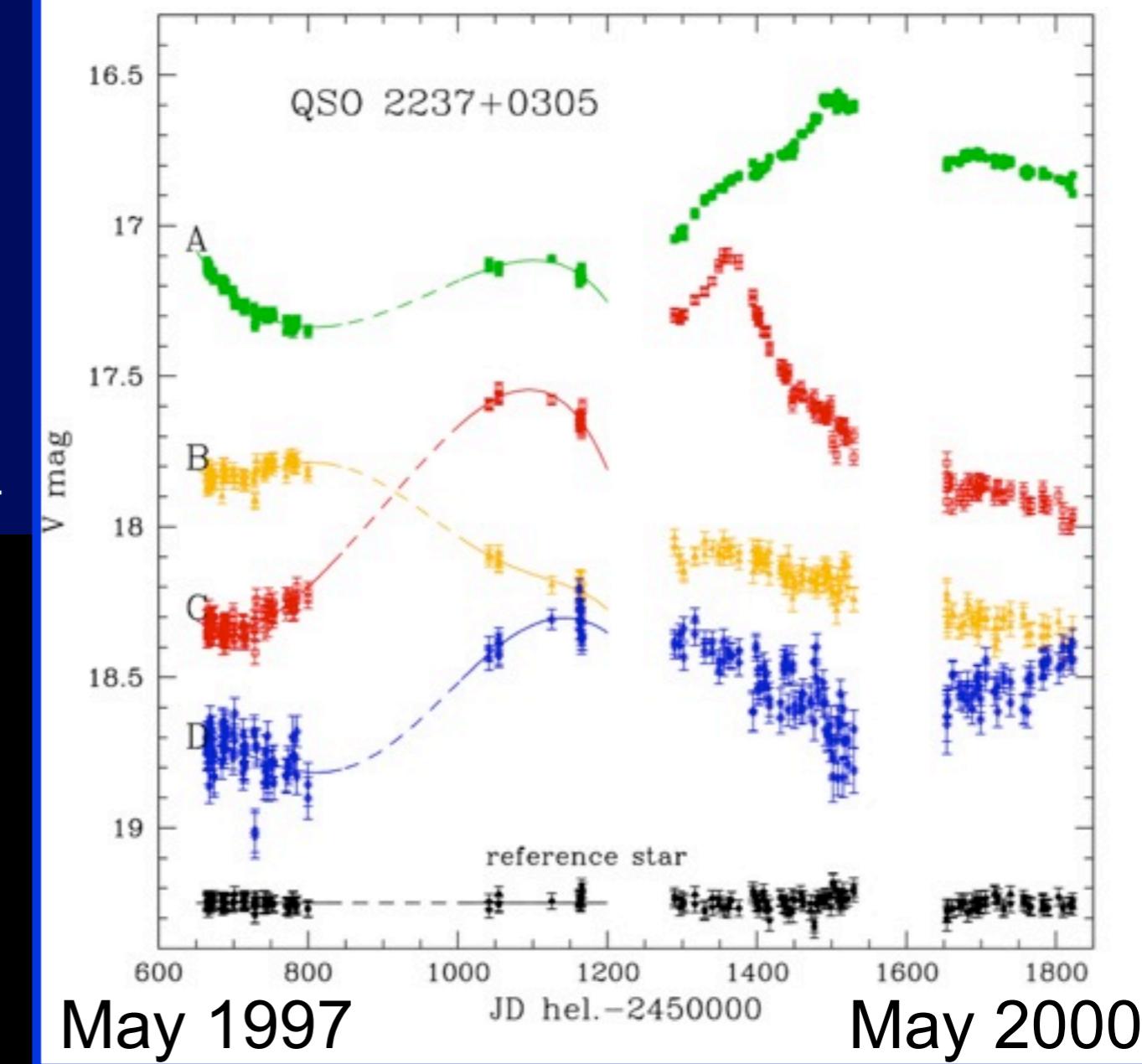


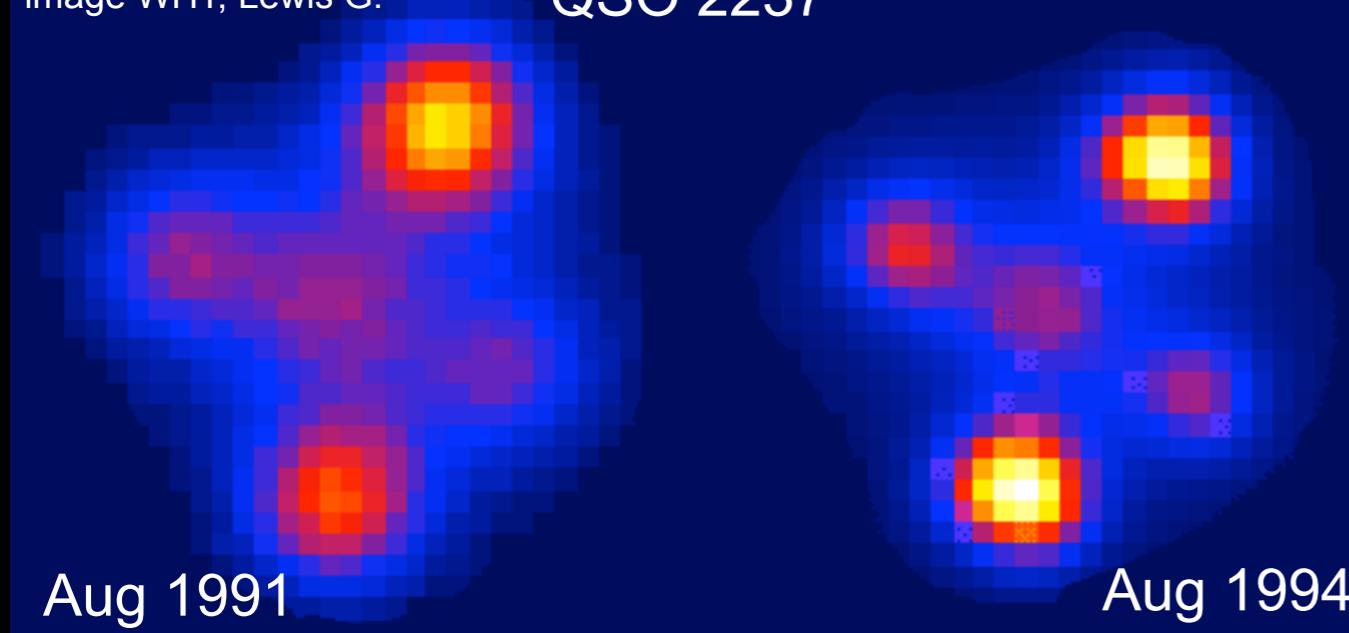
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- *uncorrelated variability due to the lens*
- *models predict constant magnification*
- *we assumed smooth matter only...*

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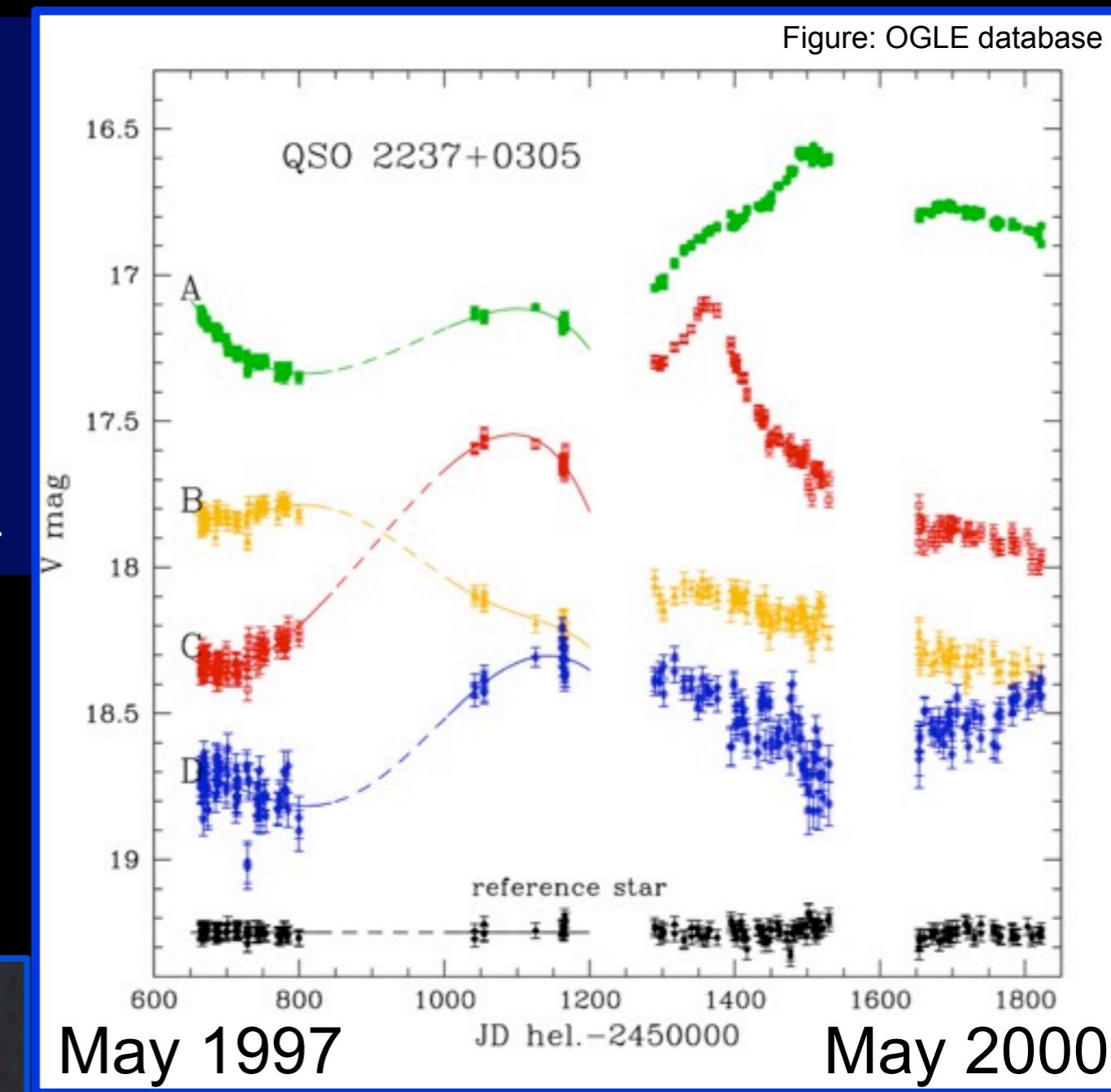


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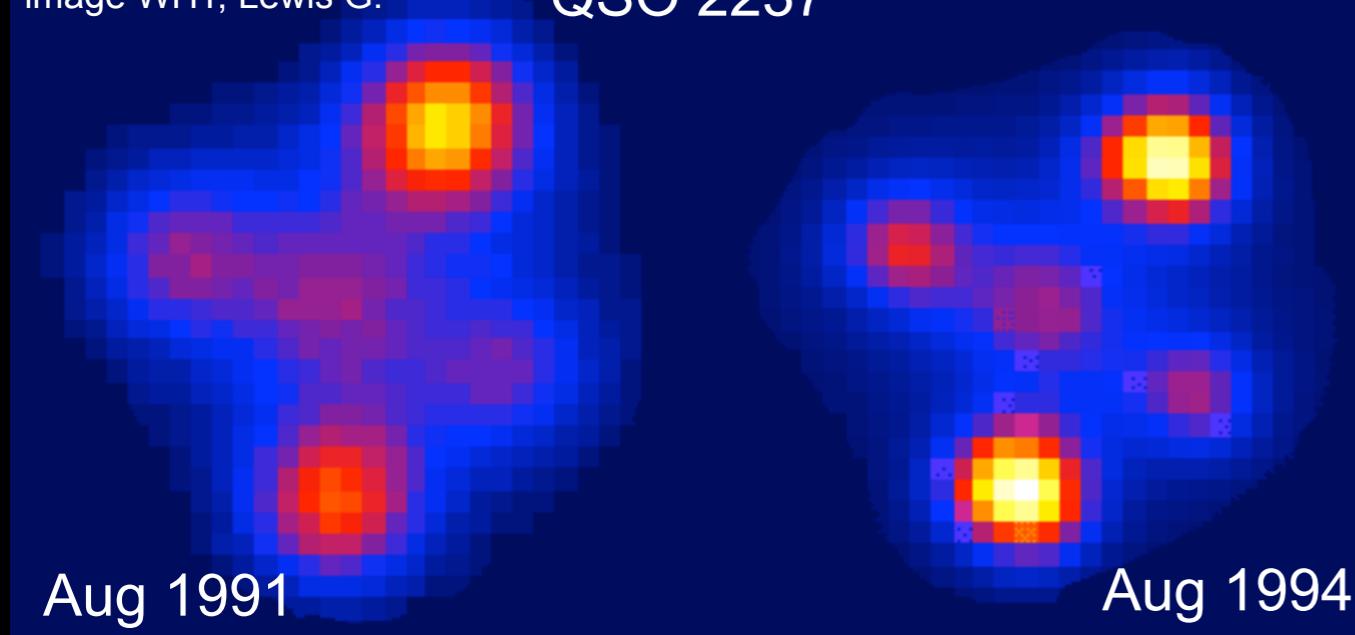
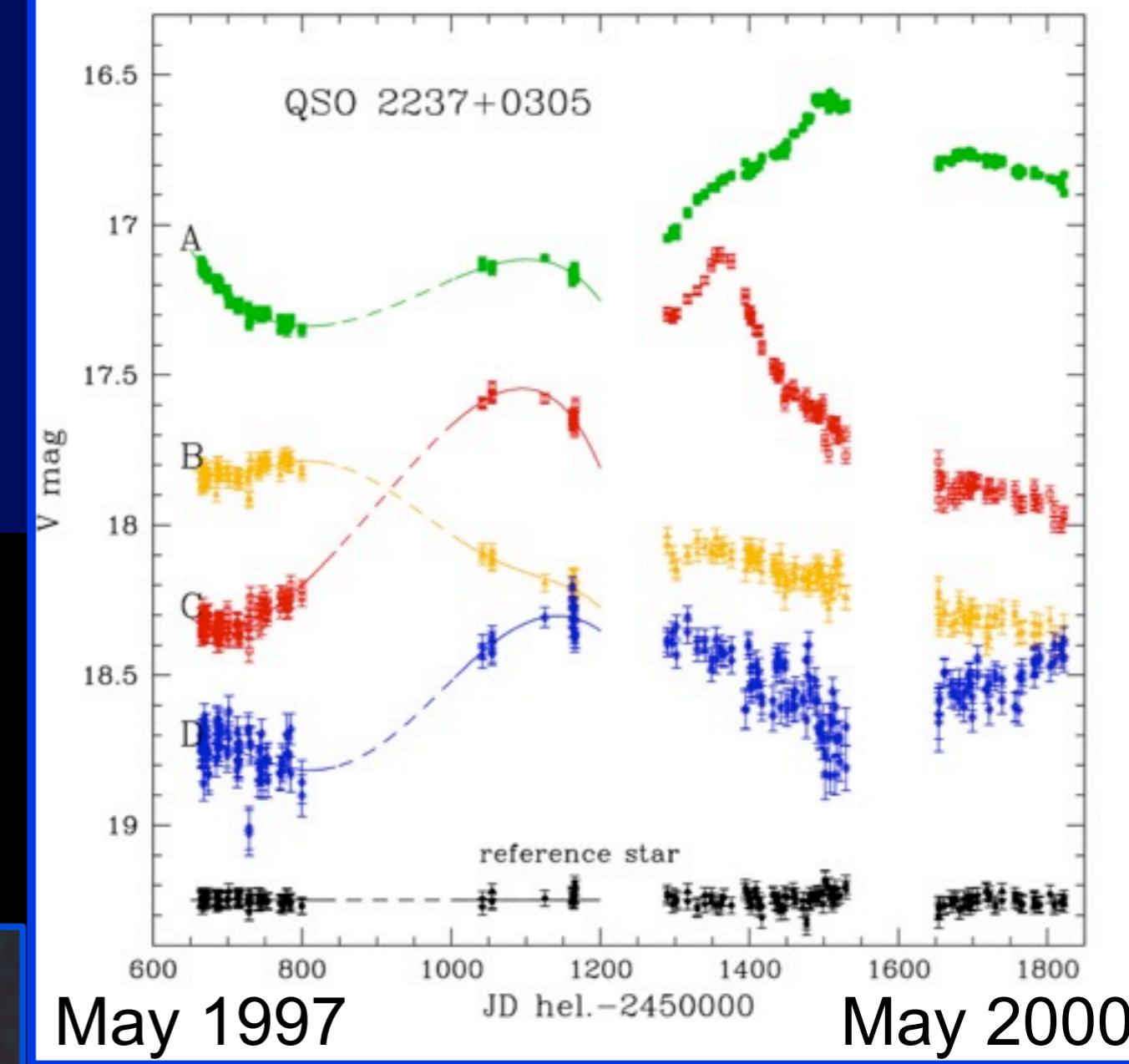


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- *uncorrelated variability due to the lens*
- *models predict constant magnification*
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compact objects  
near the line of sight  
+  
relative motion  
+  
*accretion disc size*

Quasar microlensing

# *Quasar microlensing : present*

## SINGLE OBJECTS

- ▶ Mass function, stellar mass fraction (lens galaxy)  
*(Poindexter et al. 2010, Mediavilla et al. 2009, Pooley et al. 2009)*
- ▶ Size of the broad line region, X-ray emission  
*(Floyd et al. 2012, Sluse et al. 2011, Dai et al. 2010)*
- ▶ **Accretion disk size and profile, black-hole**  
*(Blackburne et al. 2011, Morgan et al. 2010)*

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Currently there are ~90 known lensed quasars (CASTLES)  
~23 systems have been studied using microlensing

Number of systems is low due to difficulties in observing  
*(continuous monitoring, multi-wavelength)*

# *Quasar microlensing : future*

Future synoptic all-sky surveys, like **LSST**,  
are expected to find **~8000** new multiply imaged quasars  
**~3000** of which might be suitable for microlensing (*Oguri et al 2010*)

SINGLE OBJECTS



STATISTICAL SAMPLES

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STATISTICAL SAMPLES

- *Can microlensing constrain accretion discs in the future?*

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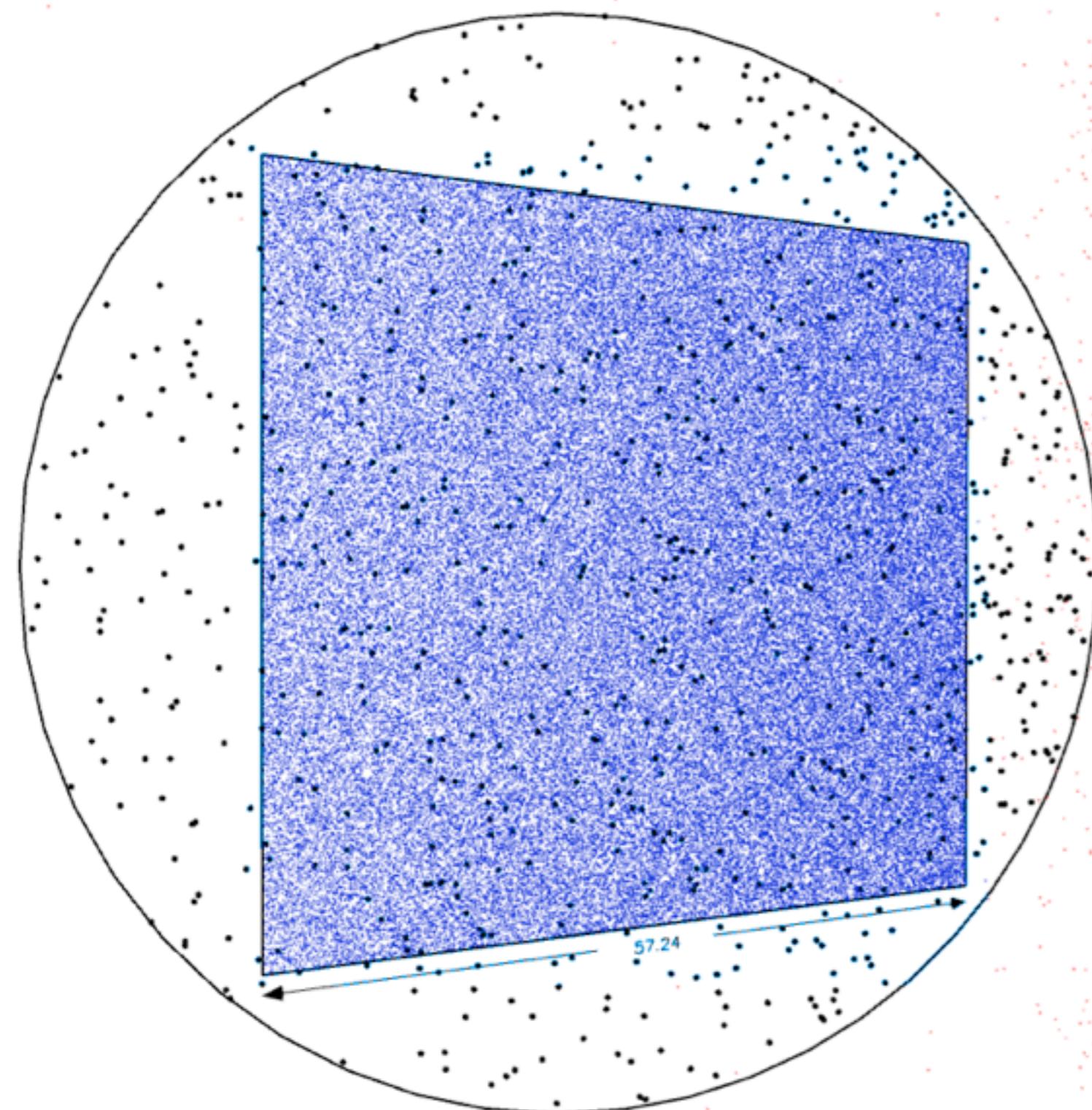


**STATISTICAL SAMPLES**

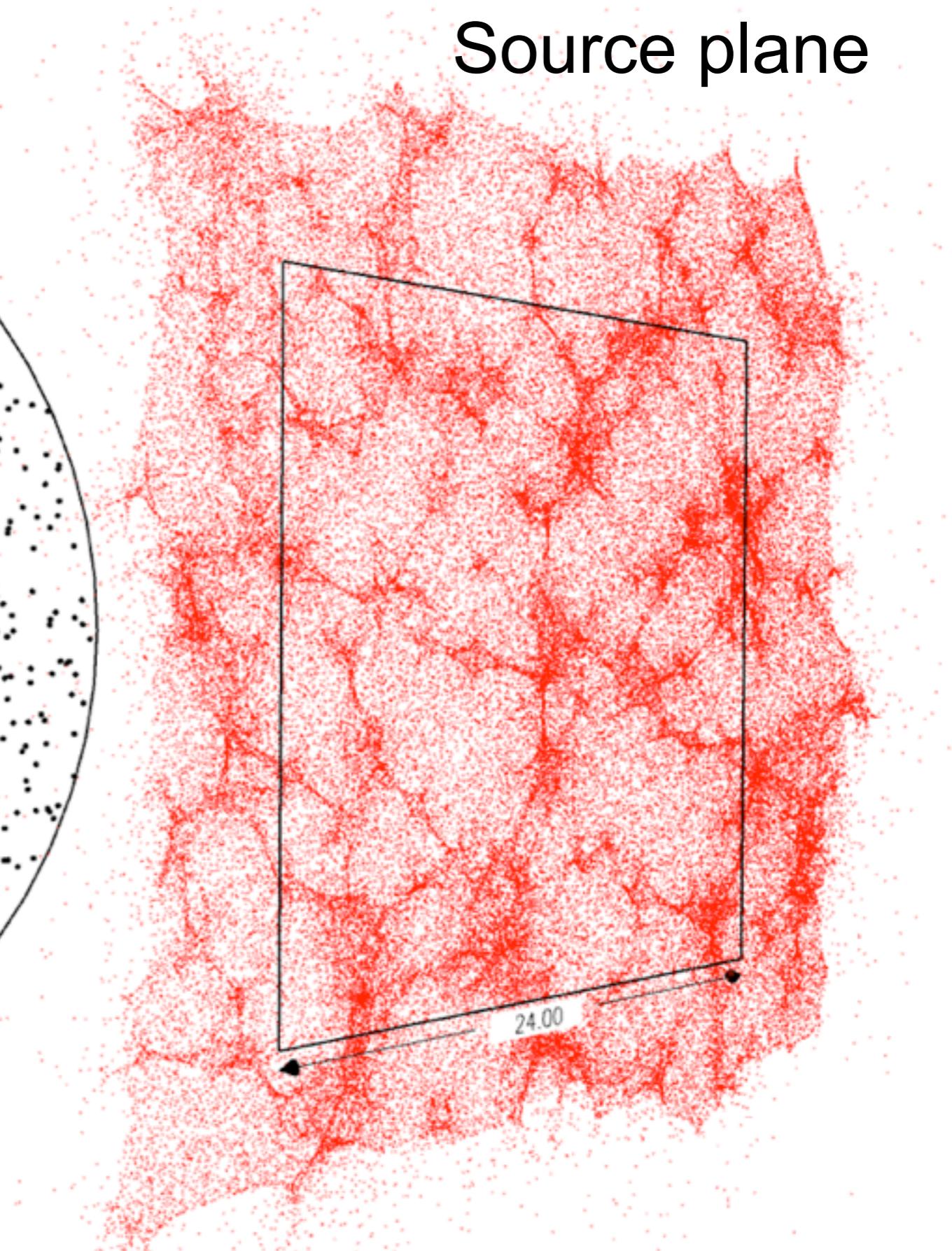
- *Can microlensing constrain accretion discs in the future?*  
→ *a lot of computational power needed !!!*

# *lensing models part 2 (micro)*

Lens plane

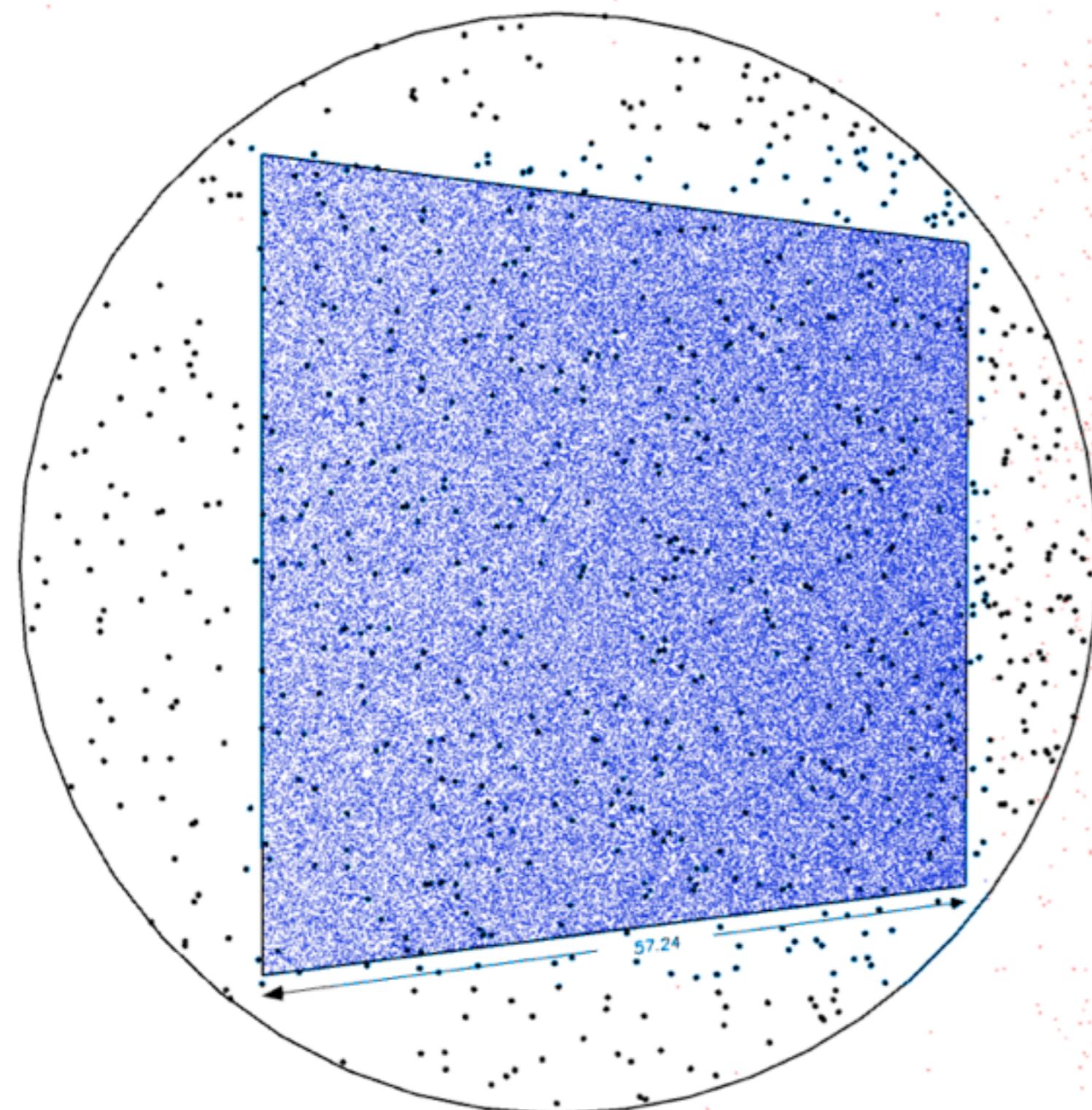


Source plane

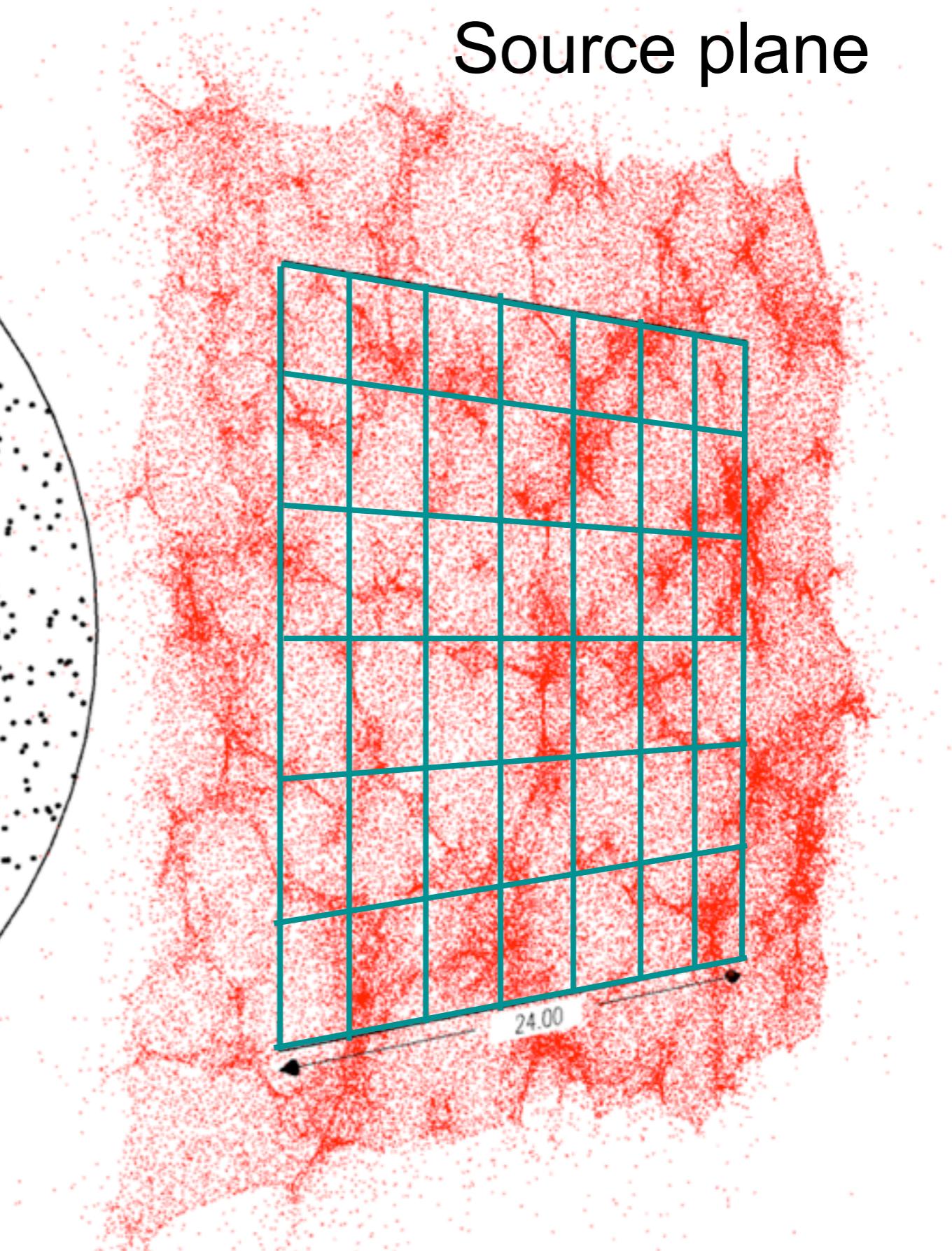


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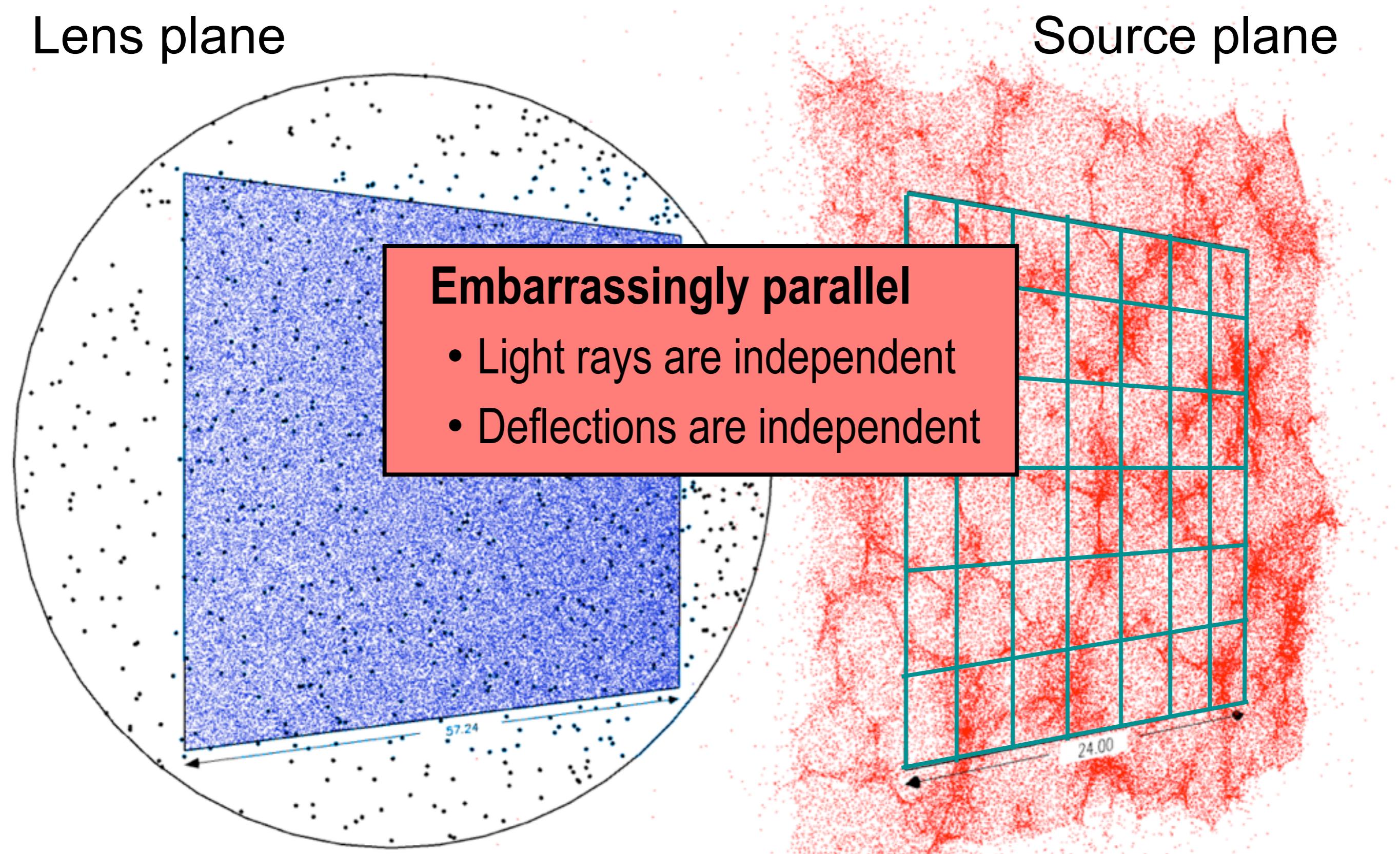
Source plane



# *lensing models part 2 (micro)*

Lens plane

Source plane



# *lensing models part 2 (micro)*

Lens plane

Source plane

## Embarrassingly parallel

- Light rays are independent
- Deflections are independent

**Direct inverse ray-shooting technique**  
*(Thompson et al. 2010, Bate et al. 2010)*

Graphics Processing Units,  
**GPUs**



**GPU supercomputers**  
(like gSTAR)



# *Understanding the microlensing parameter space*

	Wambsganss 1992	Lewis & Irwin 1995	GERLUMPH* 2013
method	tree code	contours	direct
pixels	512	-	10000
Total	<b>64</b>	<b>61</b>	<b>~50000</b>

\* *GPU-Enabled High-Resolution Micro-Lensing parameter survey*  
*(Bate & Fluke 2012)*

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Convergence,  $\kappa$  describes the focusing power of the lenses

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Microlensing

mass of the microlenses	(Wambsganss 1992, Lewis & Irwin 1995)
positions of the microlenses	(Vernardos & Fluke 2013)
map width	(Vernardos & Fluke 2013)
including smooth matter	(Vernardos et al. 2013, refereed)

Accretion disc

size	
temperature profile	in progress...
other...	

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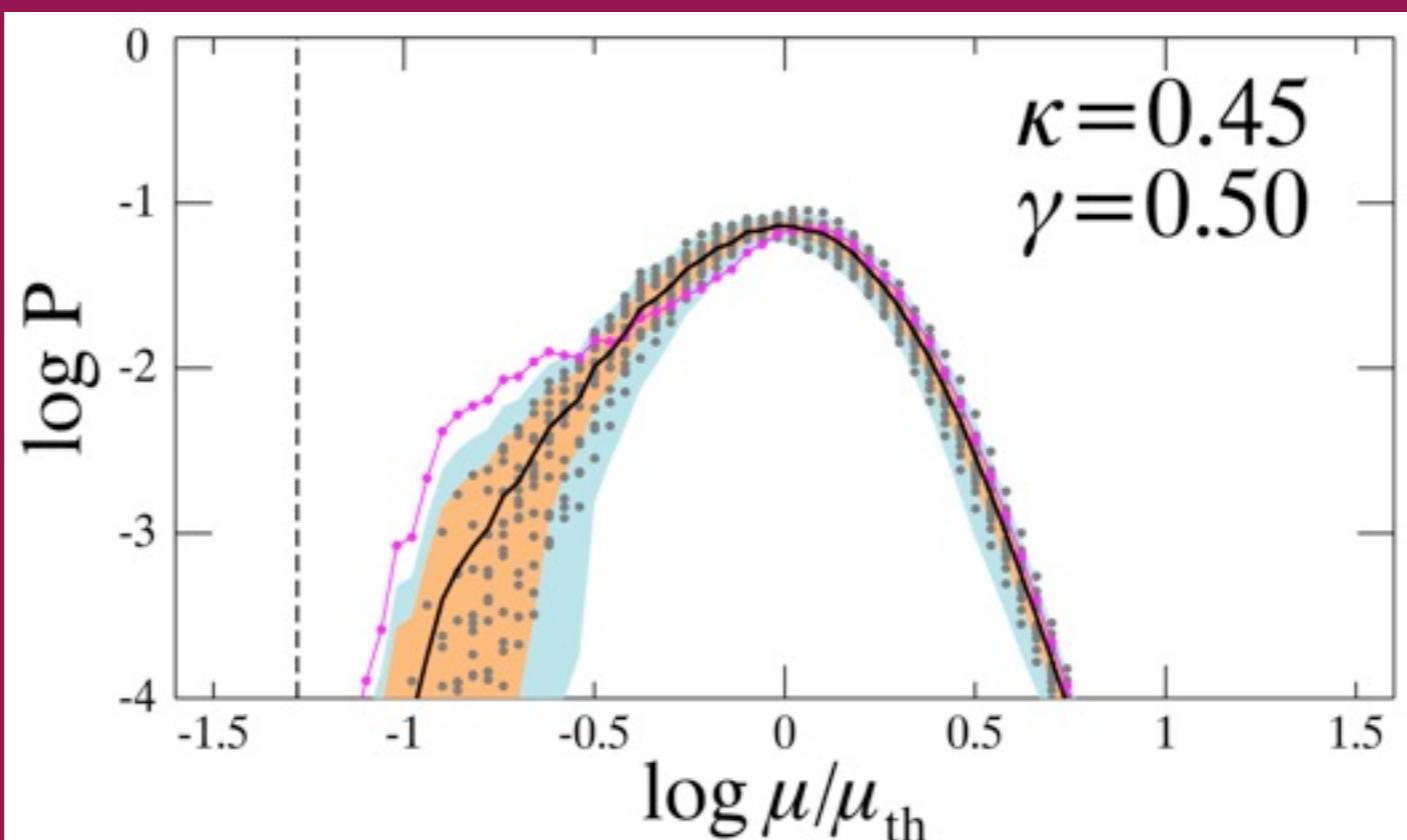
Accretion disc

size  
*temperature profile*  
*other...* *in progress...*

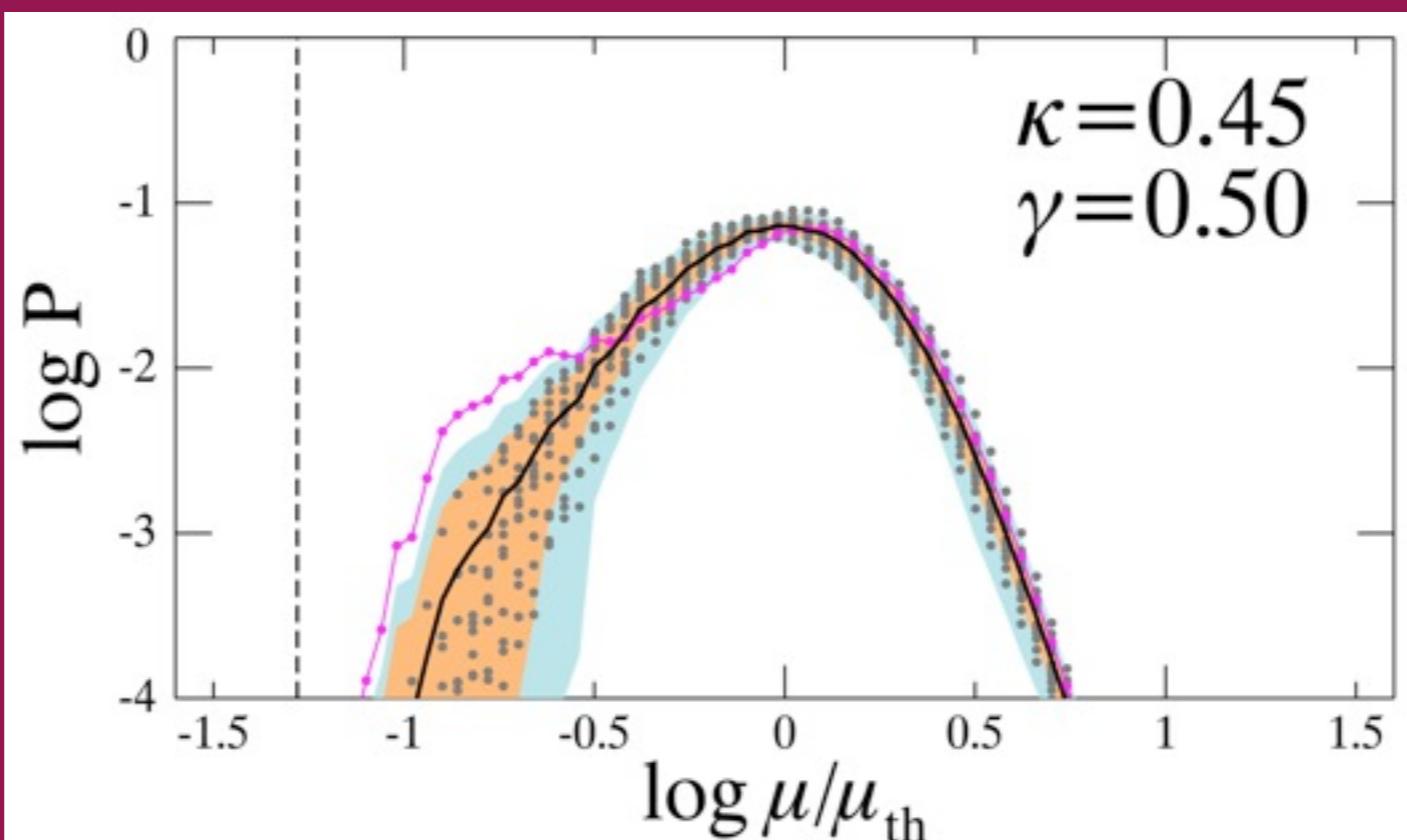
$\kappa = 0.45$   
 $\gamma = 0.50$



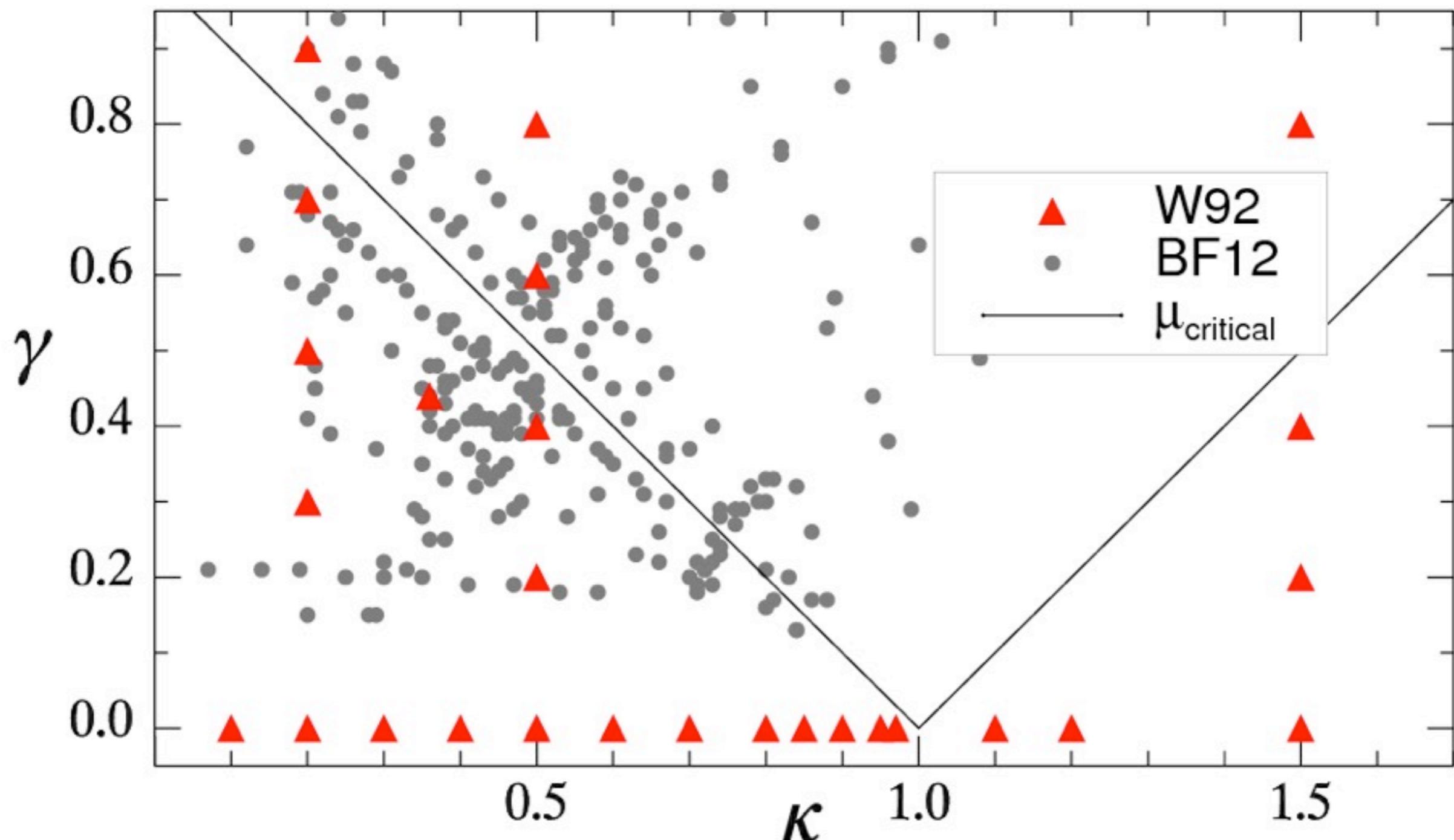
# Magnification Probability Distribution (MPD)



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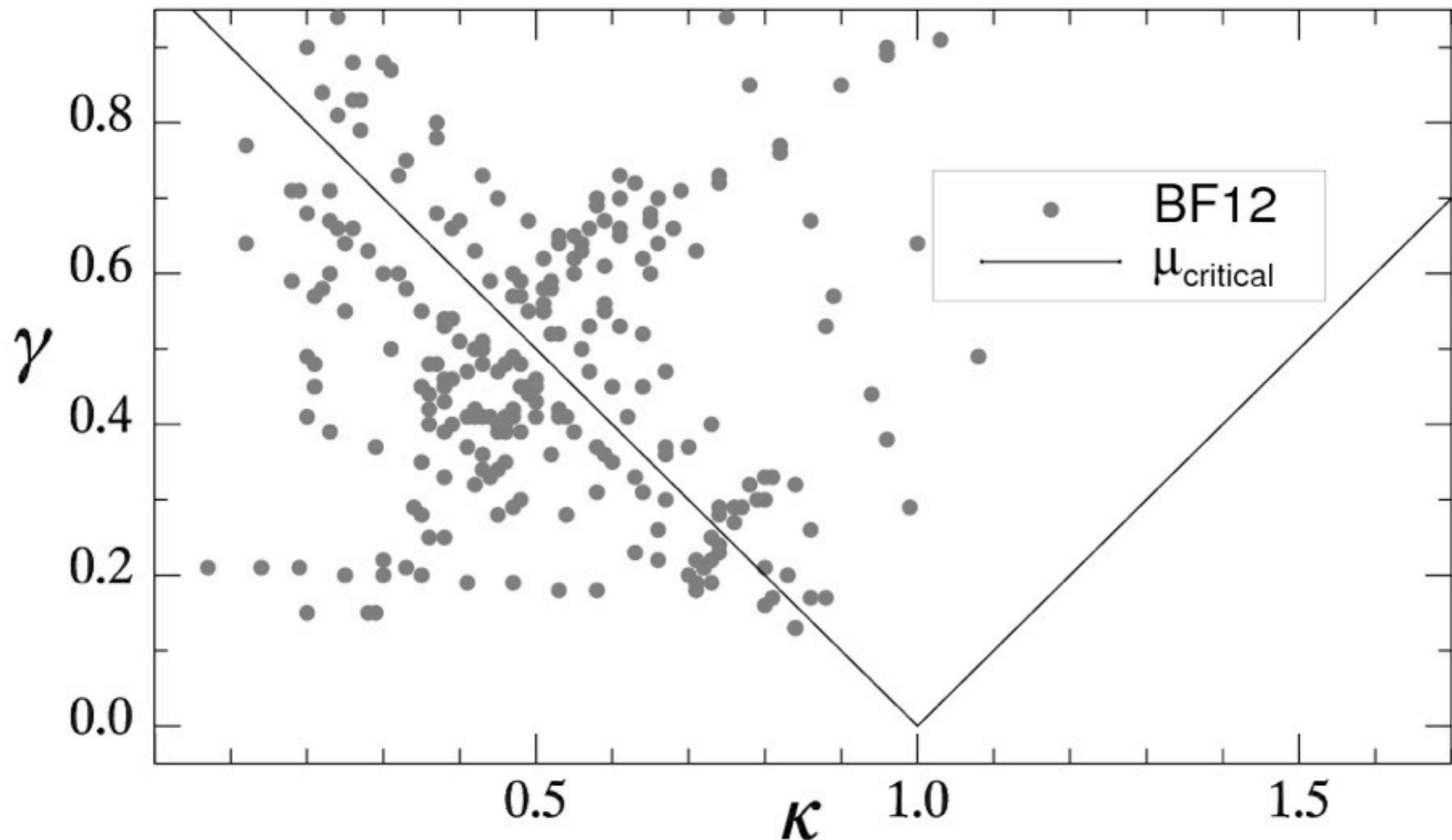
# $\kappa, \gamma$ parameter space



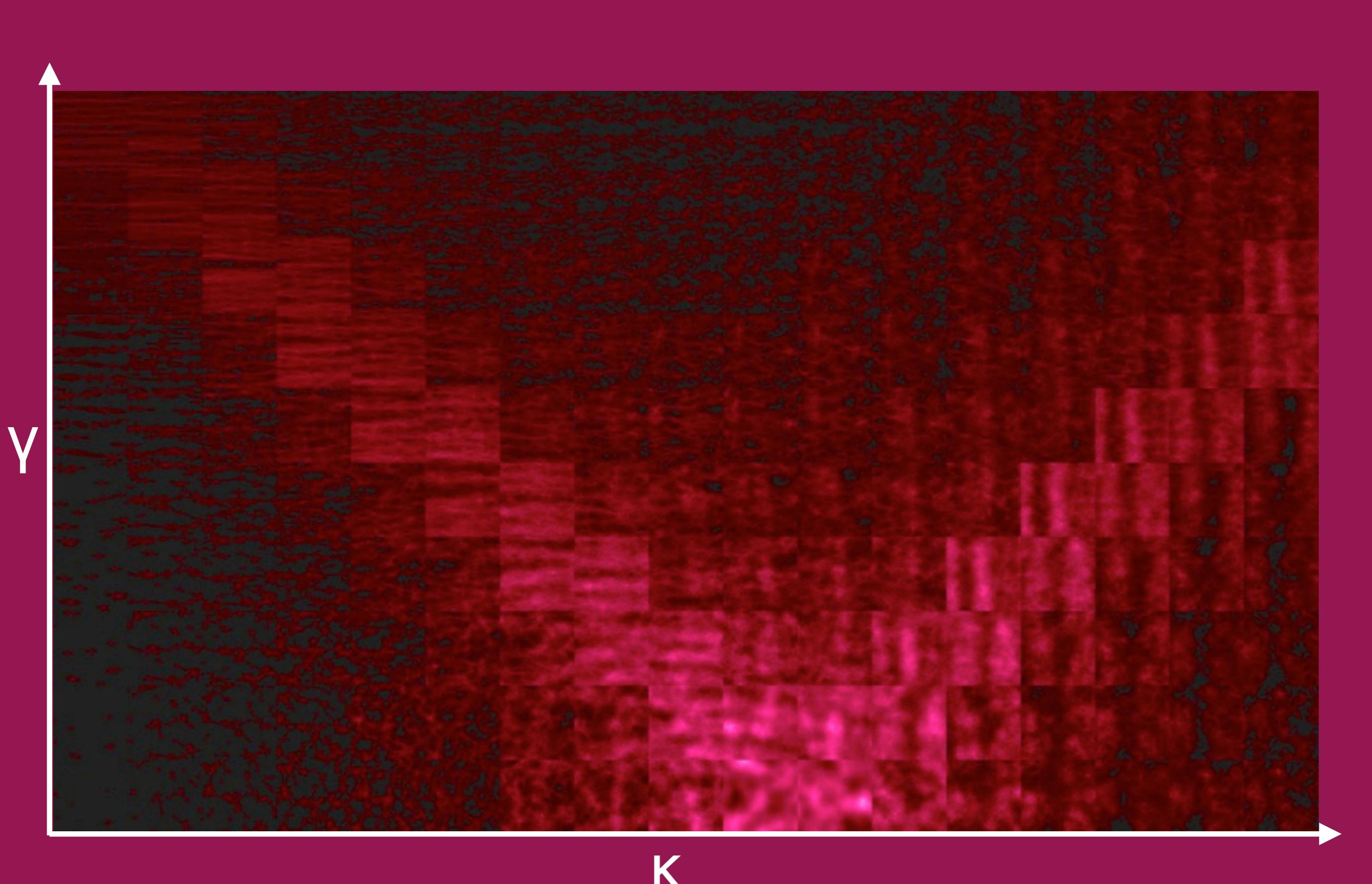
23 systems  
256  $\kappa, \gamma$  pairs

27  $\kappa, \gamma$  pairs  
64 individual maps

# $\kappa, \gamma$ parameter space



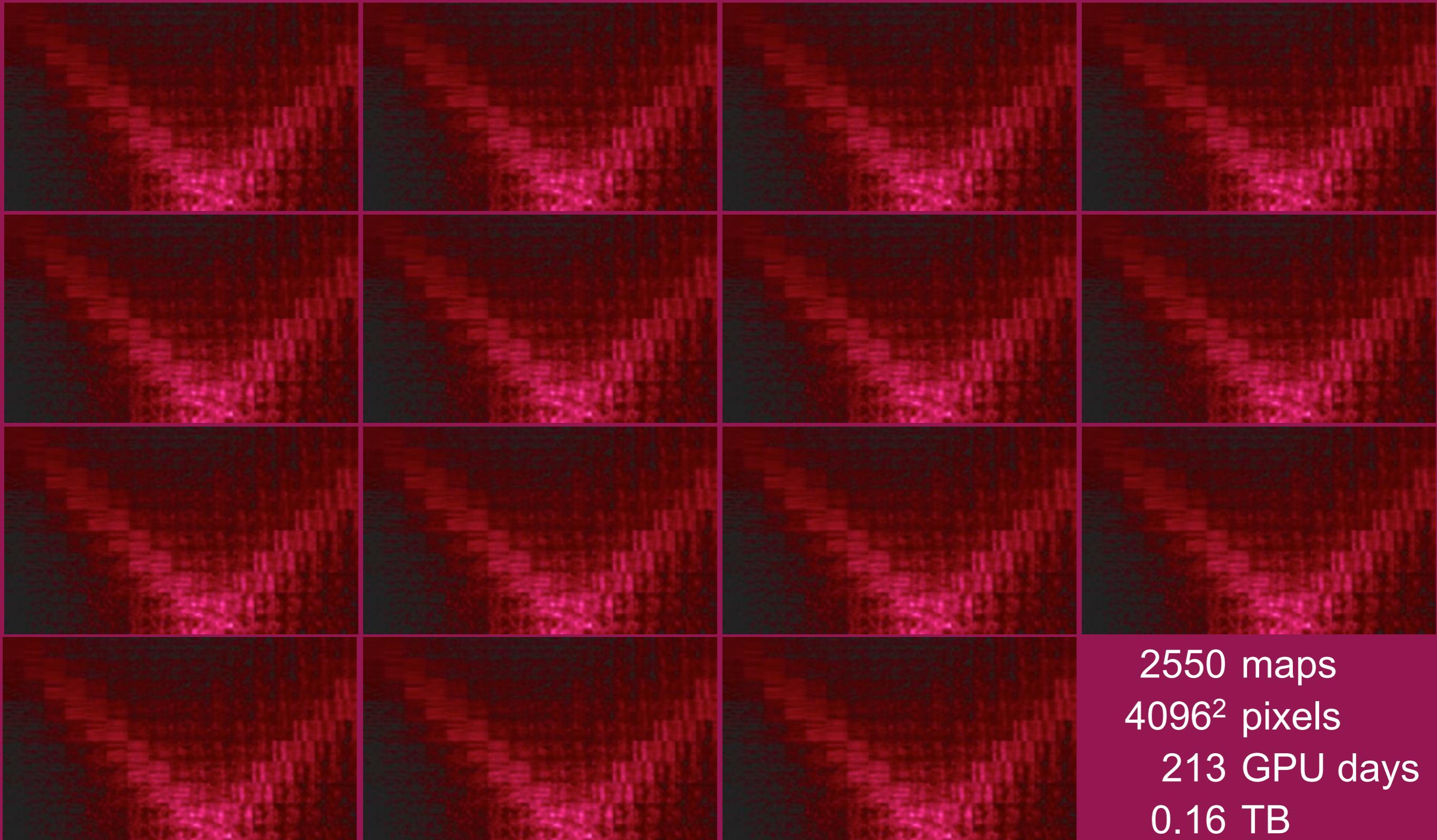
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K

170 maps, 14 GPU days

# GERLUMPH 0: 15 different random realizations



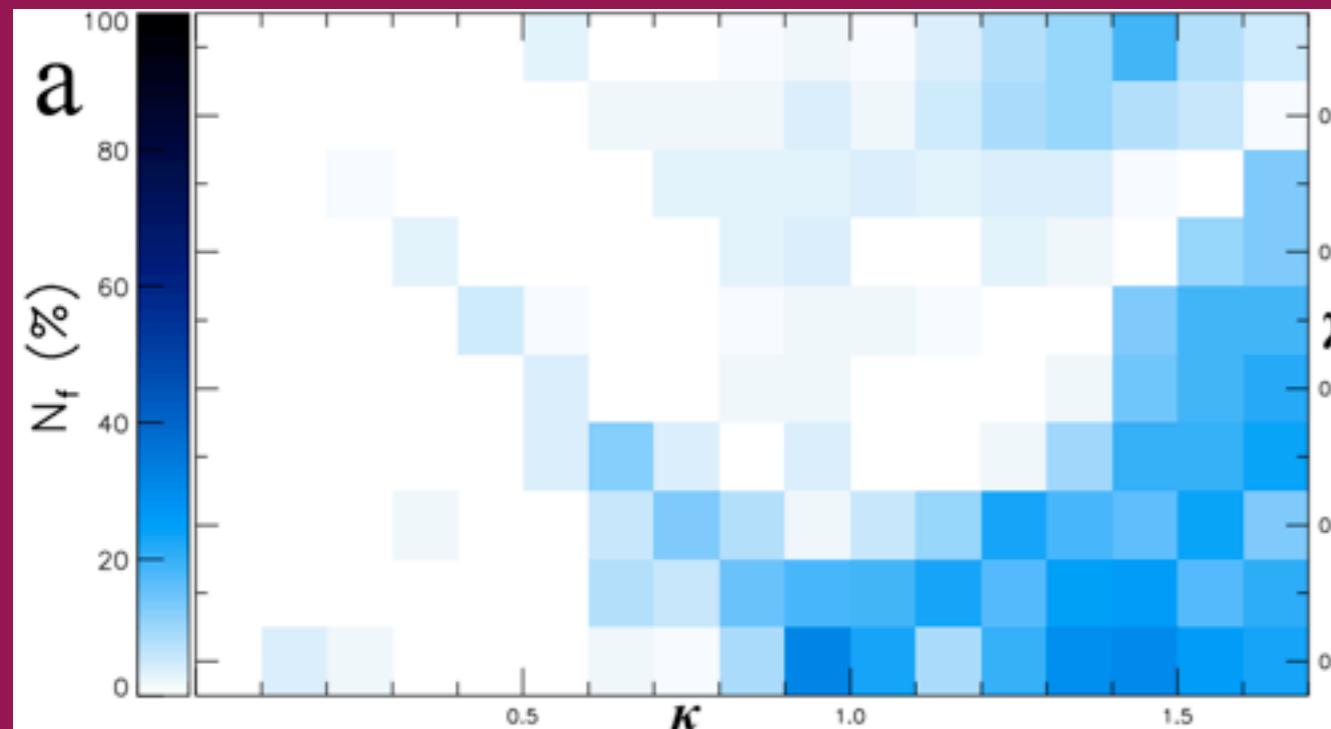


Vernardos & Fluke 2013

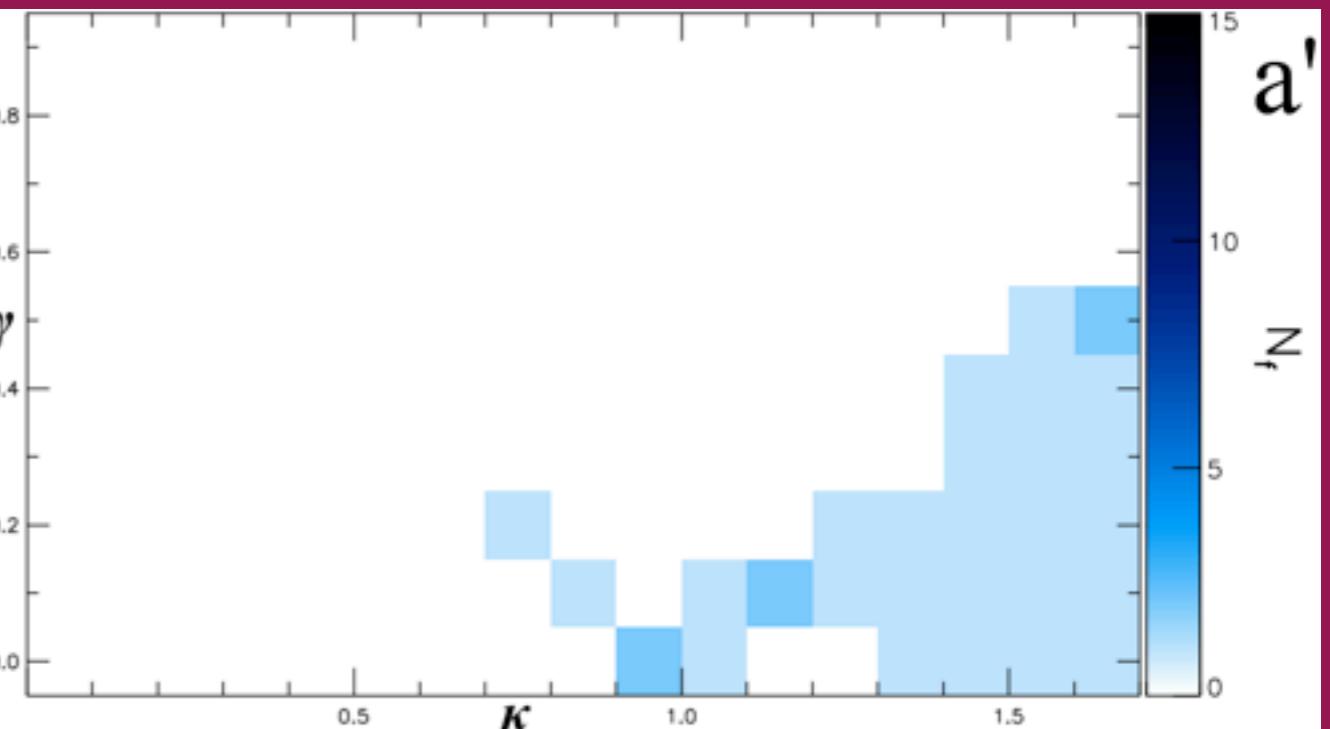
# Kolmogorov-Smirnov tests

Null hypothesis : same distributions  
failed test : p value < 0.05

Pairs of MPDs



MPDs and the mean

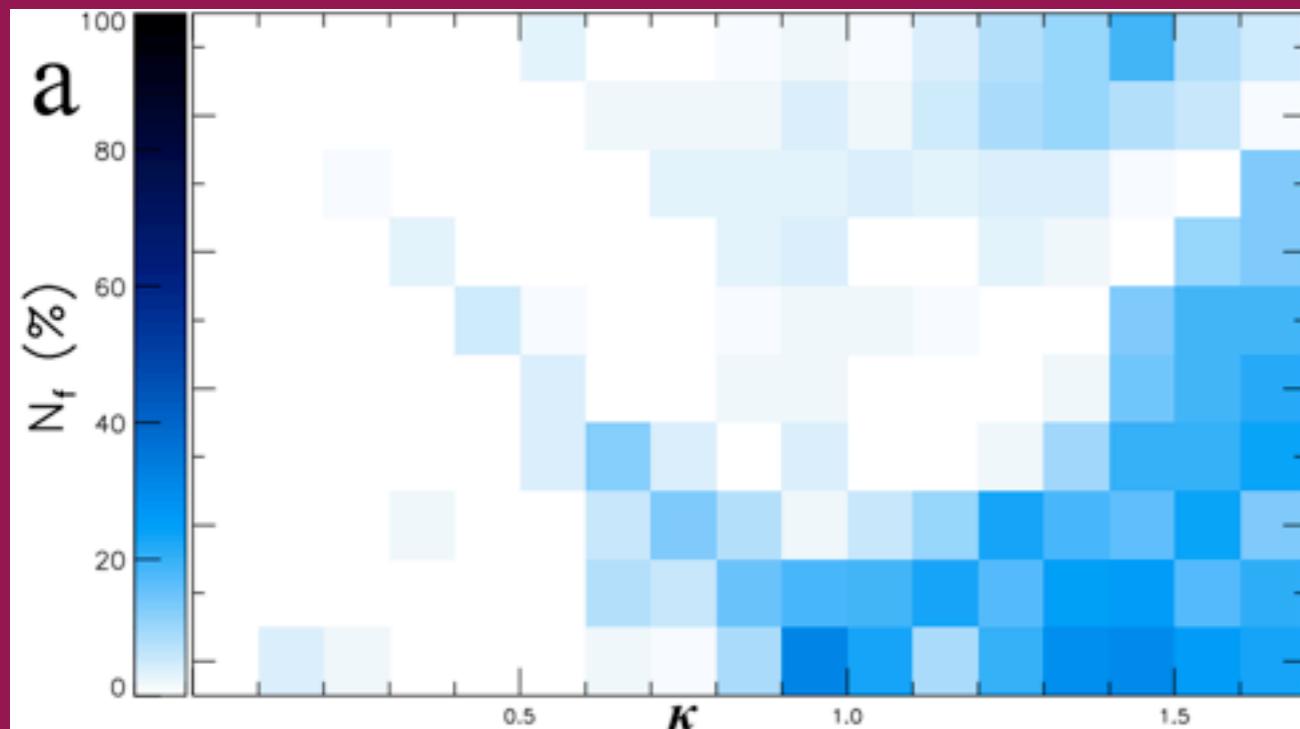


Vernardos & Fluke 2013

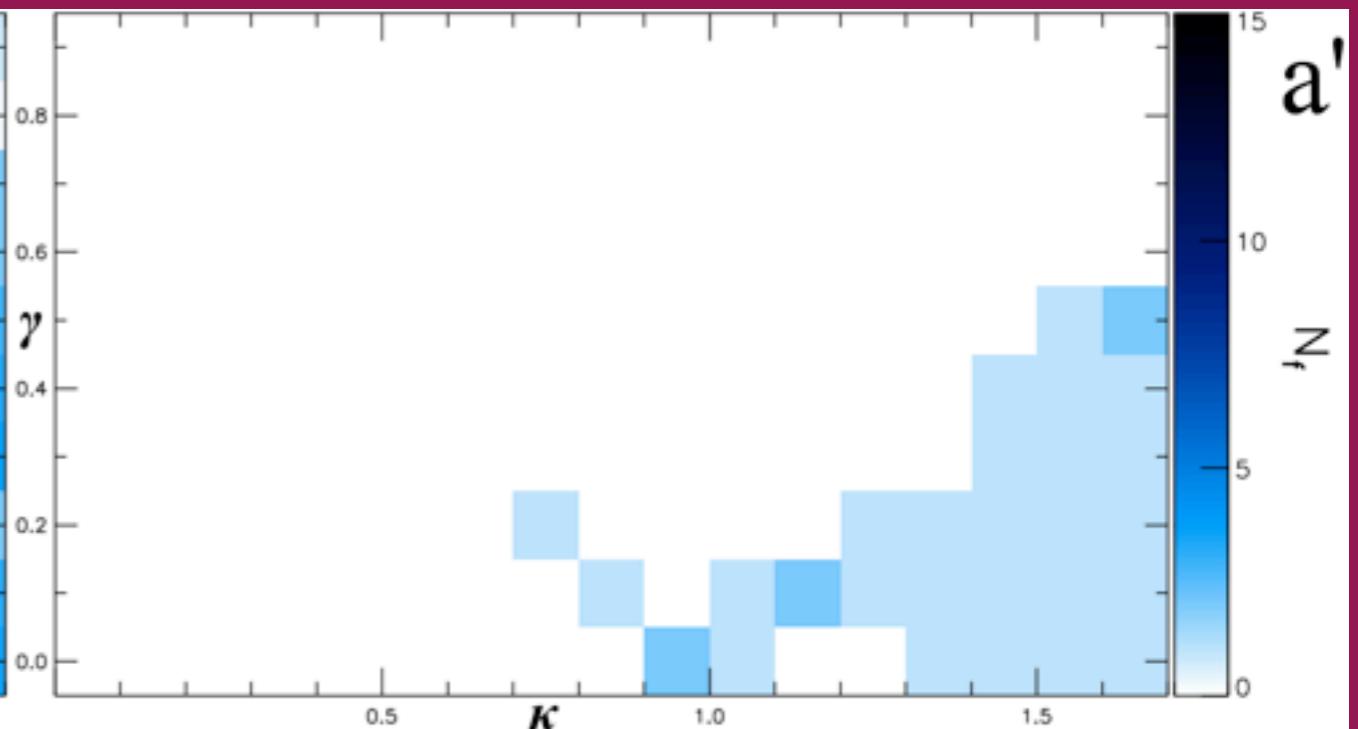
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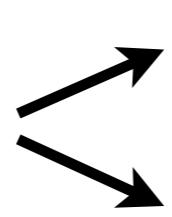
MPDs and the mean



Vernardos & Fluke 2013

*There are areas of parameter space where one map may not be representative*

convergence,  $\kappa$  :



compact  
smooth

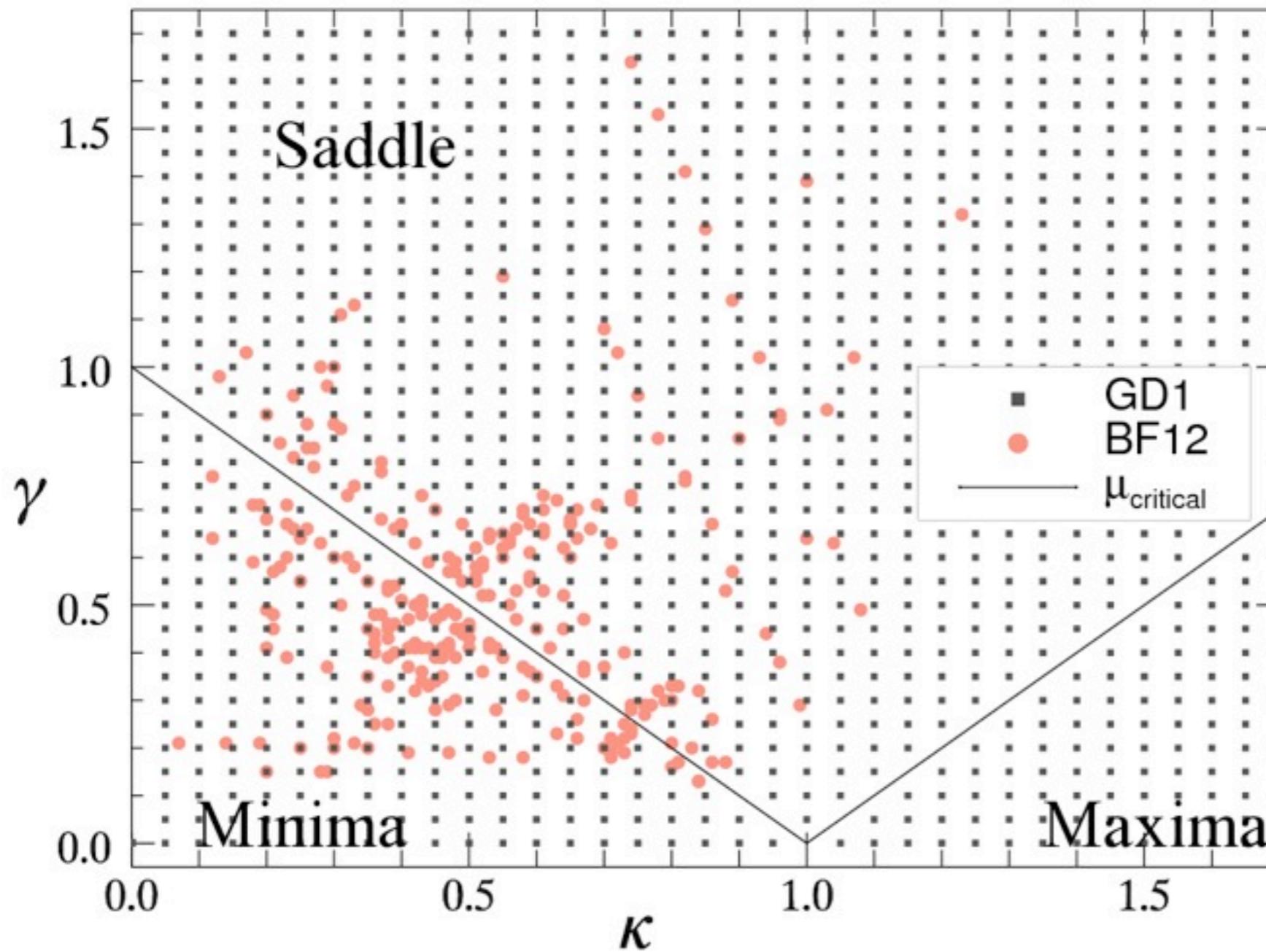
extra parameter: smooth matter fraction

# GERLUMPH I: Compact and smooth matter

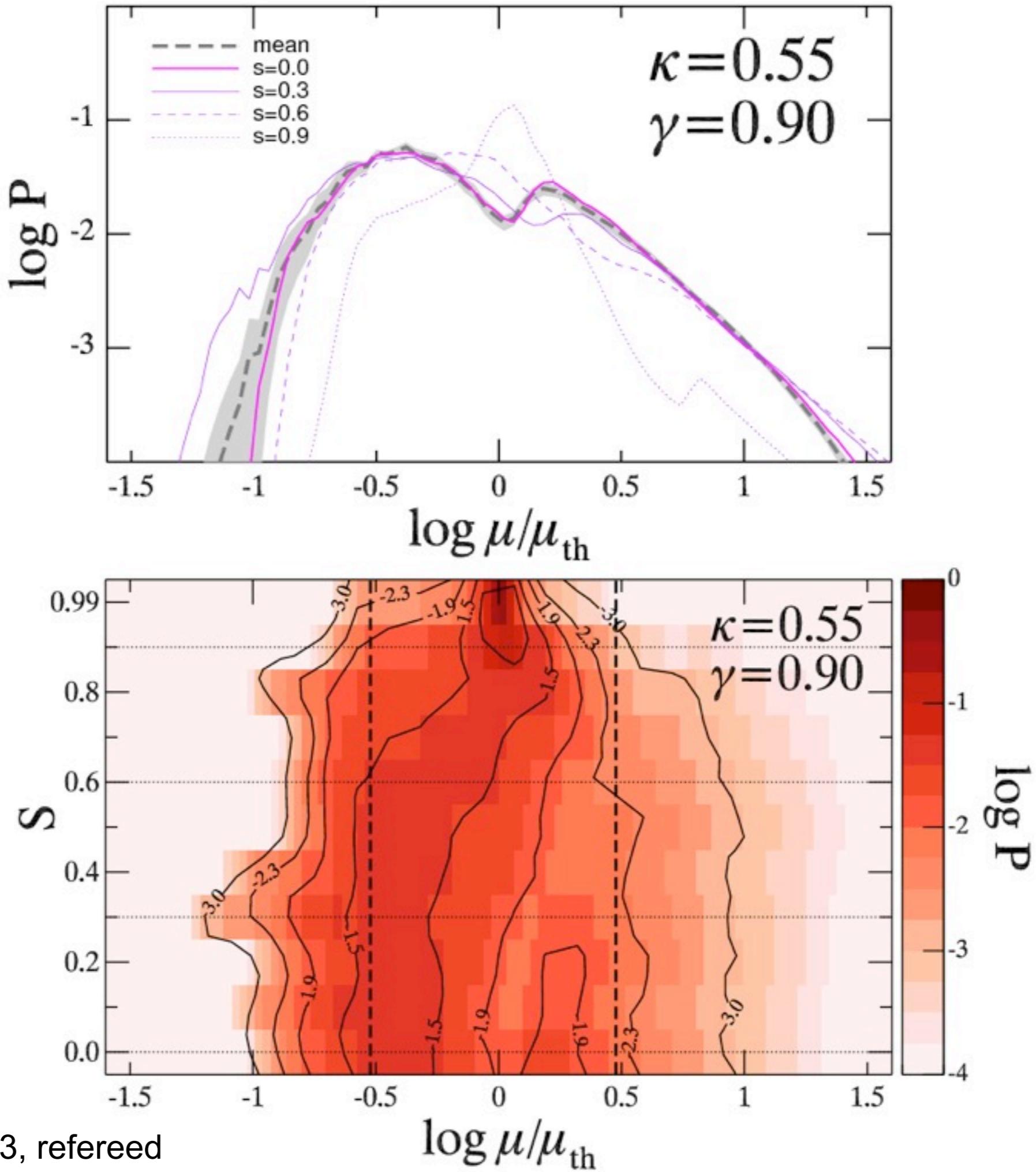
convergence,  $\kappa$  :

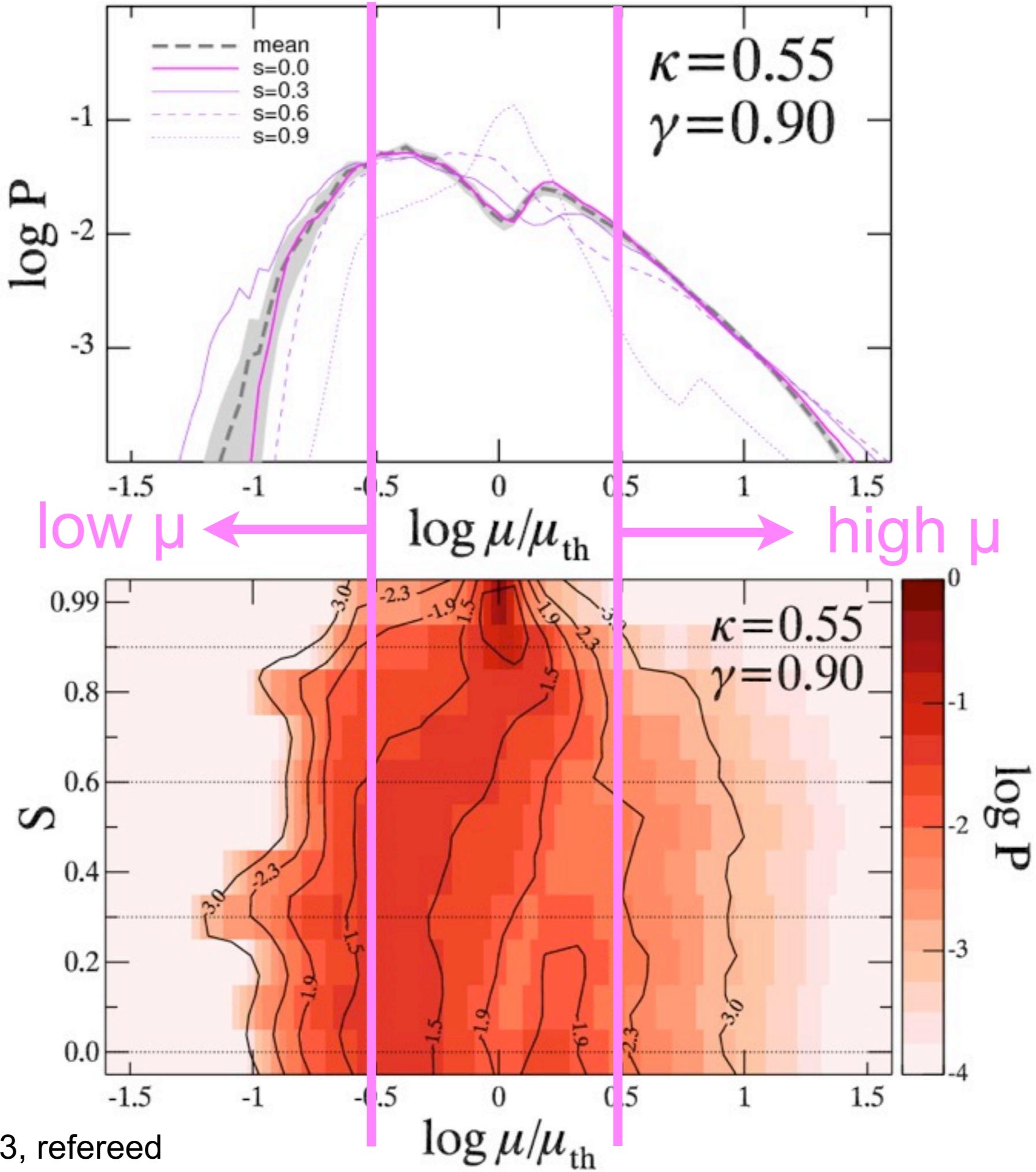
compact  
smooth

extra parameter: **smooth matter fraction**

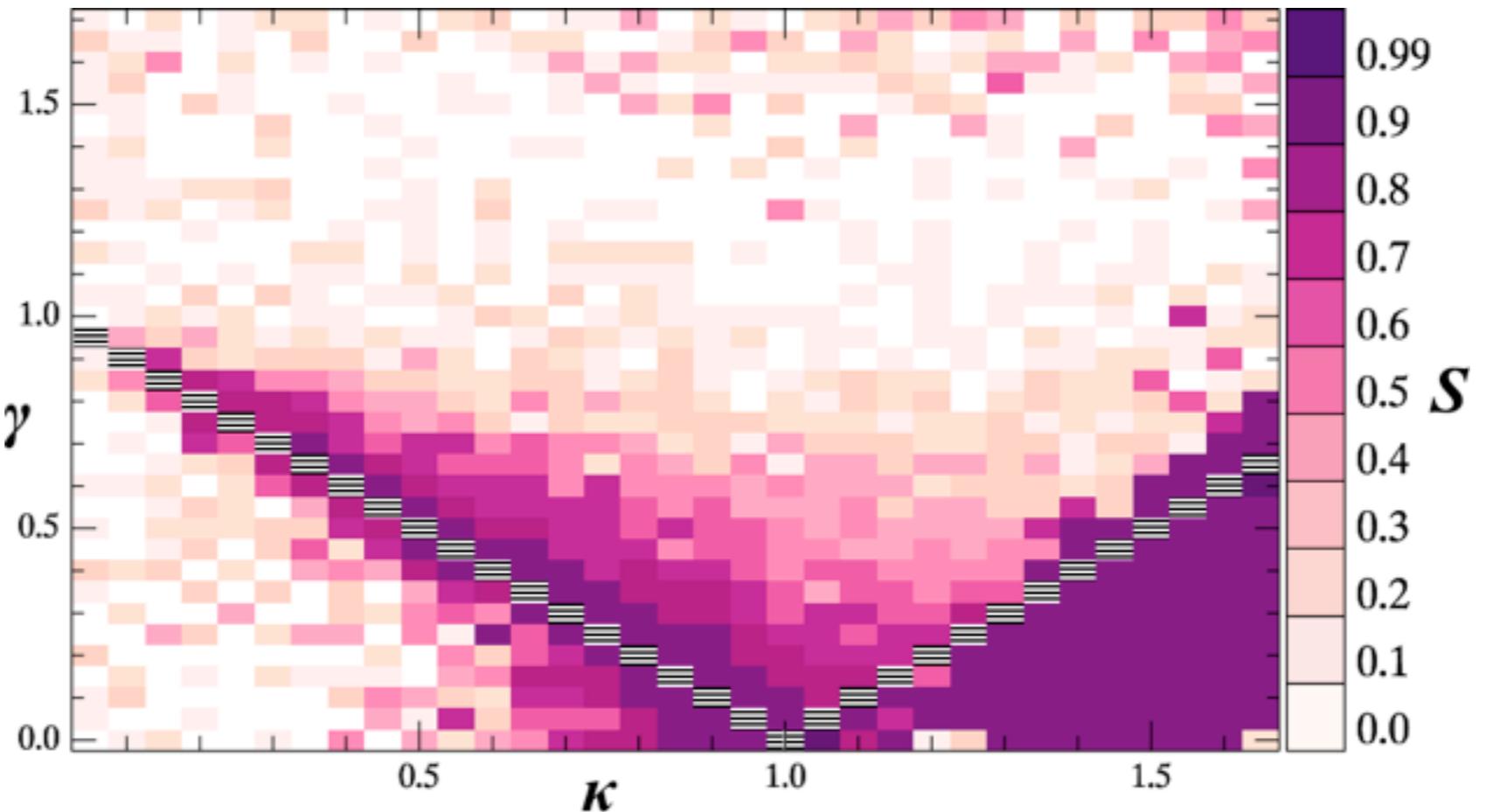


12342 maps  
 $10000^2$  pixels  
2902 GPU days  
4.5 TB

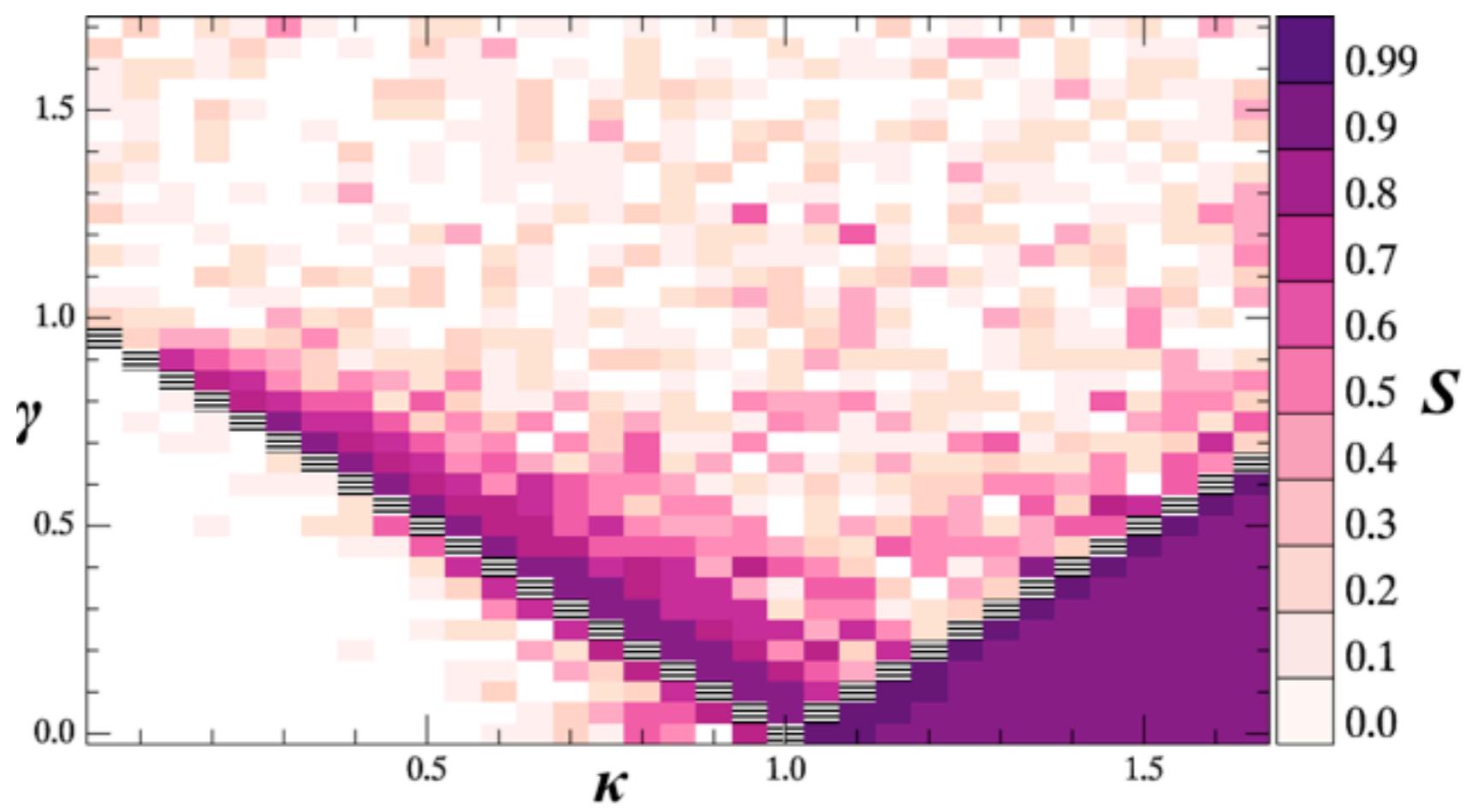




$P_{\max}$  for high  $\mu$



$P_{\max}$  for low  $\mu$



What's next?

	GERLUMPH 0	GERLUMPH I	GERLUMPH II
( $\kappa, \gamma$ )	170	1122	3753
s	1	11	11
lens positions	15	1	1
resolution	4096	10000	10000
total	<b>2550</b>	<b>12342</b>	<b>45705</b>

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## GERLUMPH I

*Can microlensing constrain accretion discs in the future?  
(predictions in the  $\kappa, \gamma$  parameter space)*

## GERLUMPH II

*Is all of quasar microlensing correct?  
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total	<b>2550</b>	<b>12342</b>	<b>45705</b>
status	complete	complete	<i>ongoing</i>
size (TB)	0.16	4.5	16.9
GPU time	213 days	2902 days	<i>15805 days</i>

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(predictions in the  $\kappa, \gamma$  parameter space)*

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*Is all of quasar microlensing correct?  
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*eResearch*



## OBSERVATION

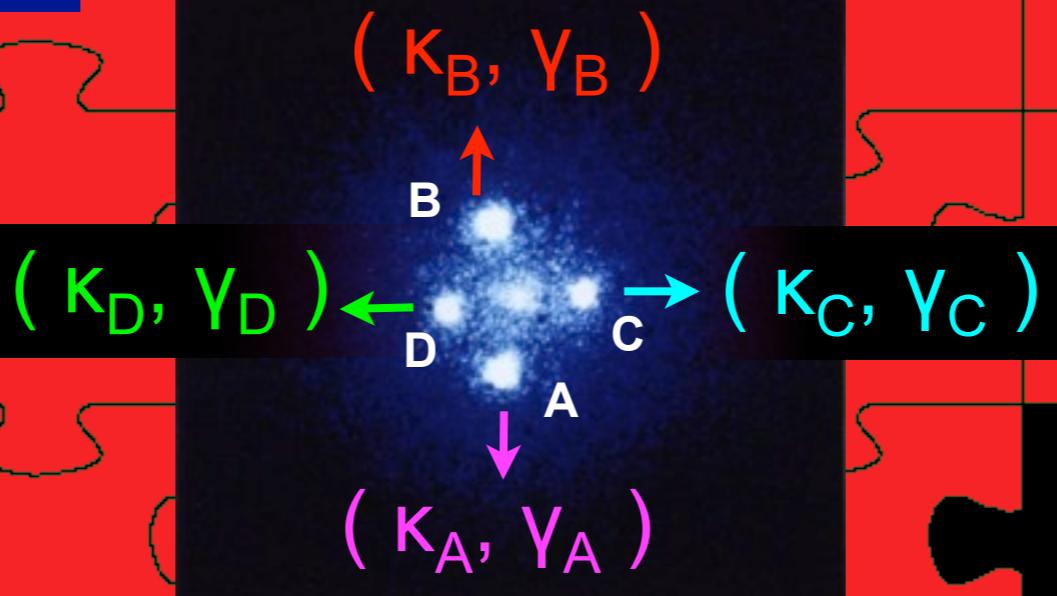
QSO-2237

Image : HST NASA/ESA

## MACRO-MODELS



## Calculate $\kappa$ and $\gamma$



## OBSERVATION

QSO-2237

Image : HST NASA/ESA

## MACRO-MODELS

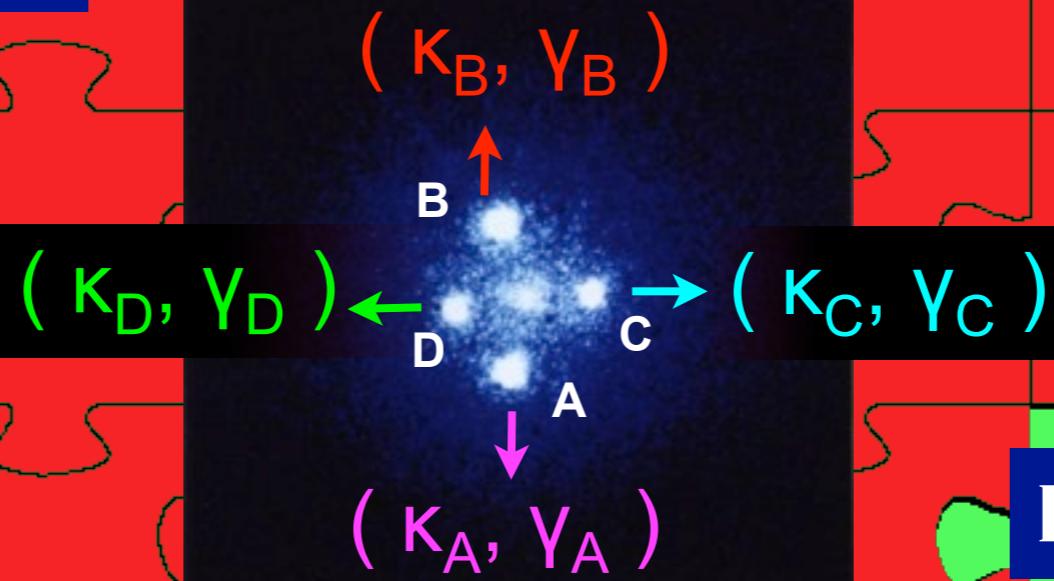


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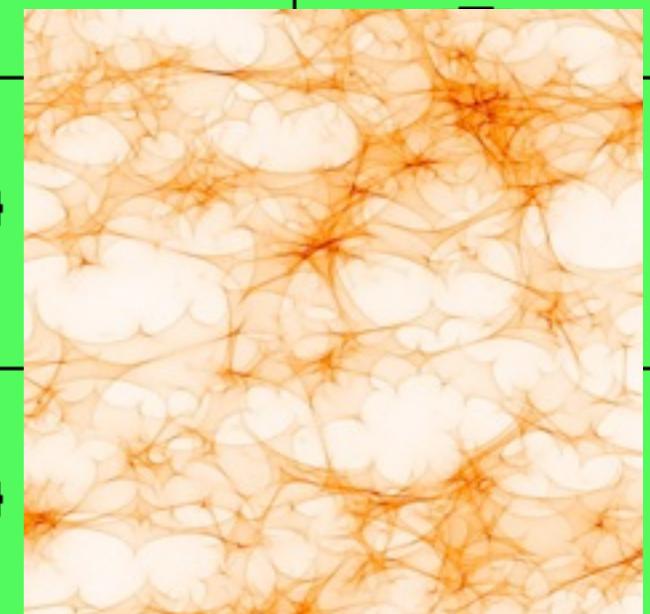


## MICRO-MODELS

PER ( $\kappa, \gamma$ )

$$y = \begin{pmatrix} 1 - \gamma & 0 \\ 0 & 1 + \gamma \end{pmatrix} x - \kappa_s x - \sum_{i=1}^{N_l} m_i \frac{(x - x_i)}{|x - x_i|^2}$$

GERLUMPH



## MACRO-MODELS



## Calculate $\kappa$ and $\gamma$

(  $\kappa_B, \gamma_B$  )

B

(  $\kappa_D, \gamma_D$  )

(  $\kappa_A, \gamma_A$  )

D

← (  $\kappa_C, \gamma_C$  ) →

C

A

## MICRO-MODELS

PER ( $\kappa, \gamma$ )

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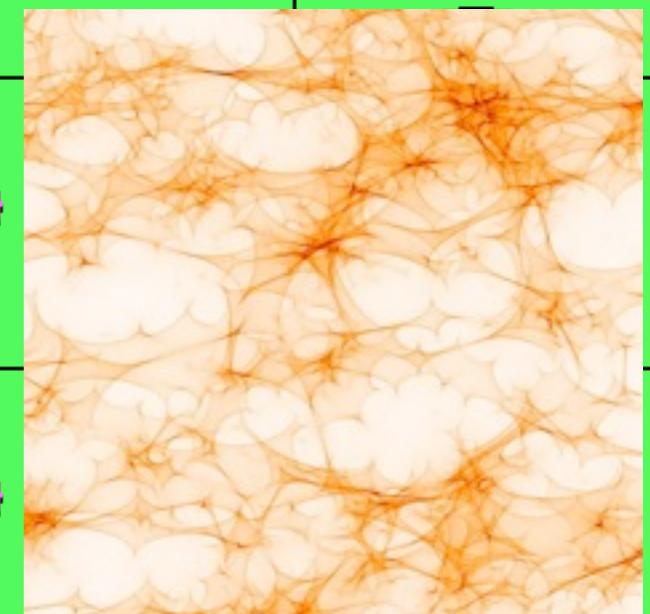
QSO-2237

## QUASAR-MODELS

*Microlensing and  
quasar accretion disks*

- Light-curve analysis
- Chromatic lensing

## GERLUMPH



## MACRO-MODELS

Calculate  $\kappa$  and  $\gamma$

(  $\kappa_B, \gamma_B$  )

B  
↑

(  $\kappa_D, \gamma_D$  )

D  
←

C  
→

(  $\kappa_C, \gamma_C$  )

A  
↓

(  $\kappa_A, \gamma_A$  )

## MICRO-MODELS

PER ( $\kappa, \gamma$ )

$$y = \begin{pmatrix} 1 - \gamma & 0 \\ 0 & 1 + \gamma \end{pmatrix} x - \kappa_s x - \sum_{i=1}^{N_l} m_i \frac{(x - x_i)}{|x - x_i|^2}$$

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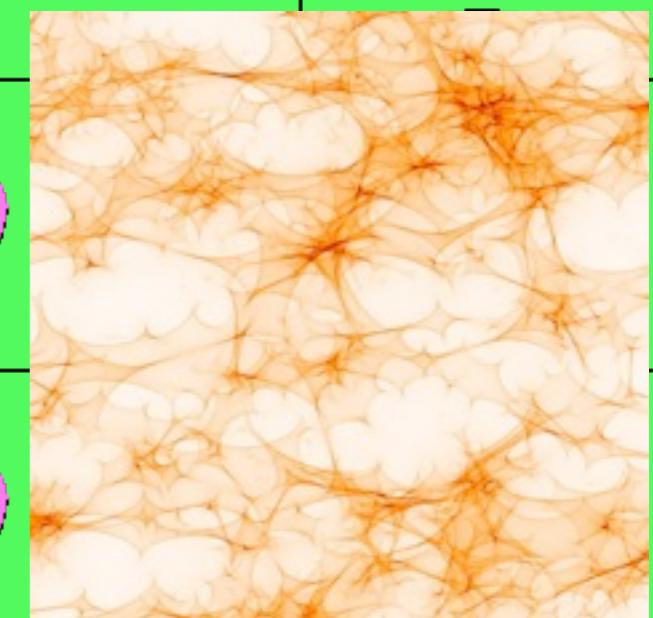
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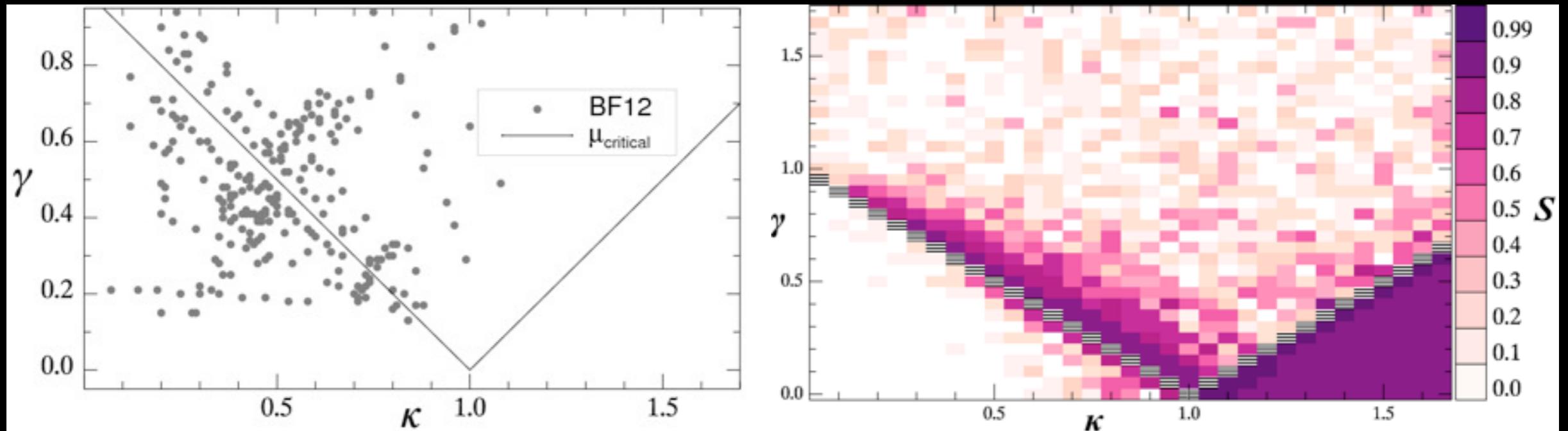
- Light-curve analysis
- Chromatic lensing

## GERLUMPH



# Conclusions

## Microlensing parameter space



a few systems now (23), thousands in the future

## eResearch

Much easier to test a variety of alternative accretion disc/SMBH models  
once we have statistically significant samples

*gerlumph.swin.edu.au*

*Σας ευχαριστώ!*

# Science with magnification maps: *Light-curve analysis*

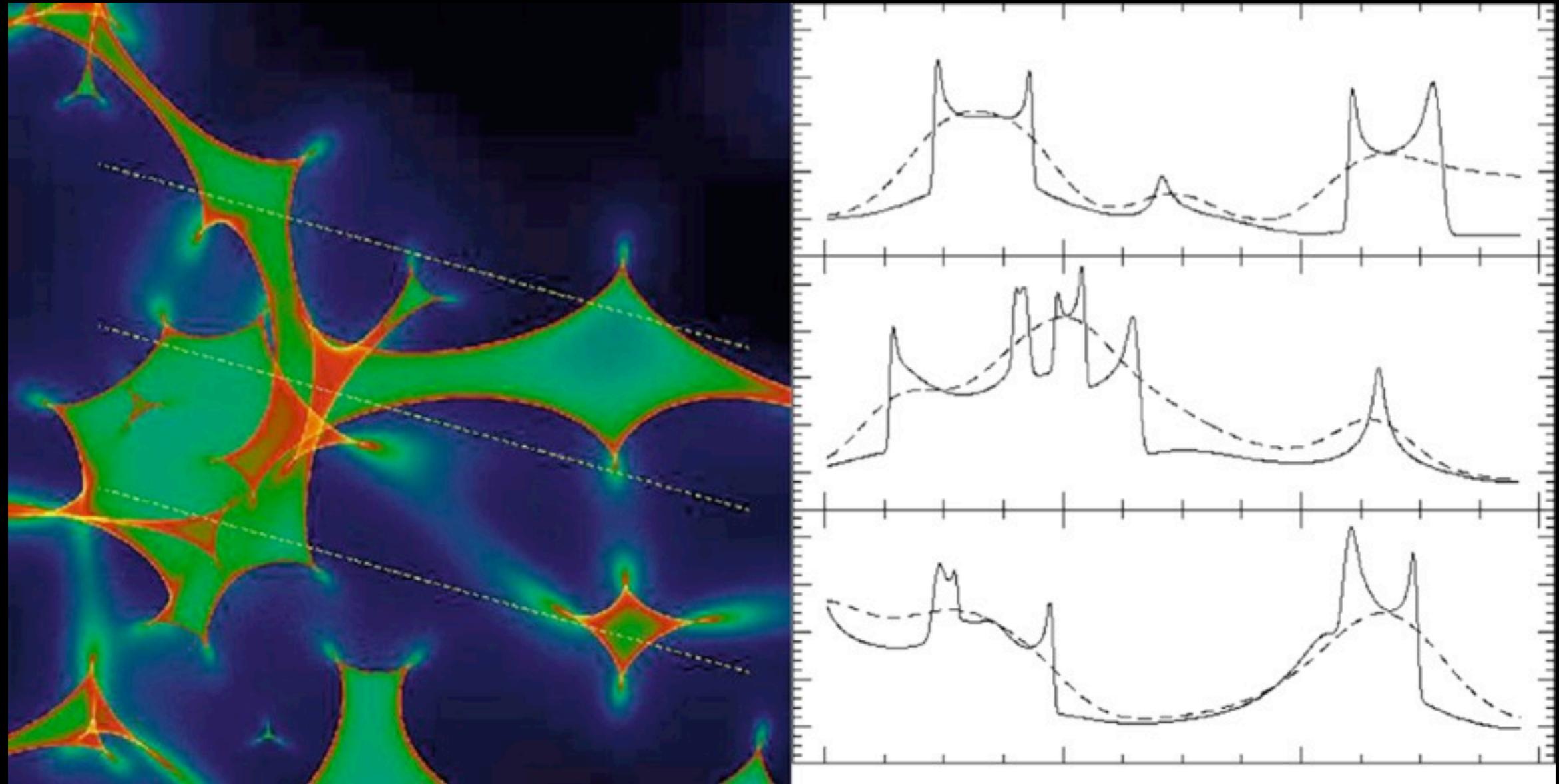


Figure : Schmidt & Wambsganss 2010

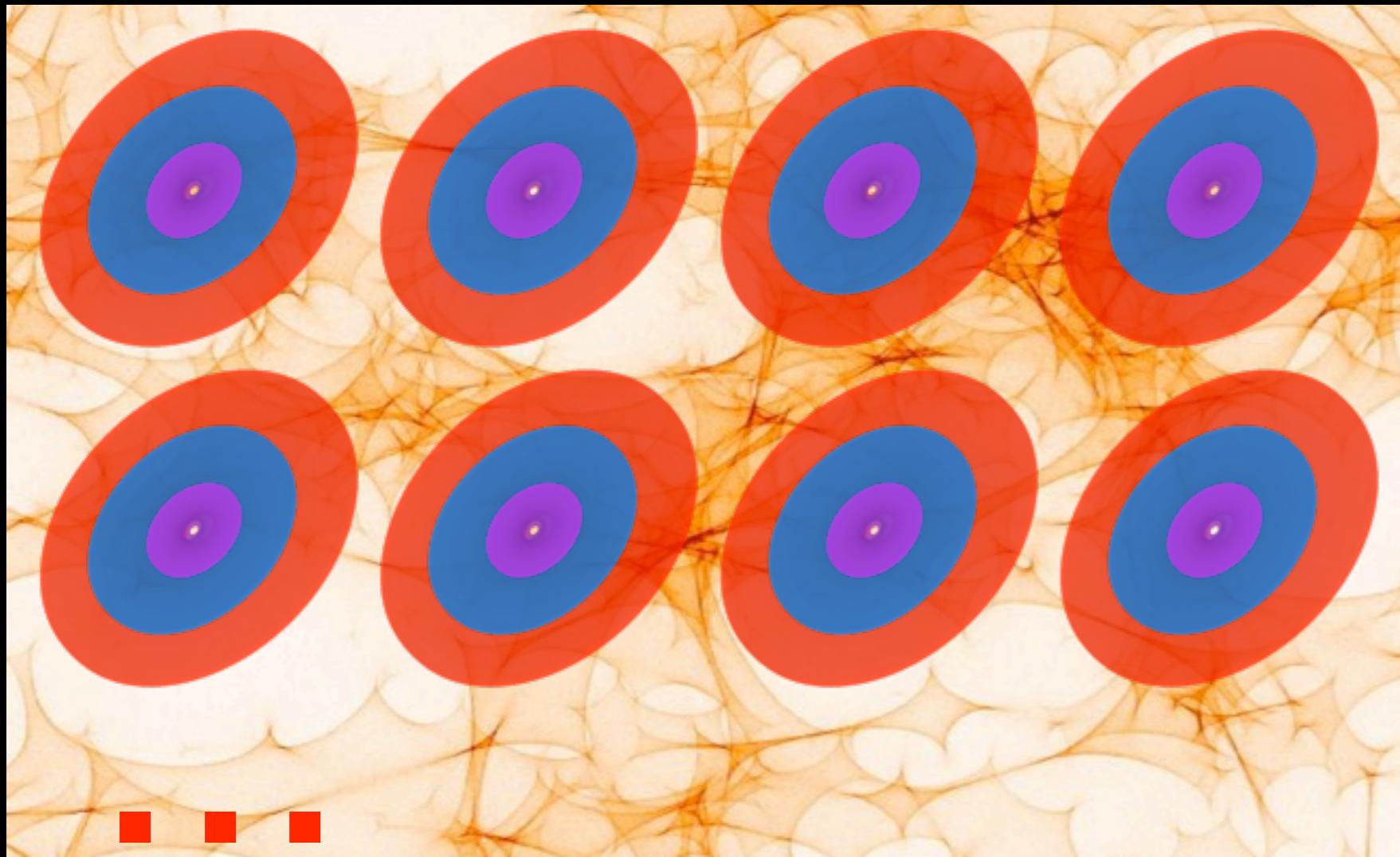
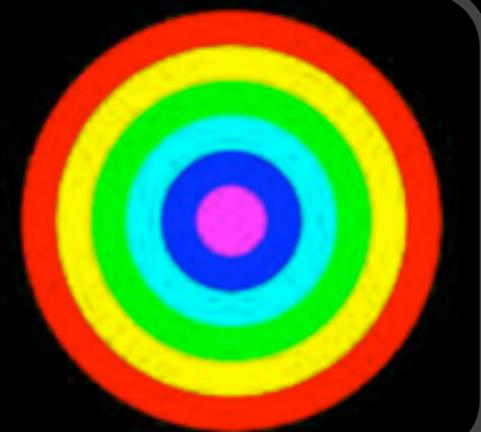
*Smaller sources appear more magnified*

# Science with magnification maps: *Chromatic lensing*

$$\lambda_1, \lambda_2, \lambda_3 \\ \downarrow \\ R_1, R_2, R_3$$

*Thin disk model*  
Shakura Sunyaev 1973

$$T \propto R^\beta, \beta = -3/4$$



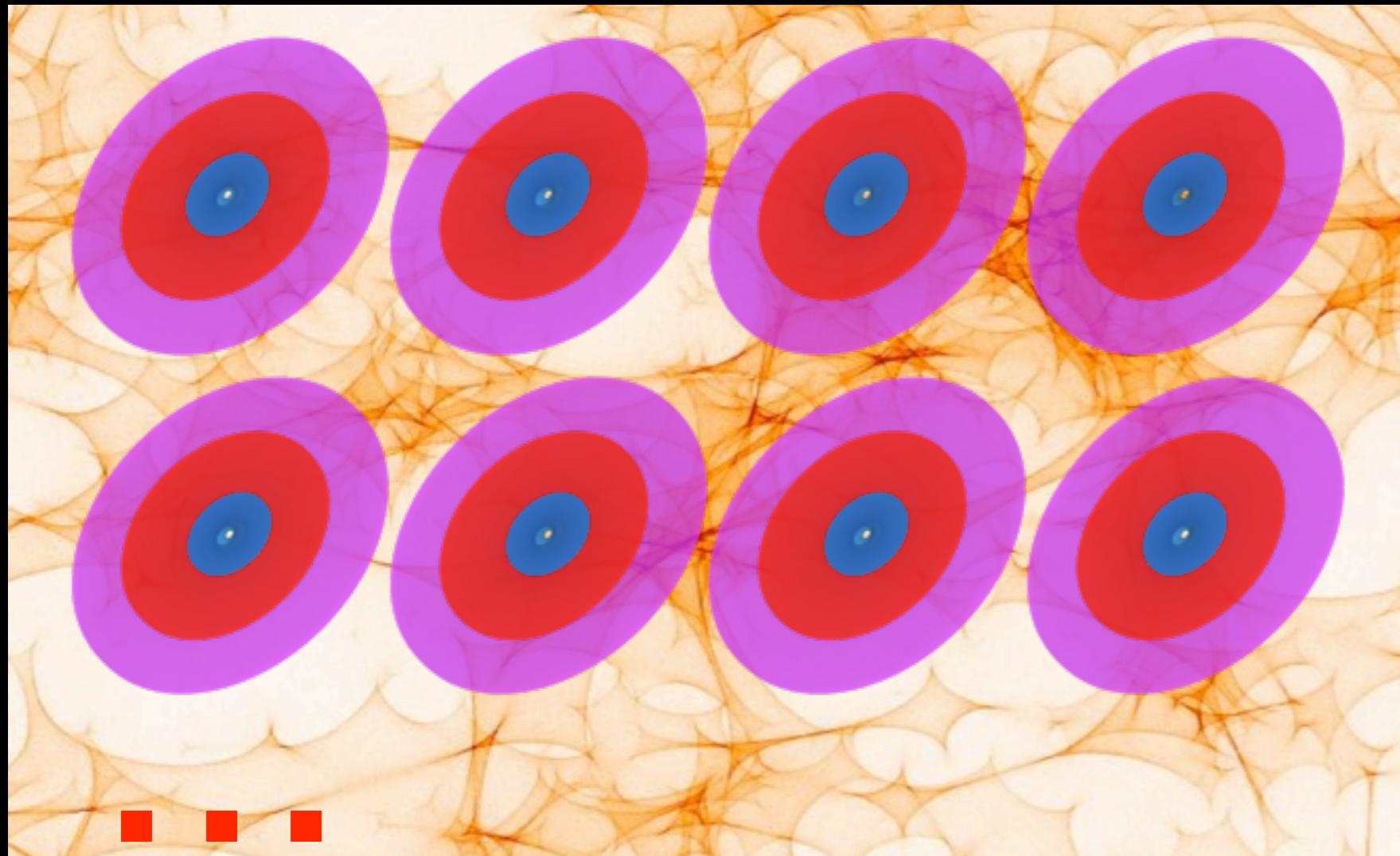
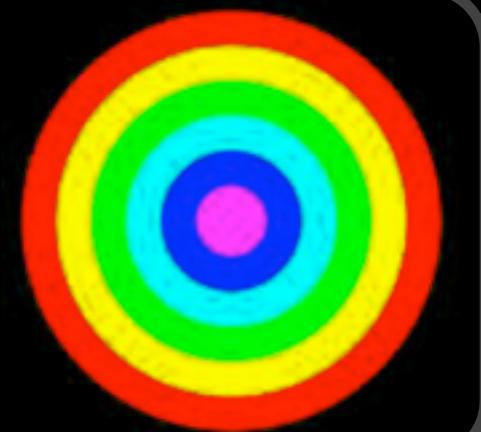
$$p(F_{12}) \\ = p(F_{13}) \\ p(F_{23})$$

# Science with magnification maps: *Chromatic lensing*

$$\lambda_1, \lambda_2, \lambda_3 \\ \downarrow \\ R_1, R_2, R_3$$

*Thin disk model*  
Shakura Sunyaev 1973

$$T \propto R^\beta, \beta = -3/4$$

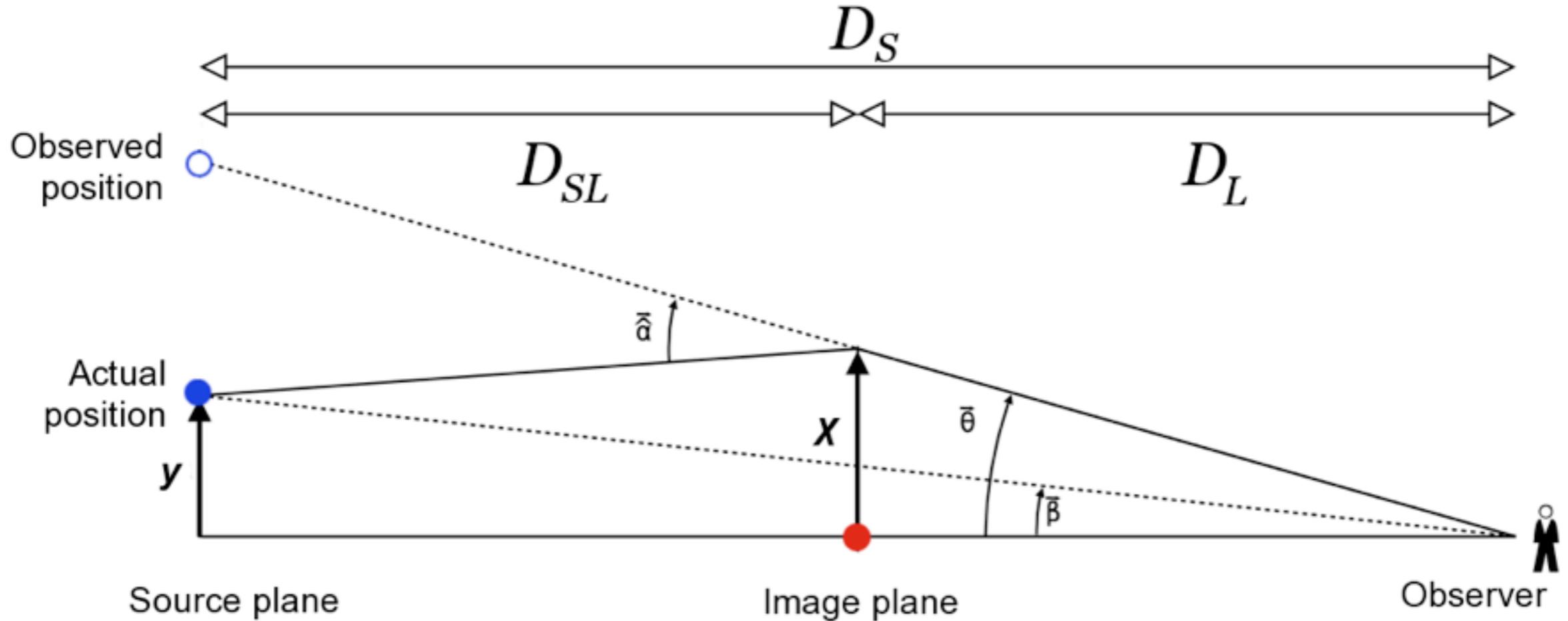


$$p'(F_{12}) \\ = p'(F_{13}) \\ p'(F_{23})$$



$$\pmb{y} = \begin{pmatrix} 1-\gamma & 0 \\ 0 & 1+\gamma \end{pmatrix}\pmb{x} - \kappa_s\pmb{x} - \sum_{i=1}^{N_l} m_i \frac{(\pmb{x}-\pmb{x}_i)}{|\pmb{x}-\pmb{x}_i|^2}$$

$$R_\lambda^{theory}=9.7\times10^{15}\left(\frac{\lambda_{rest}}{\mu m}\right)^{4/3}\left(\frac{M_{BH}}{10^9 M_\odot}\right)^{2/3}\left(\frac{L}{\eta L_E}\right)^{1/3}cm$$



$$\hat{\alpha}(\theta) = \frac{4GM}{c^2} \frac{1}{\theta}$$

$$\beta(\theta) = \theta - \frac{D_{LS}}{D_L D_S} \frac{4GM}{c^2} \frac{1}{\theta}$$

$$\theta_E = \sqrt{\frac{4GM}{c^2} \frac{D_{LS}}{D_L D_S}} \quad , \quad z_L = 0.5 \\ z_S = 2 \quad H = 50 \text{ km s}^{-1} \text{ Mpc}^{-1} \quad \rightarrow \quad \theta_E = 1.8 \sqrt{\frac{M}{10^{12} M_\odot}} \text{ arcsec} \\ D_{LS} \neq D_S - D_L$$

For objects with  $M \sim M_\odot \Rightarrow \theta_E \sim \mu \text{ arcsec}$ :

**the projected  $R_{\text{Ein}}$  is comparable to the accretion disc size**

# Micro-models

from Macro-models

$\kappa$  : **convergence**  
(compact,smooth)  
 $\gamma$  : **shear**

$$\mathbf{y} = \begin{pmatrix} 1 - \gamma & 0 \\ 0 & 1 + \gamma \end{pmatrix} \mathbf{x} - \kappa_s \mathbf{x} - \sum_{i=1}^{N_l} m_i \frac{(\mathbf{x} - \mathbf{x}_i)}{|\mathbf{x} - \mathbf{x}_i|^2}$$



$N_l$  is of the order of  $10^6$

$$N_l = \frac{\kappa_l S}{\pi \langle M \rangle}$$

$N_l$

has to be solved numerically

*Direct inverse ray-shooting*  
“Ridiculously parallelizable problem”

+ GPUs

