

# **The importance of inner boxiness for understanding barred galaxies Dynamics**

Panos Patsis

RCAAM

(results from recent work with M. Katsanikas and L. Tsigaridi)

# Bars

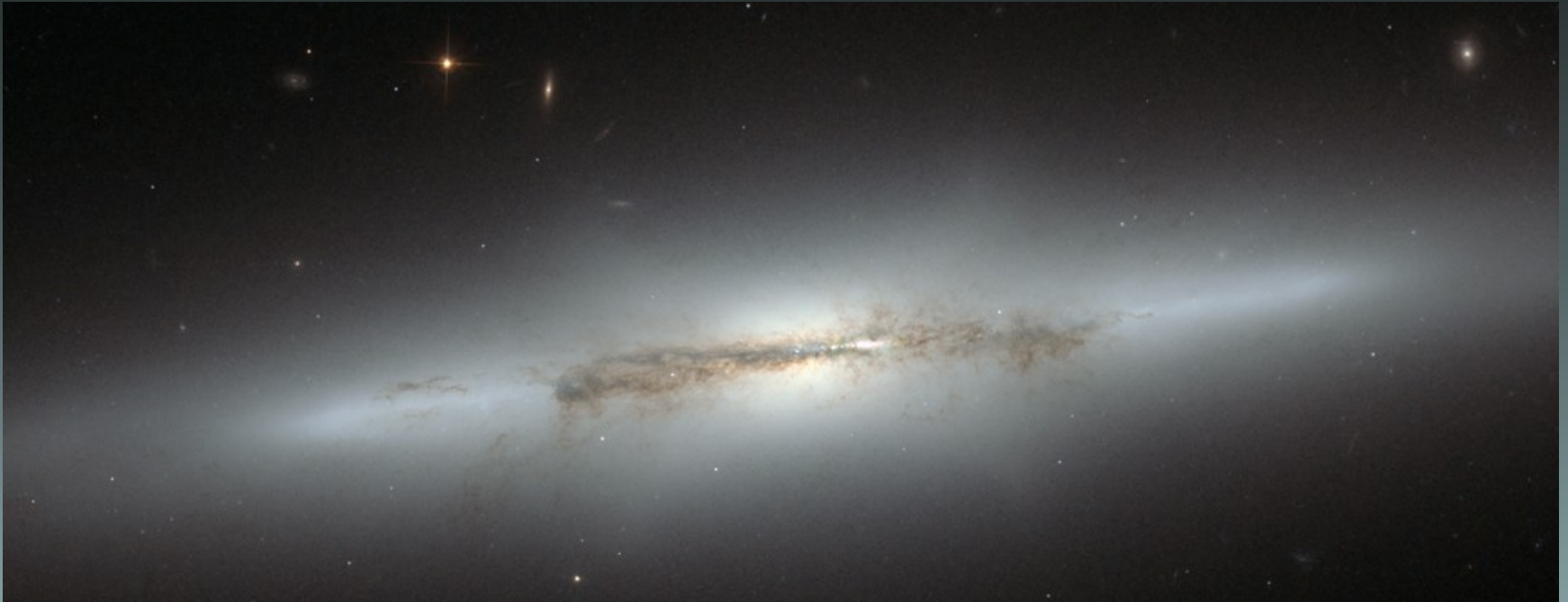
- NGC 1300 (VLT, HAWK-I)



# Bars edge-on: Boxy, Peanut-shaped bulges

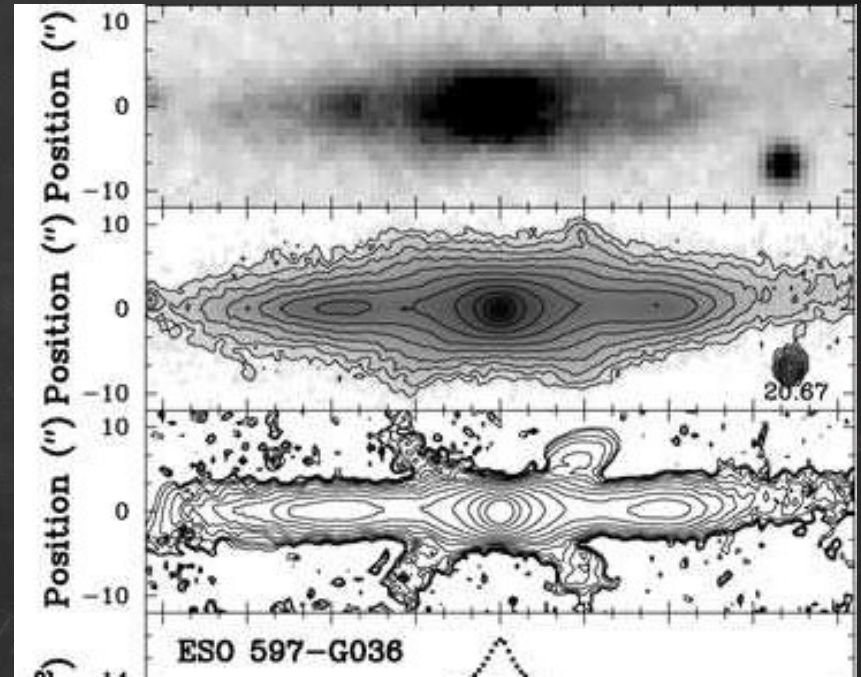
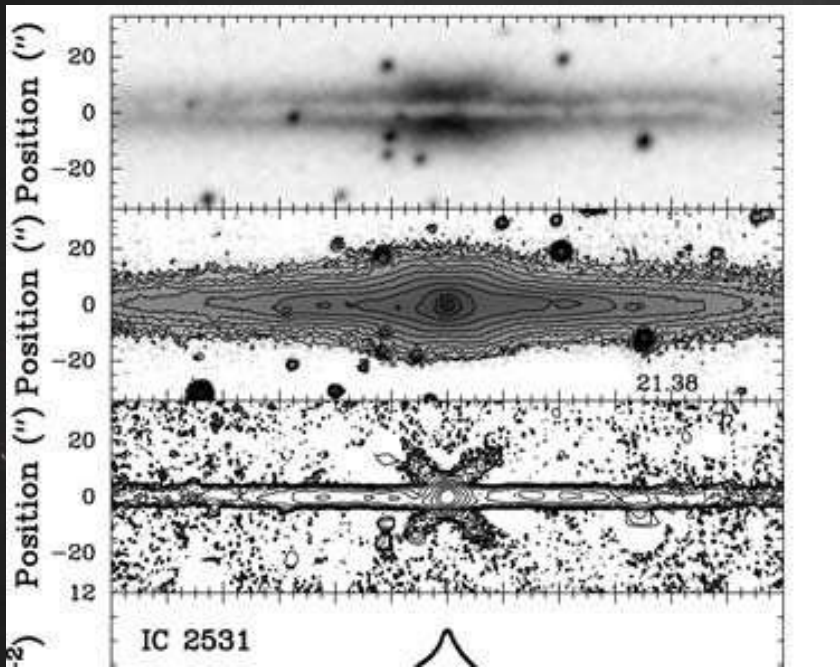


NGC 4710,  $\alpha=12^{\text{h}} 49^{\text{m}} 38.9$  ,  $\delta=+15^{\circ} 9' 56''$

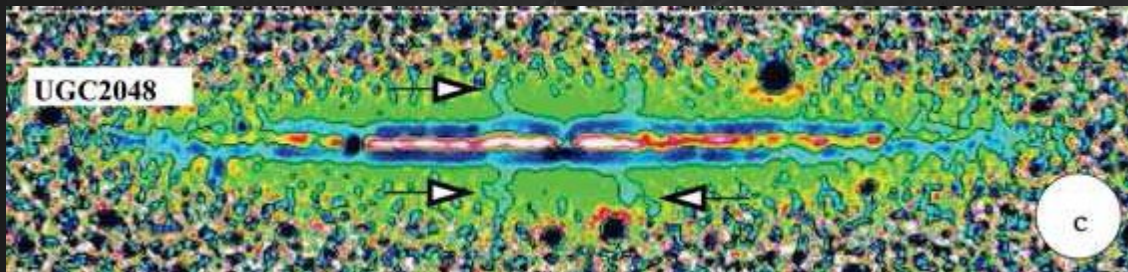


This natural-color photo was taken with the Hubble Space Telescope's Advanced Camera for Surveys on January 15, 2006

# CX vs OX profiles

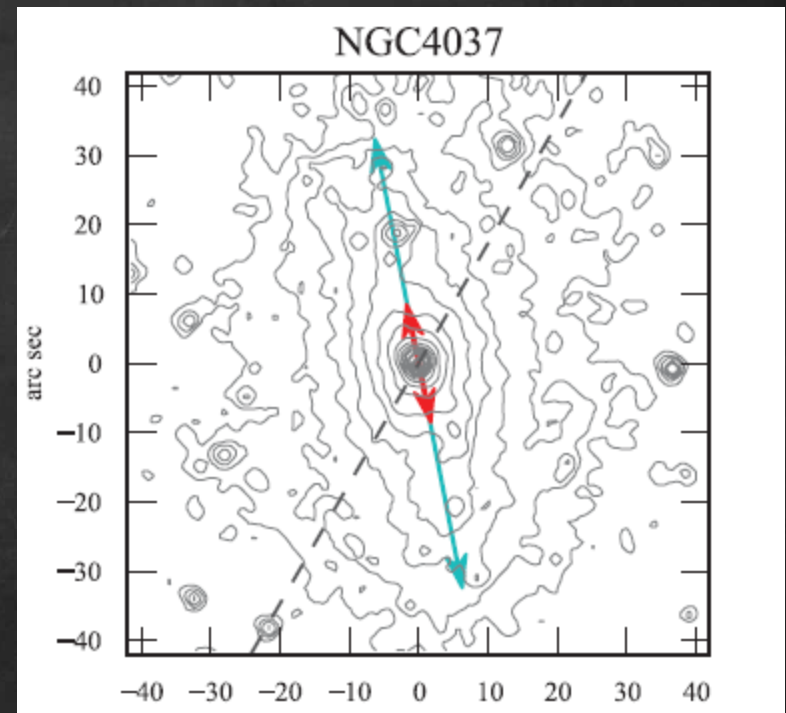
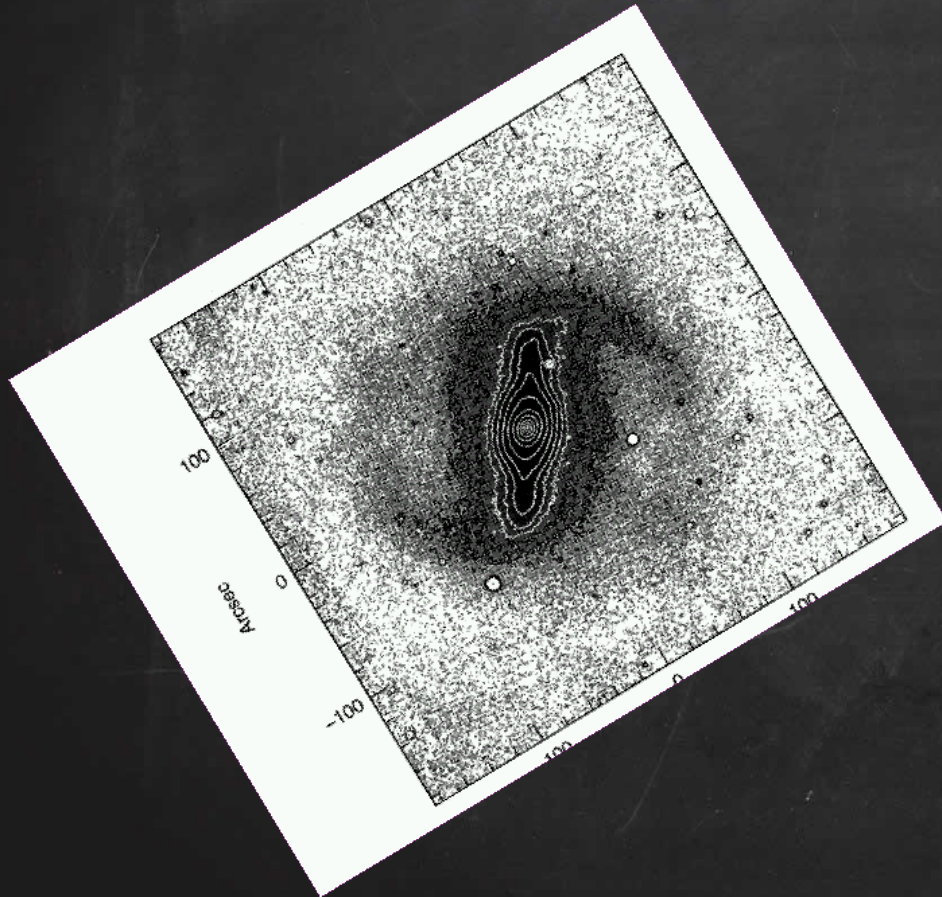


Bureau et al. 2006



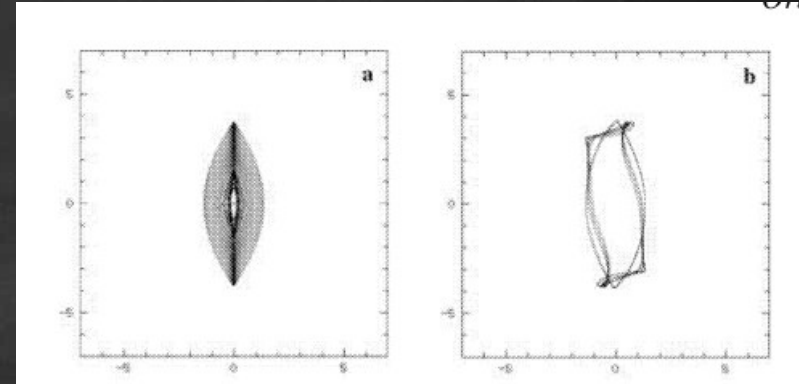
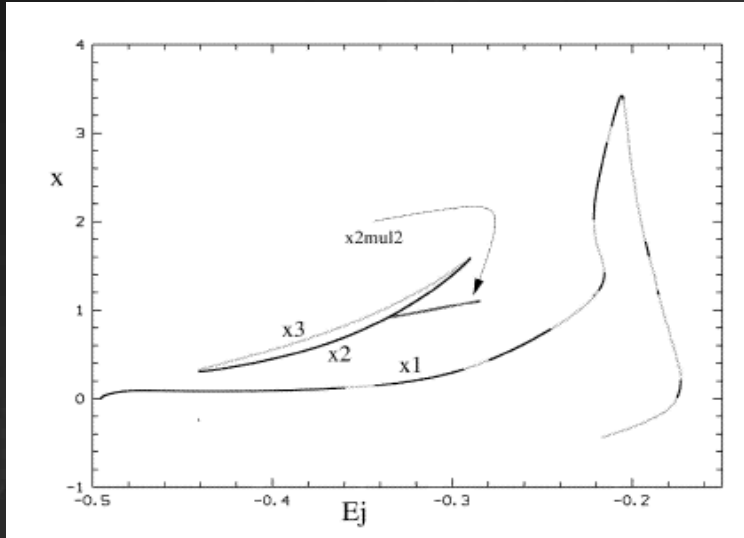
Patsis & Xilouris 2006

# Outer and Inner boxiness of the bars in face-on views



Erwin & Debattista 2013

# Standard bar building blocks



Skokos, Patsis,  
Athanassaoula  
2002, 2003

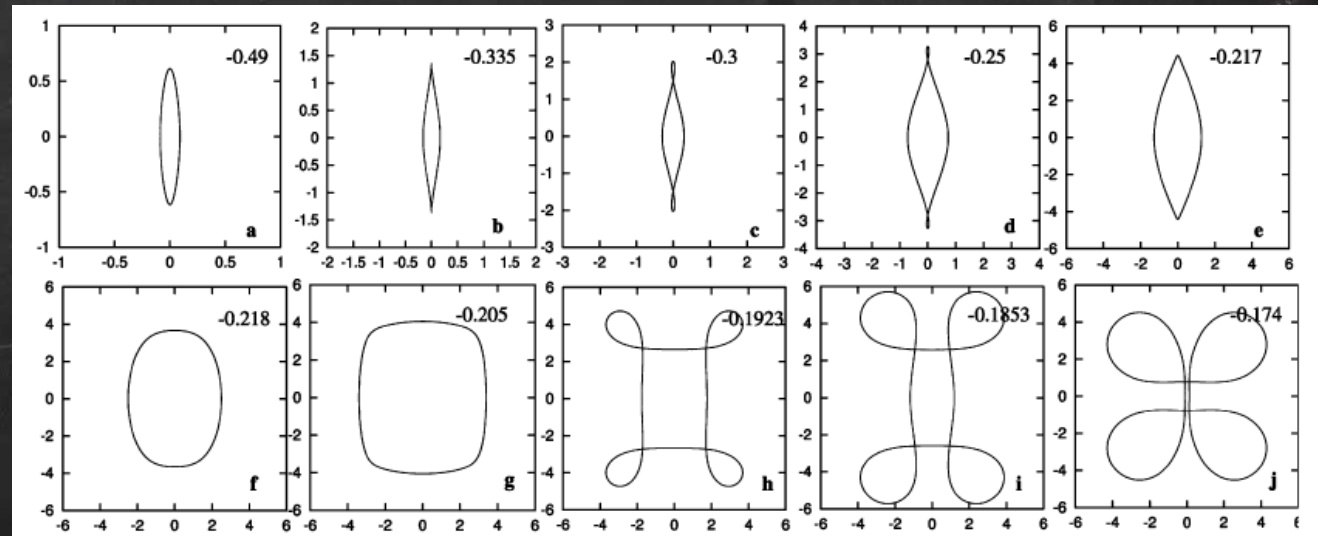
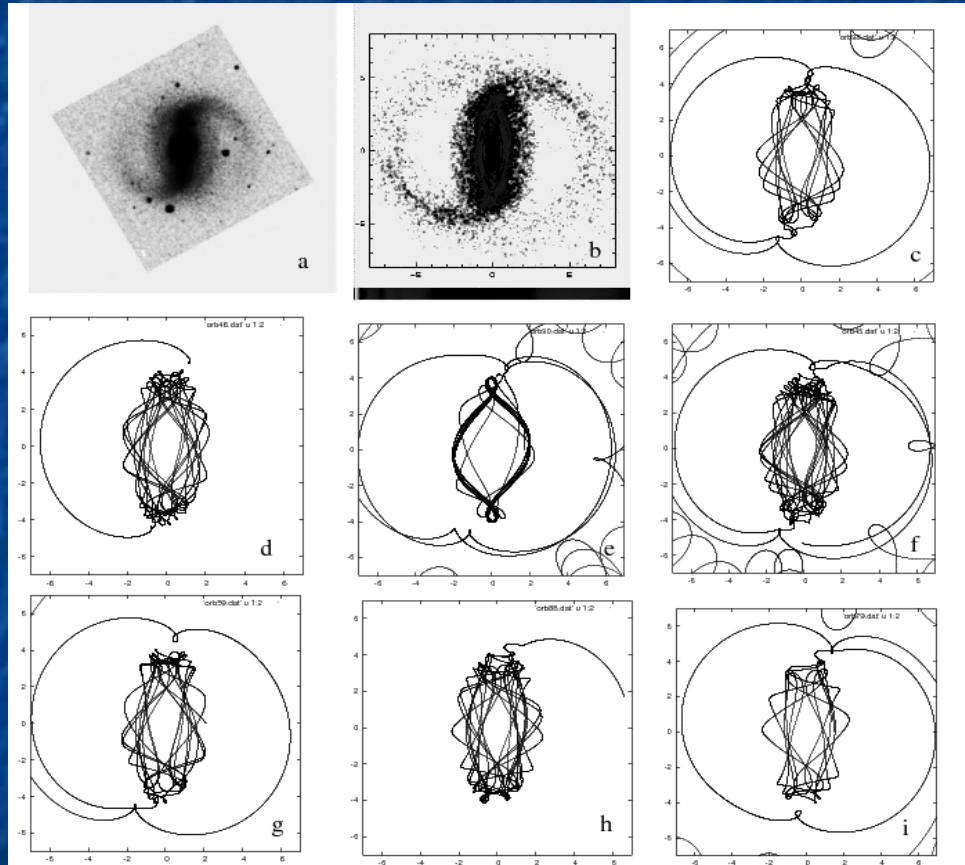


Figure 2.  $x_1$  stable orbits in model A1. The numbers at the upper right-hand corners of the panels indicate their  $E_j$  values.

# 4:1 resonance-type chaotic orbits.





$\Phi = \text{Miyamoto disk} + \text{Plummmmer sphere} + \text{3D Ferrers bar}$

$$H = \frac{1}{2}(p_x^2 + p_y^2 + p_z^2) + \Phi(x, y, z) - \Omega_b(xp_y - yp_x),$$

with

$$\Phi(x, y, z)_{eff} = \Phi(x, y, z) - \Omega_b(xp_y - yp_x)$$

$$\begin{aligned} \dot{x} &= p_x + \Omega_b y, & \dot{y} &= p_y - \Omega_b x, & \dot{z} &= p_z \\ \dot{p}_x &= -\frac{\partial \Phi}{\partial x} + \Omega_b p_y, & \dot{p}_y &= -\frac{\partial \Phi}{\partial y} - \Omega_b p_x, & \dot{p}_z &= -\frac{\partial \Phi}{\partial z} \end{aligned}$$

$$\Phi(x, y, z) = \Phi_D + \Phi_S + \Phi_B$$

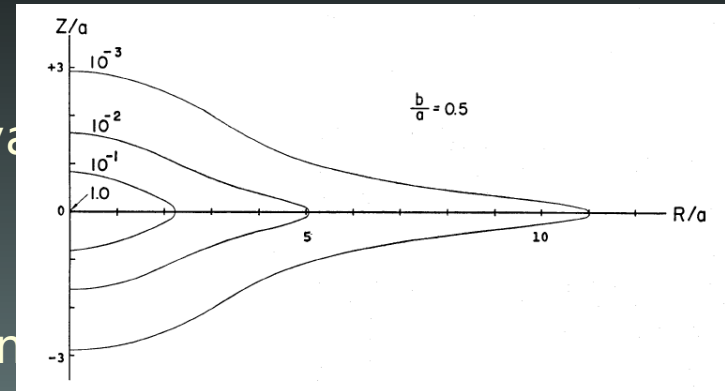
4D space of section, i.c.  $(x, p_x, z, p_z)$  in the plane  $y=0$  with  $p_y > 0$

$$\Phi_D = -\frac{GM_D}{\sqrt{x^2 + y^2 + (A + \sqrt{B^2 + z^2})^2}},$$

- Miyamoto

$$\Phi_S = -\frac{GM_S}{\sqrt{x^2 + y^2 + z^2 + \epsilon_s^2}},$$

- Plummer

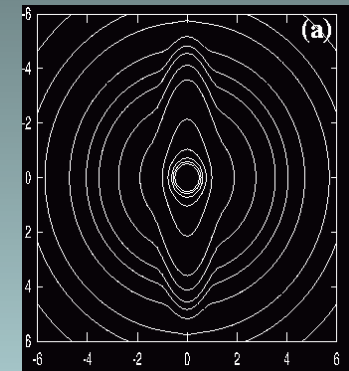


$$\rho = \begin{cases} \frac{105M_B}{32\pi abc} (1 - m^2)^2 & \text{for } m \leq 1 \\ 0 & \text{for } m > 1 \end{cases},$$

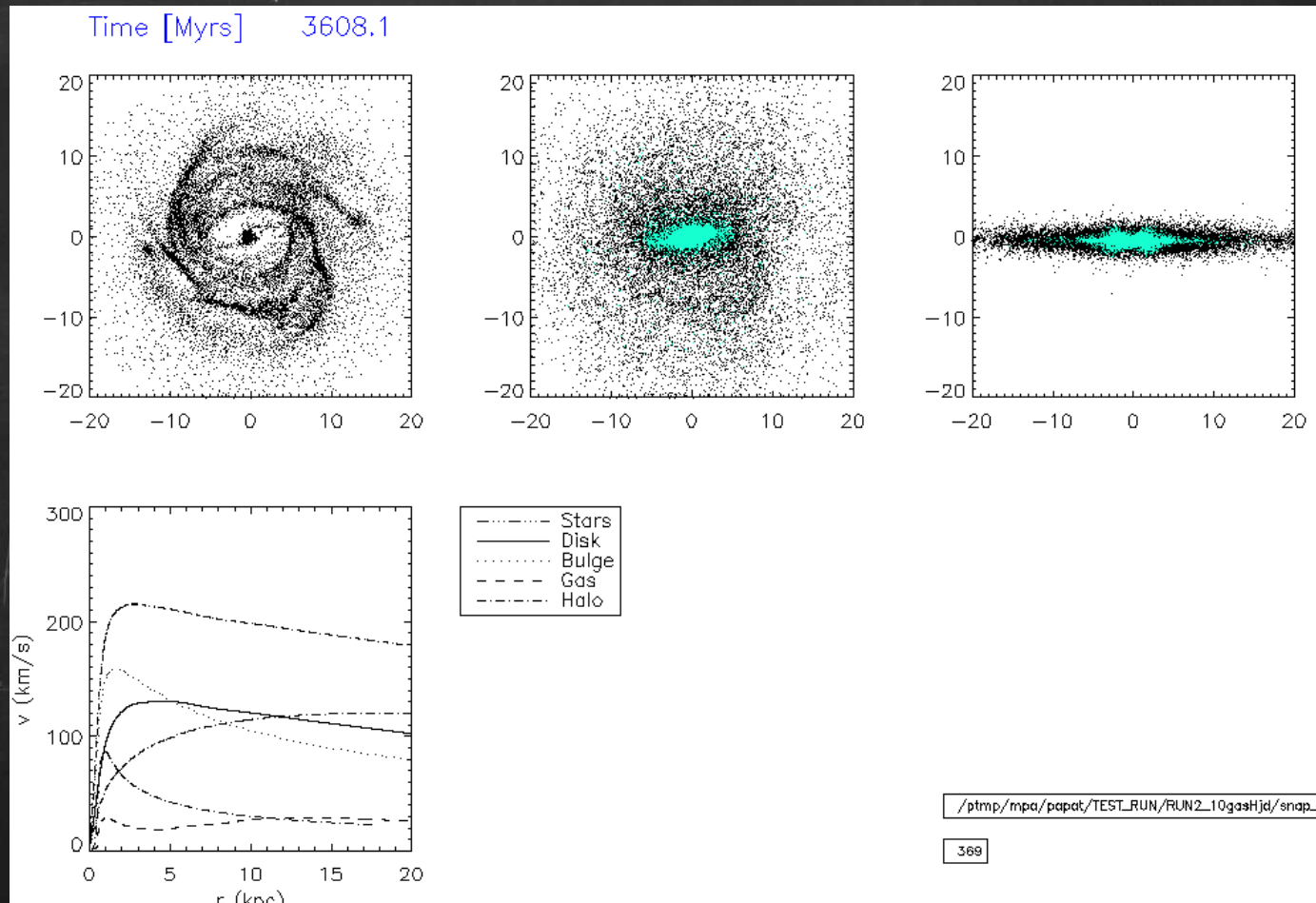
- Ferrers bar, a:b:c = 6:1.5:0.6

where

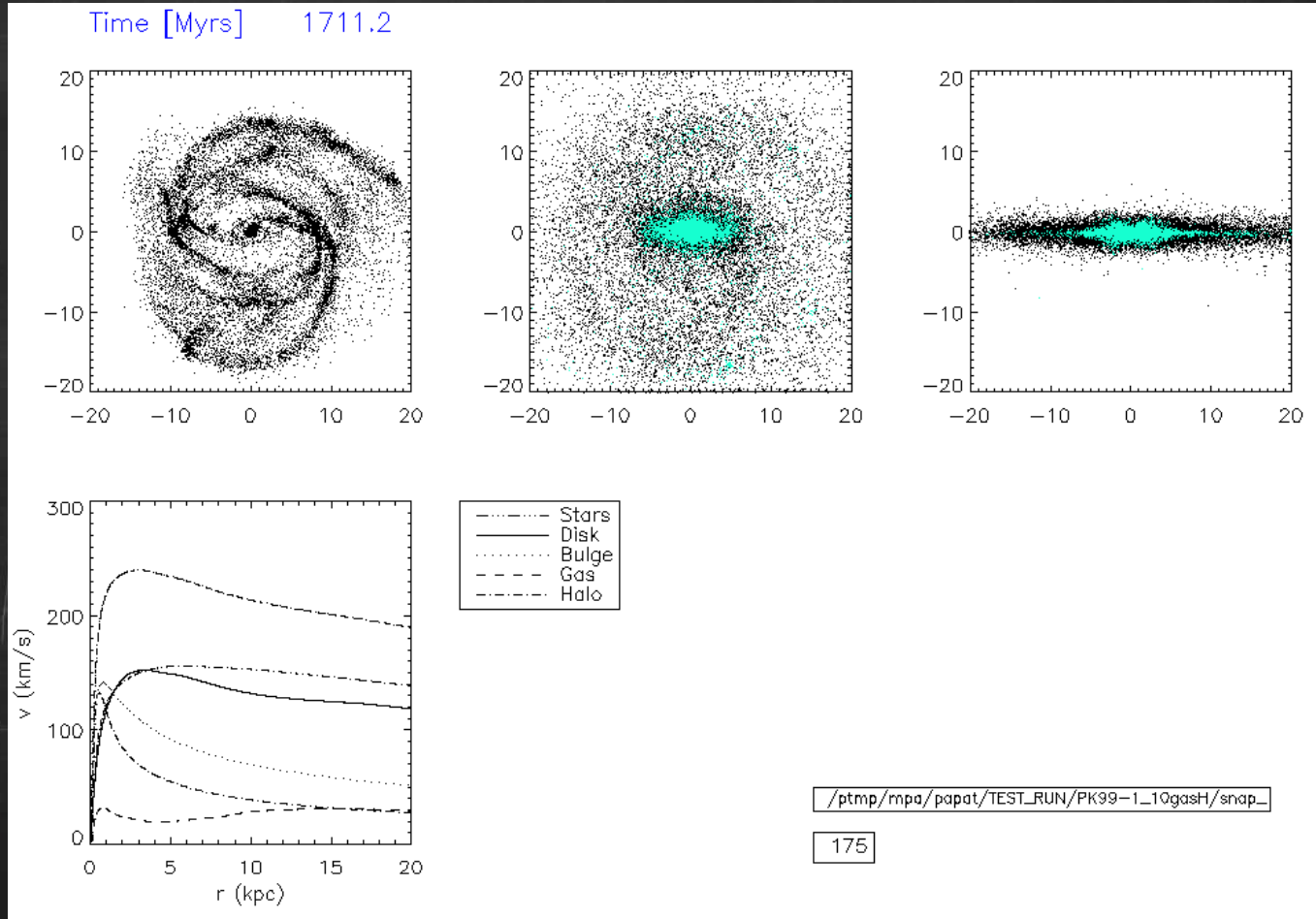
$$m^2 = \frac{y^2}{a^2} + \frac{x^2}{b^2} + \frac{z^2}{c^2}, \quad a > b > c,$$



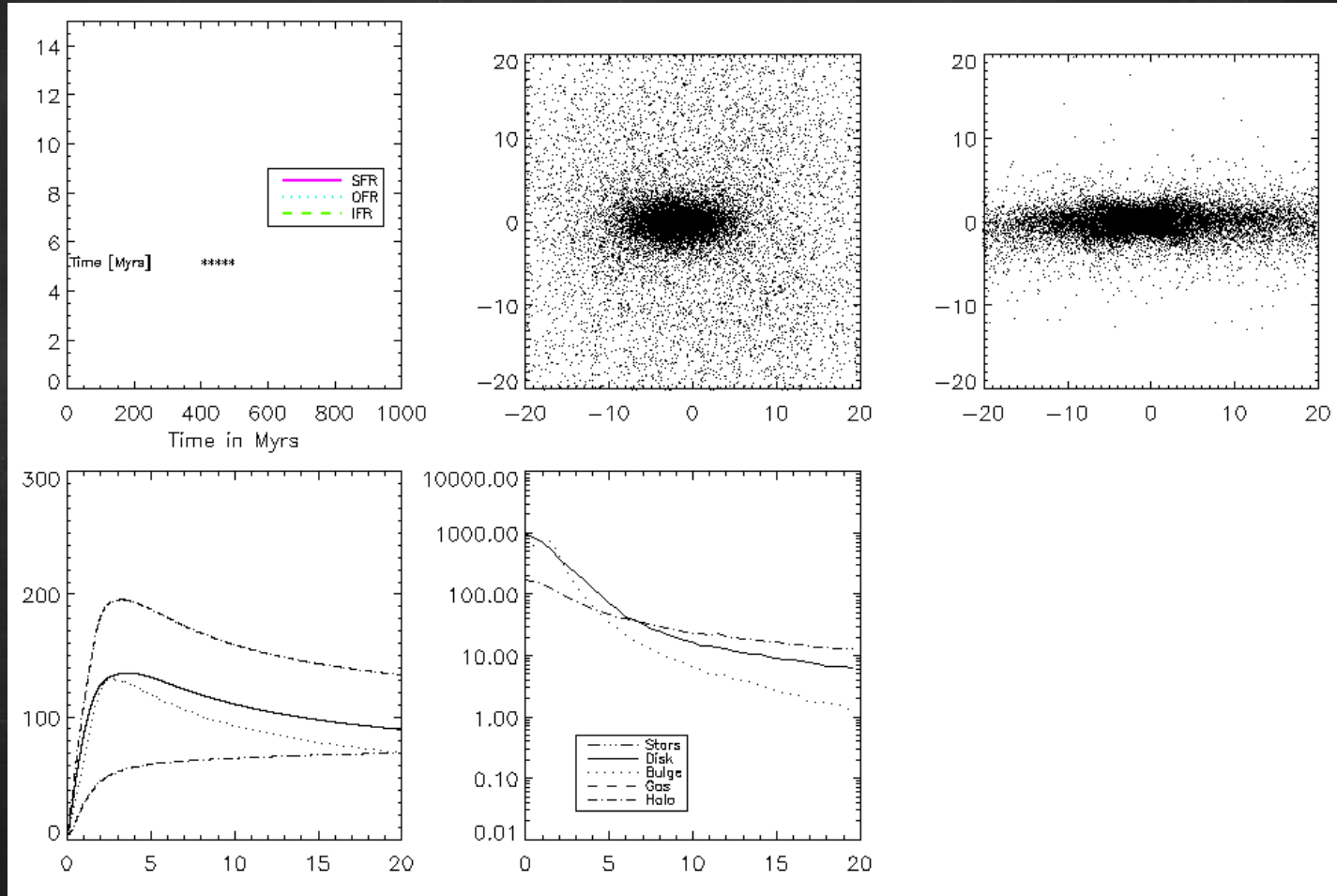
# N-body peanuts I



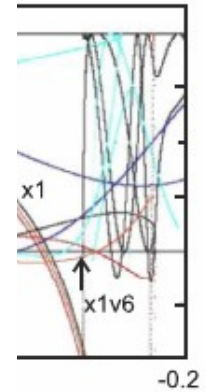
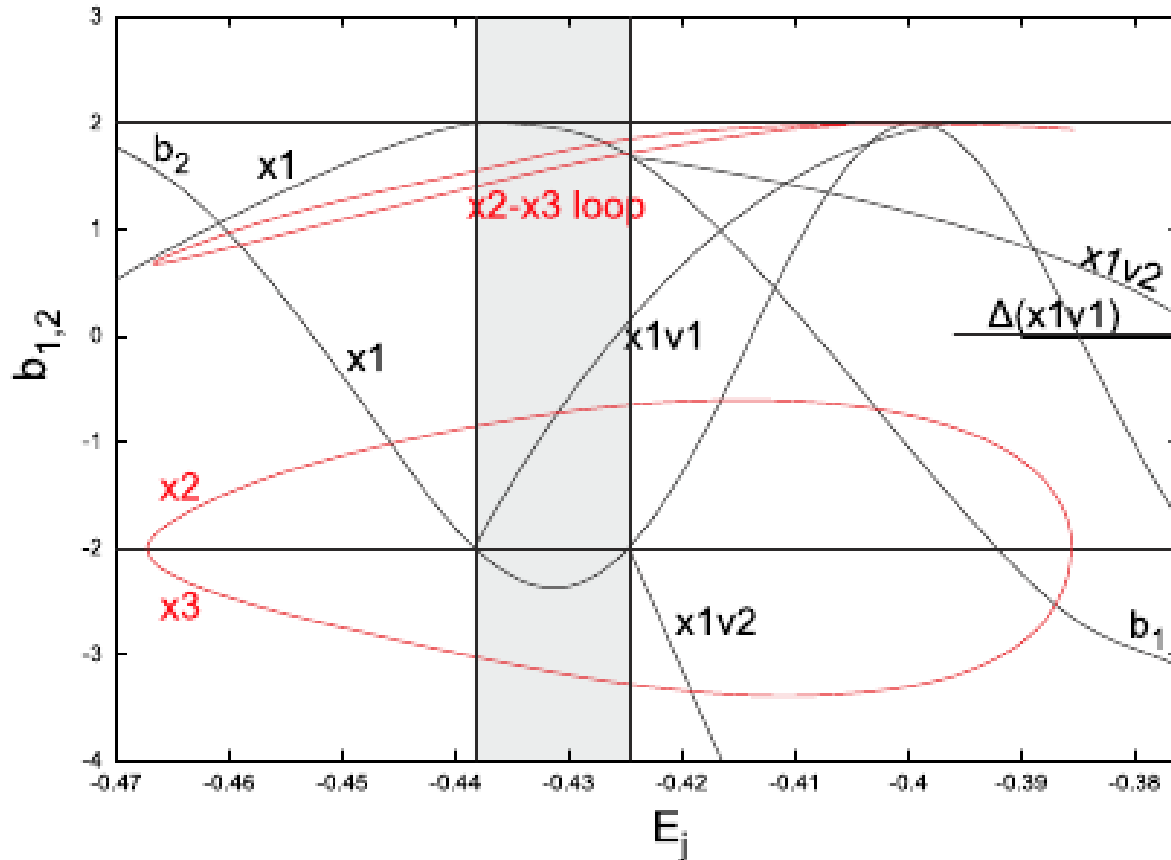
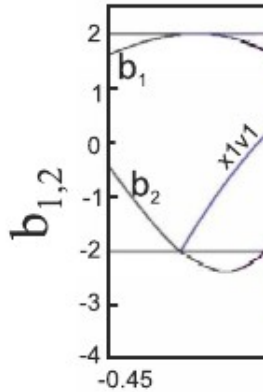
# N-body peanuts II



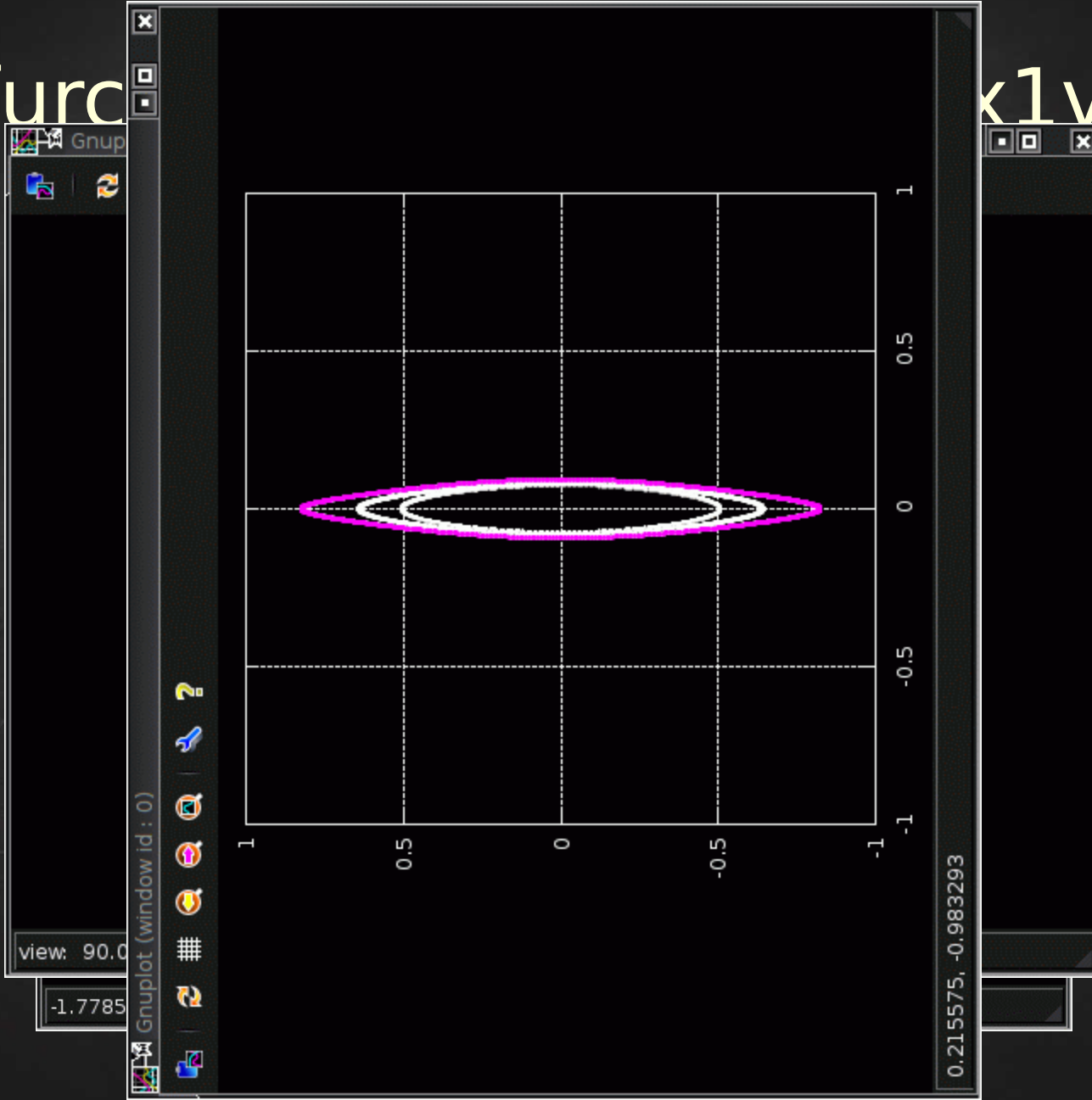
# N-body peanuts III



# Where does the b/p start?



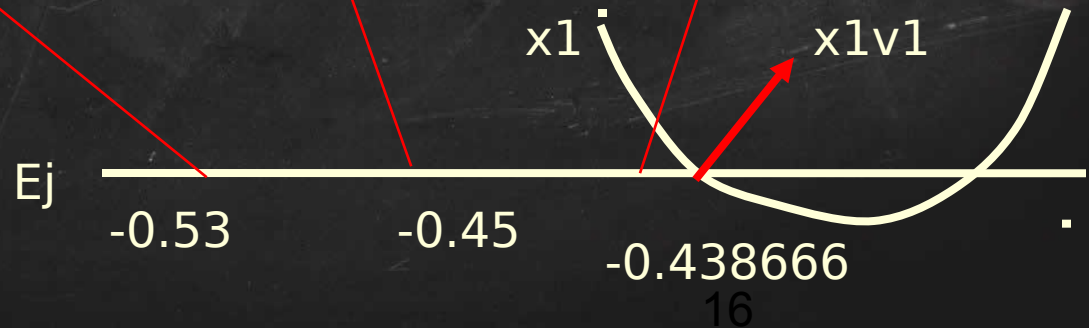
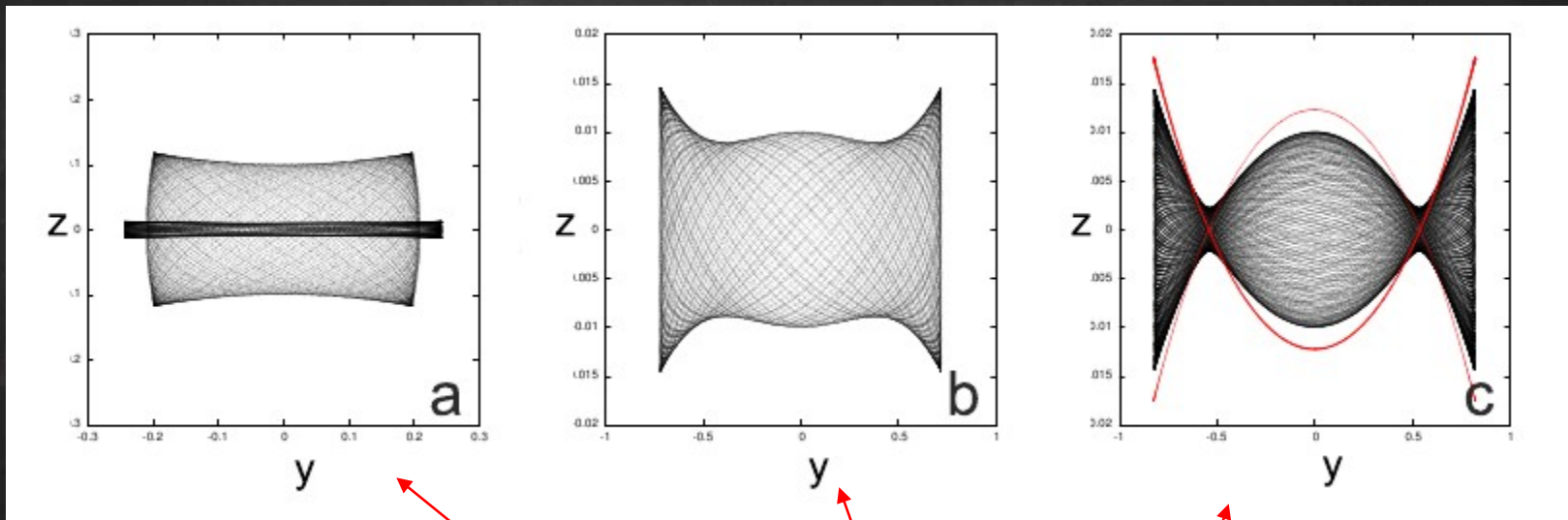
# Bifurc



$x_1 v_1'$

# Early q-p x1 orbits

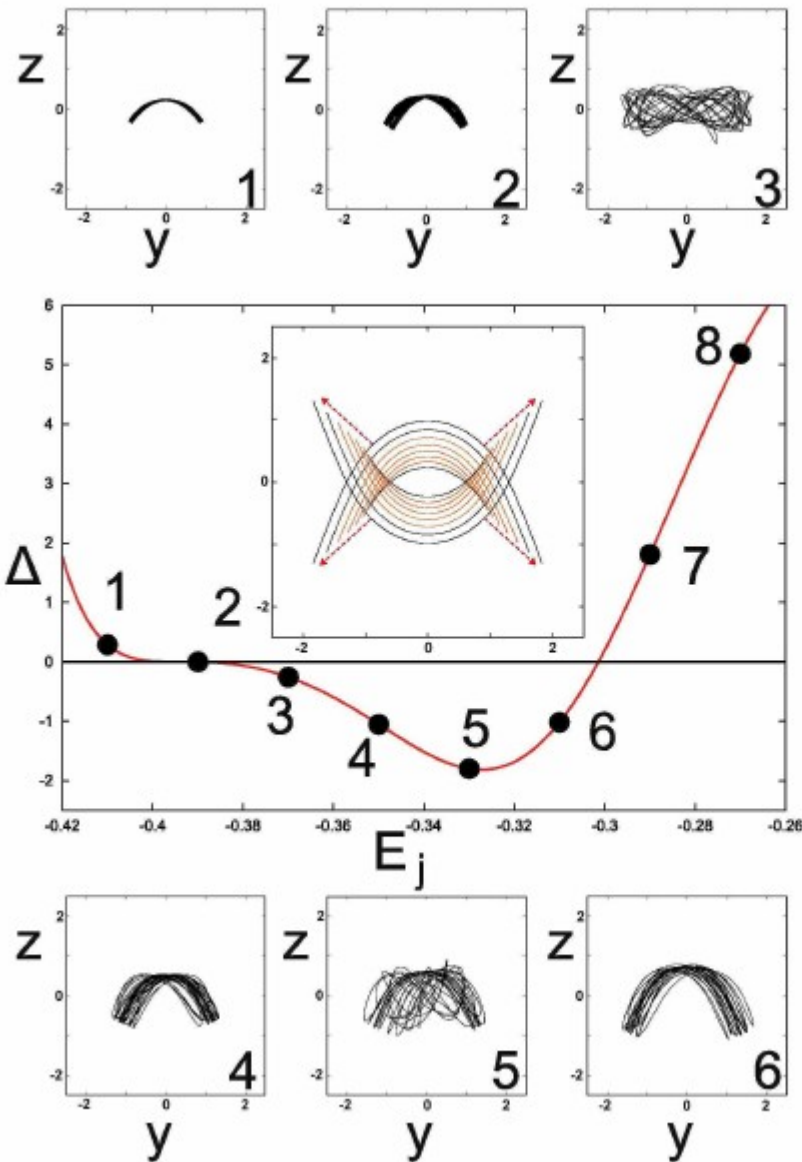
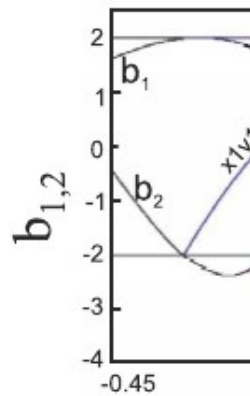
x1v1





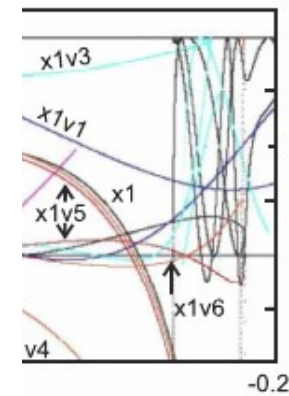
Asse

- $x_1, x_2$

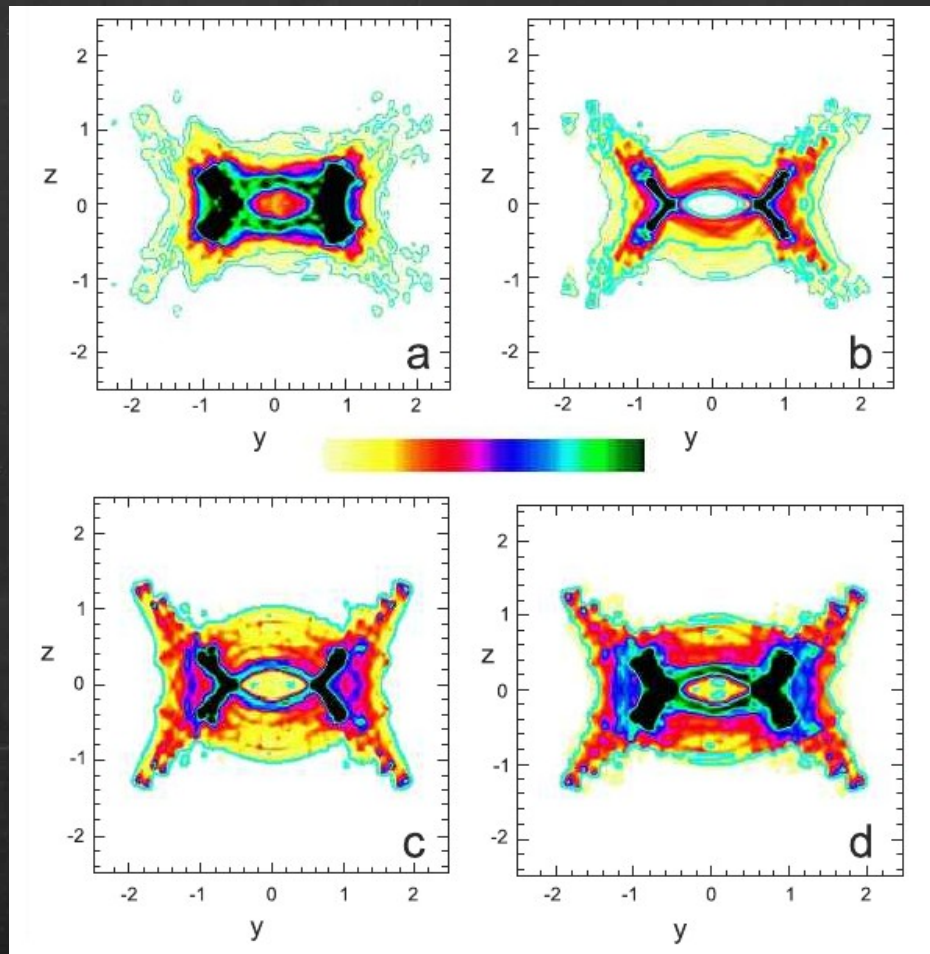


p.o.

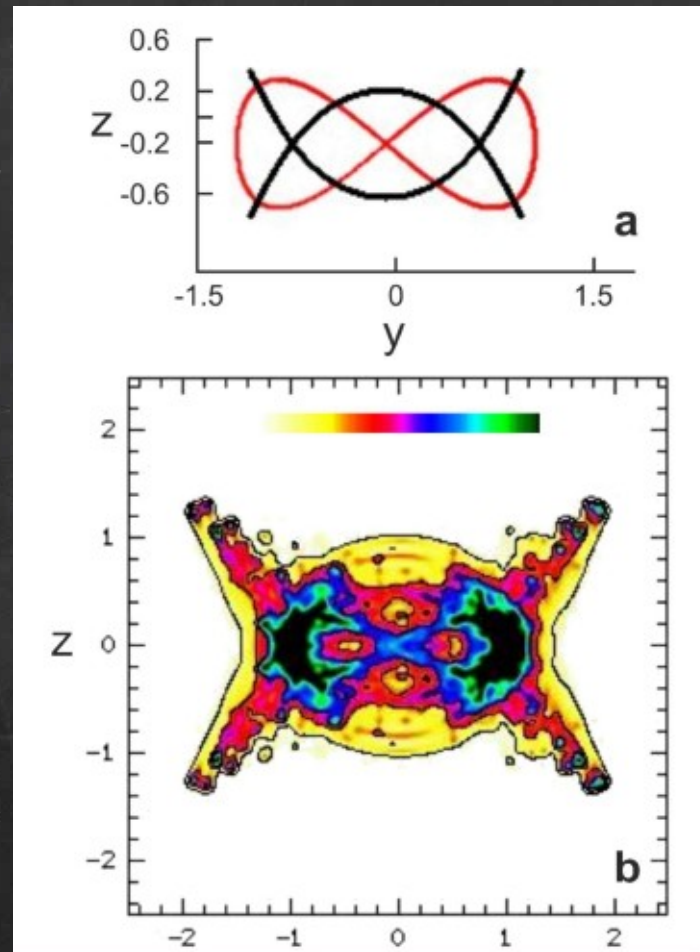
am)



# the “x1v1” scenario

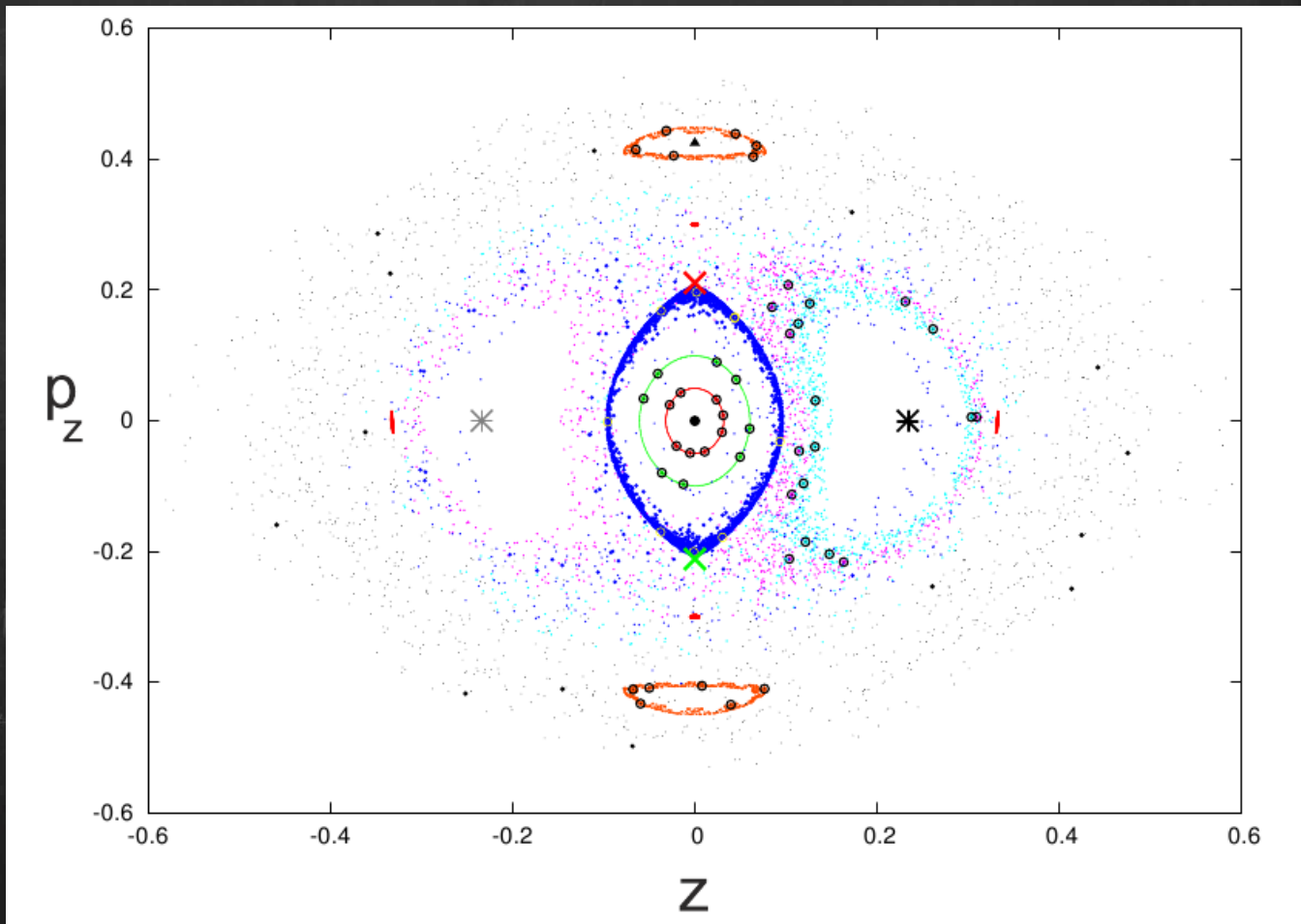


# adding x1v2-like (CX-OX profiles)

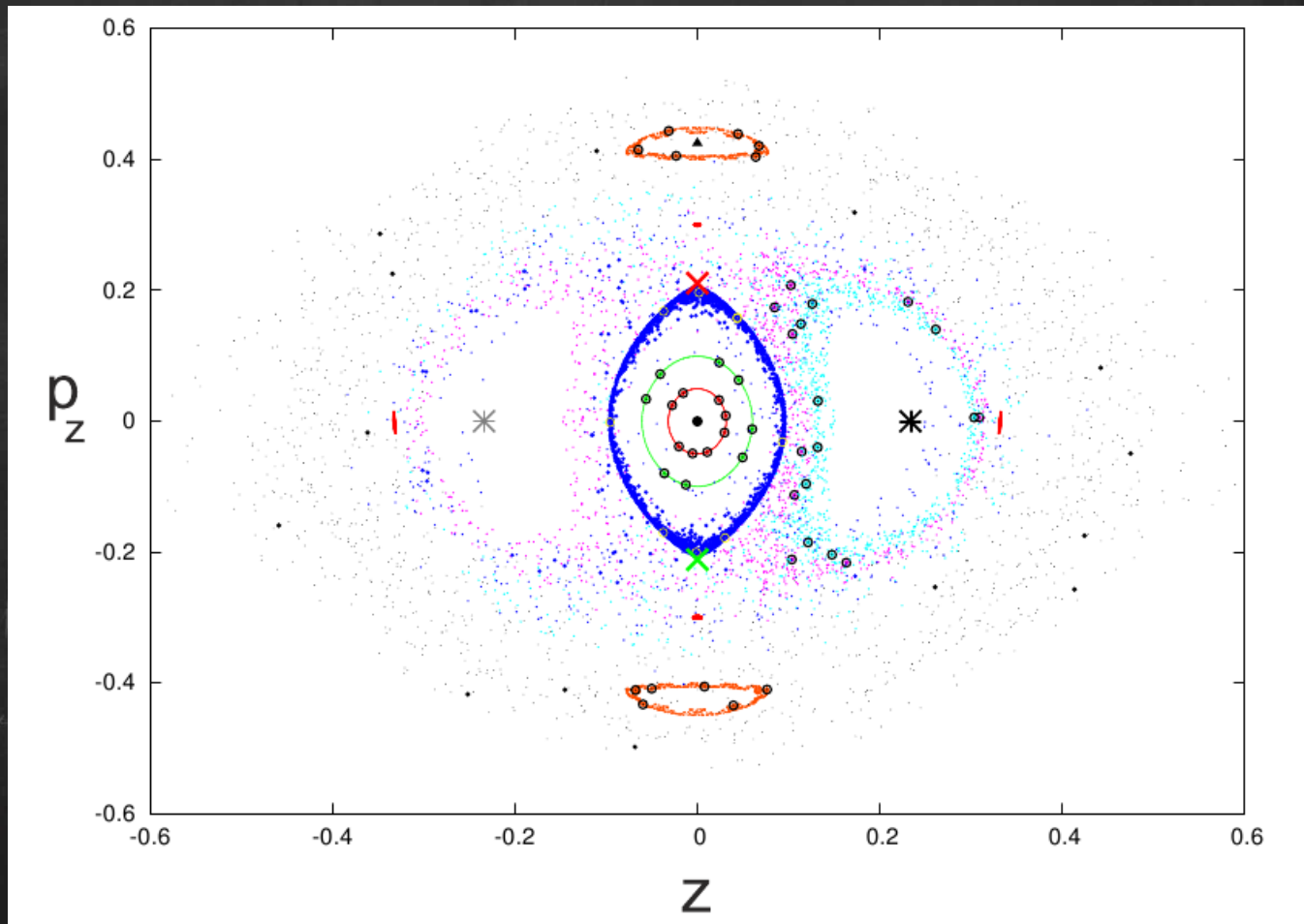


# “CX”-profiles

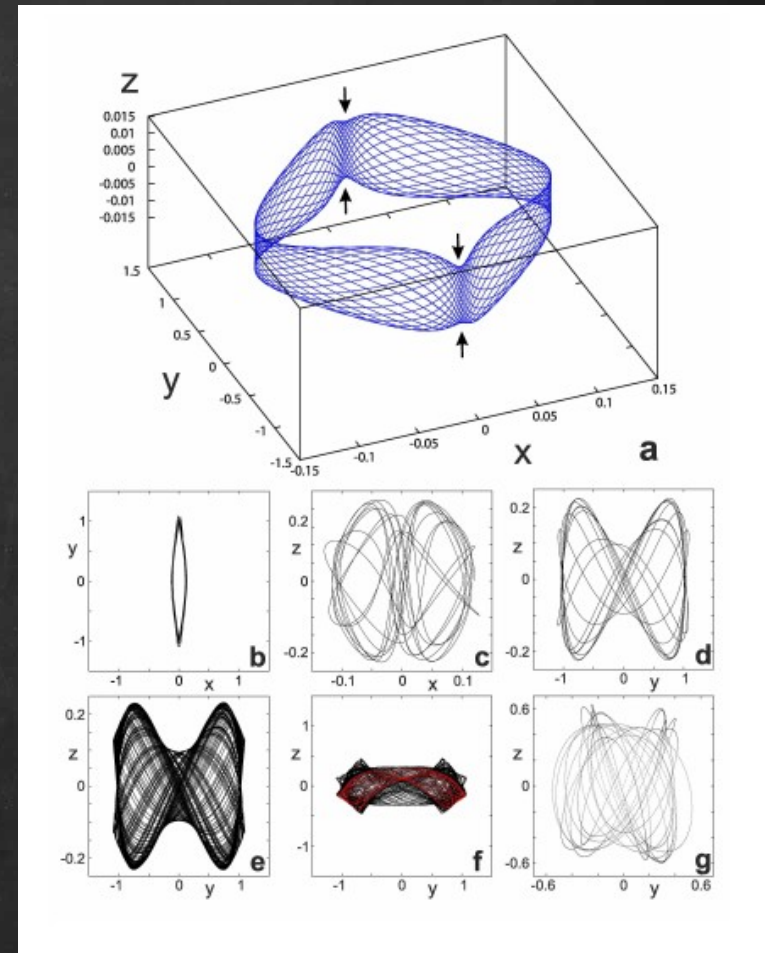
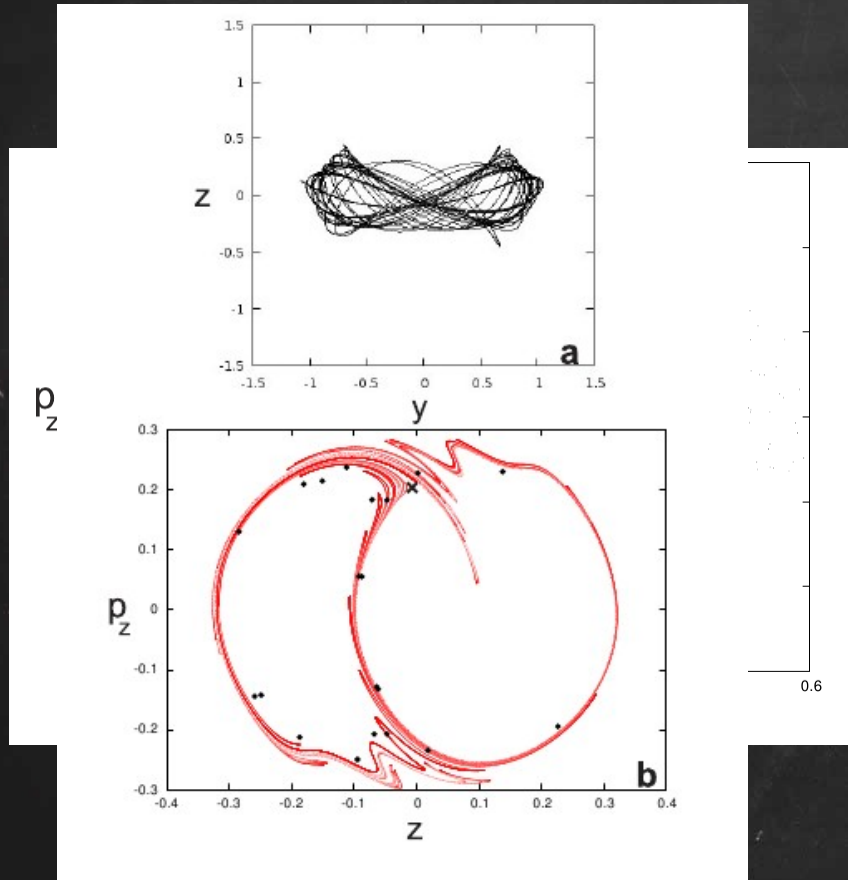
$E_j = -0.41$  (x1,x1v1 S; x1v2 U)



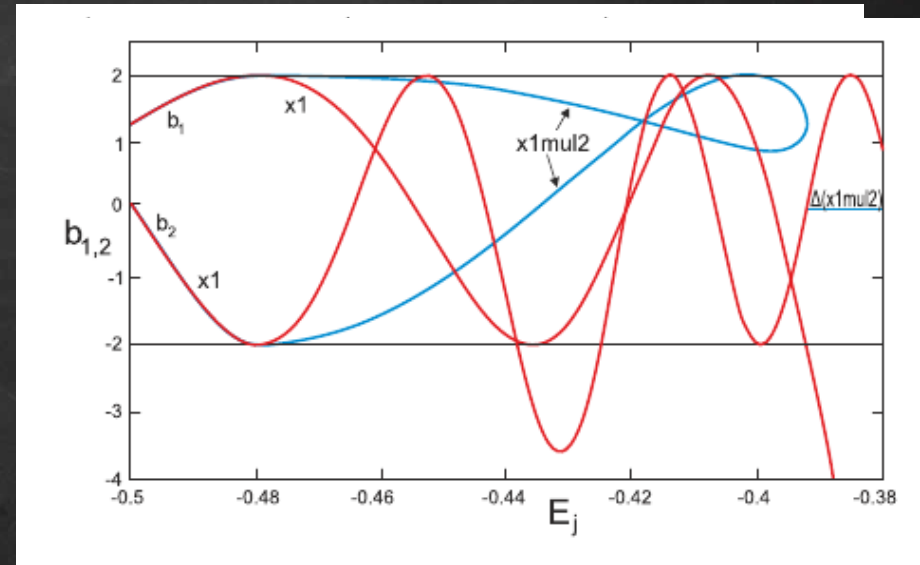
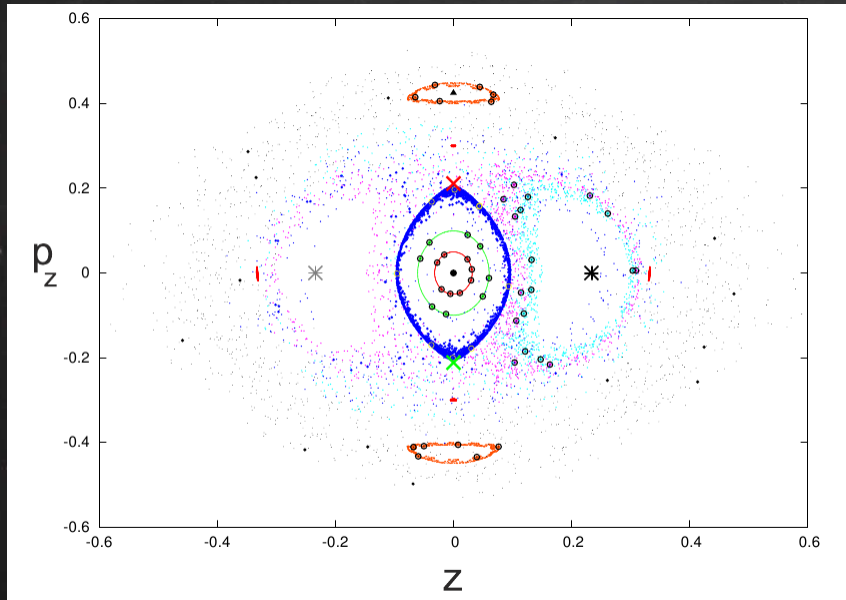
# The $x1v1 - x1v1'$ attractor



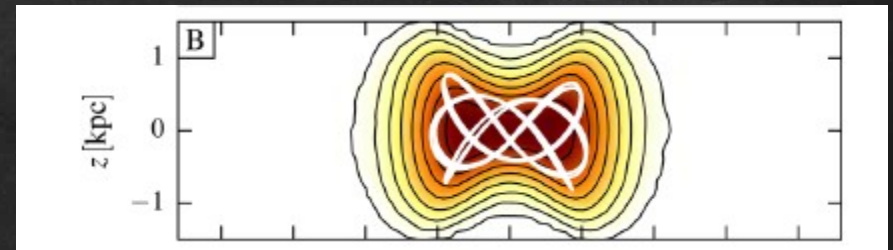
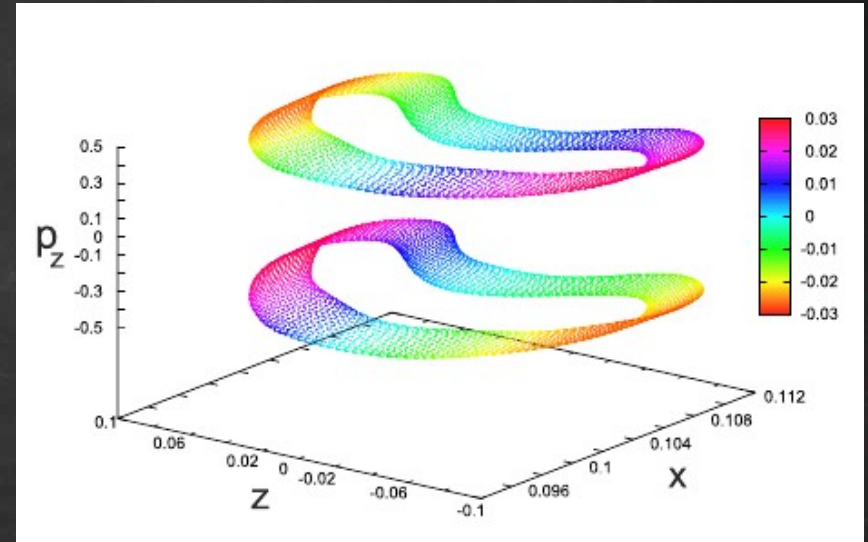
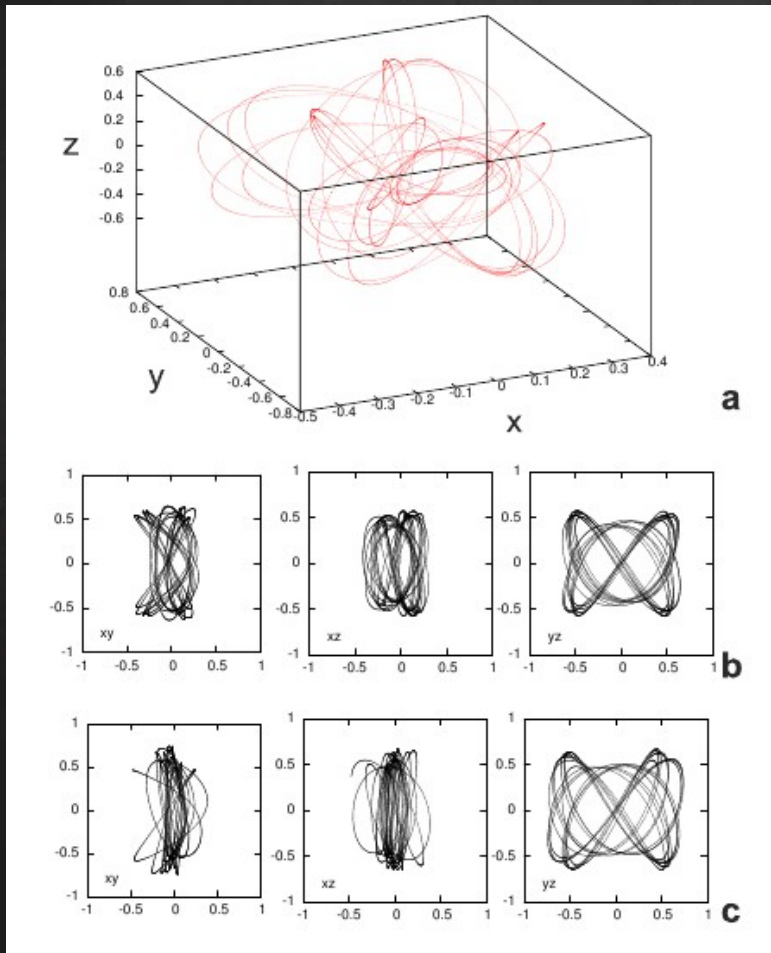
# $E_j = -0.41$



# x1mul2



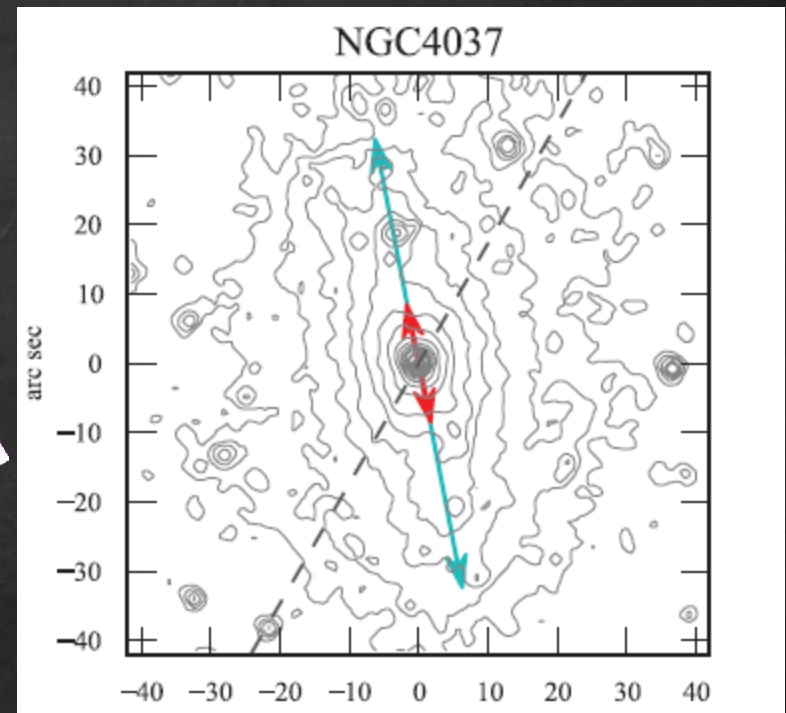
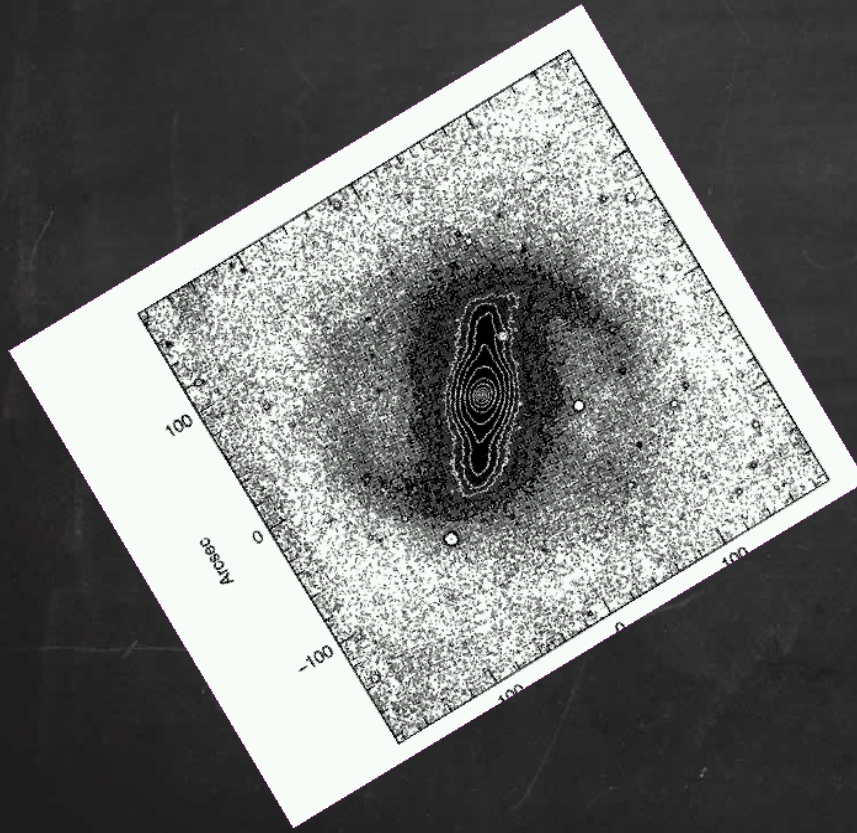
# s & $\Delta x1mul2$



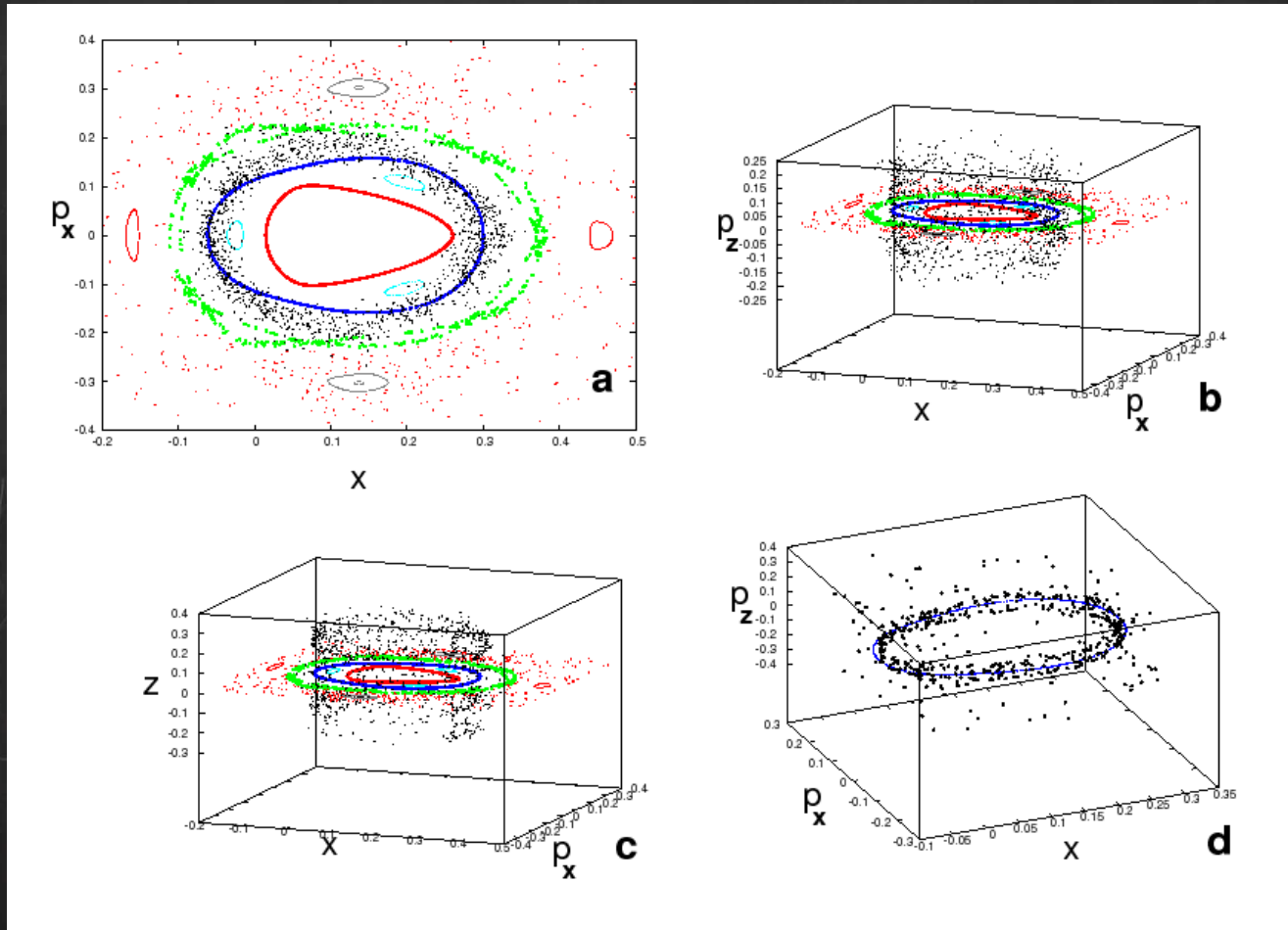
Portail, Wegg & Gerhard 2015



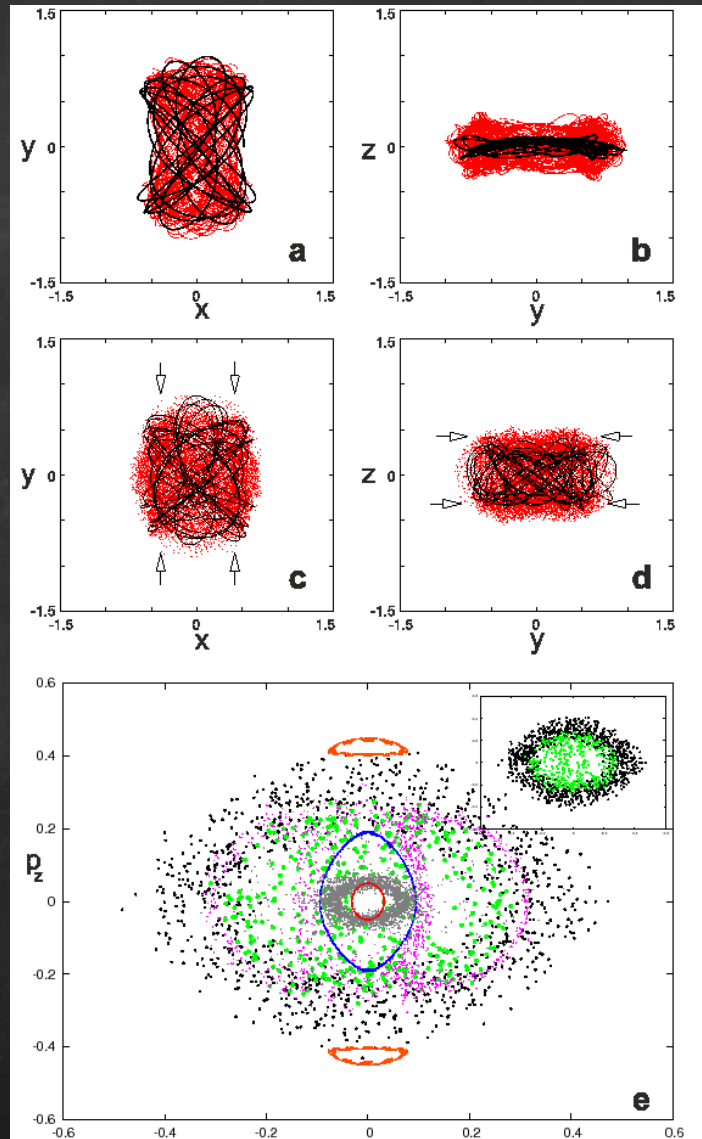
# 4. Inner boxiness of the bars



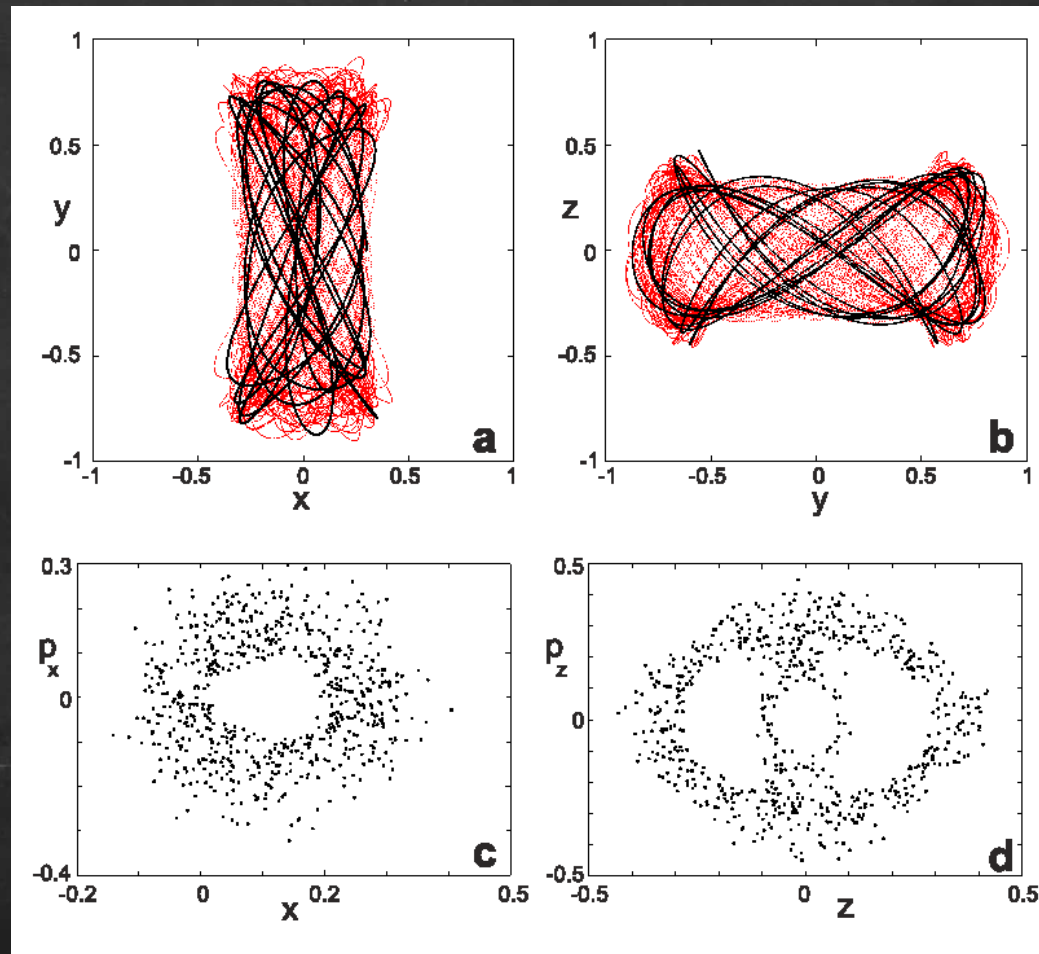
# $(x, p_x)$ + vertical perturbations



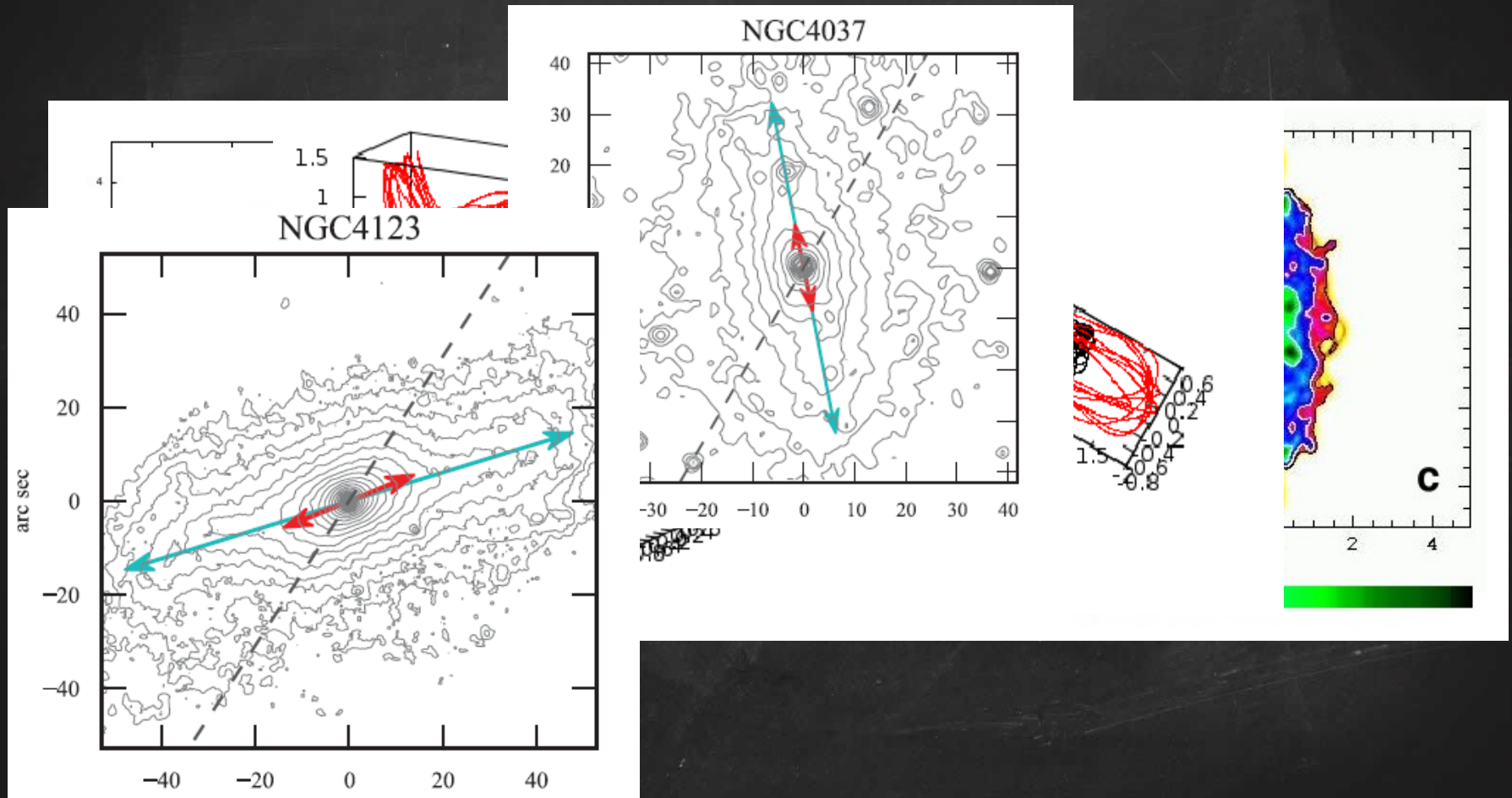
# $(x, p_x)$ in the chaotic sea



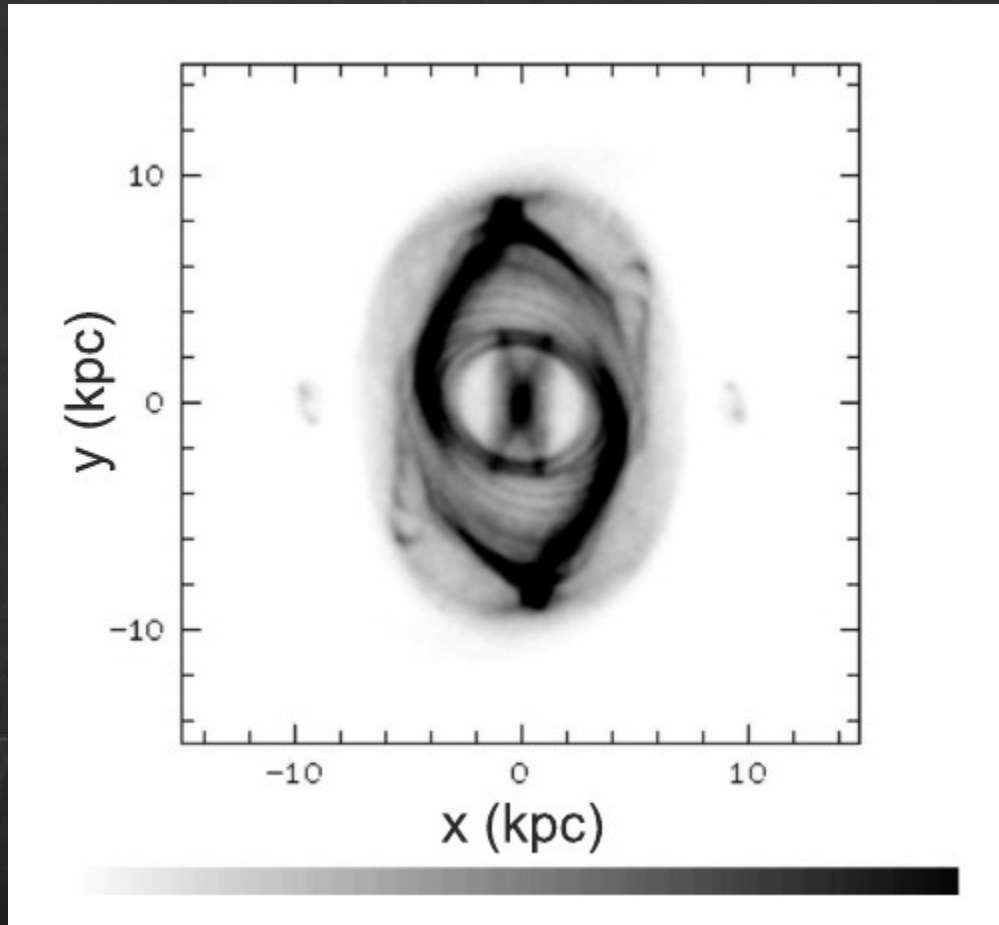
# $(x, p_x)$ in the stability island

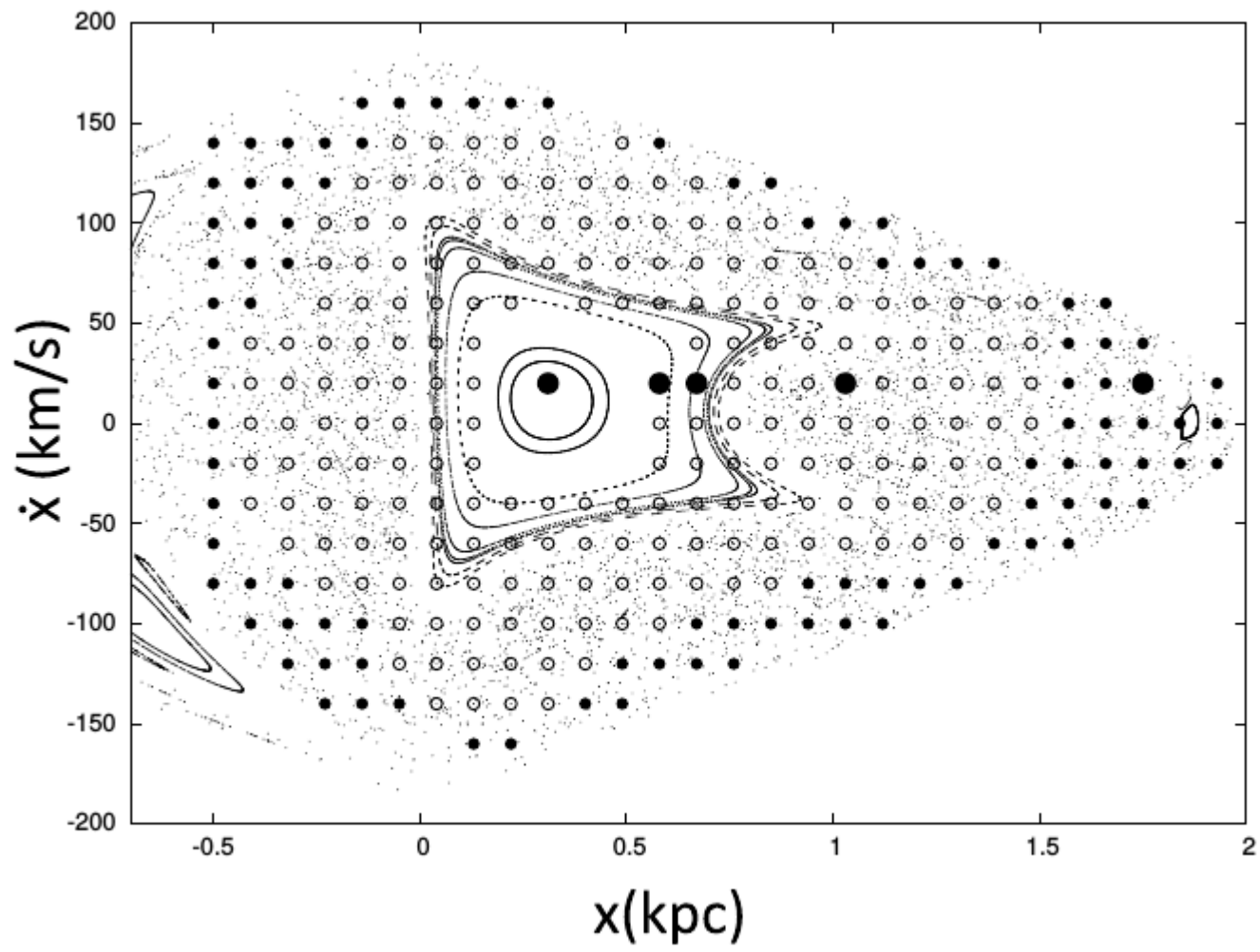


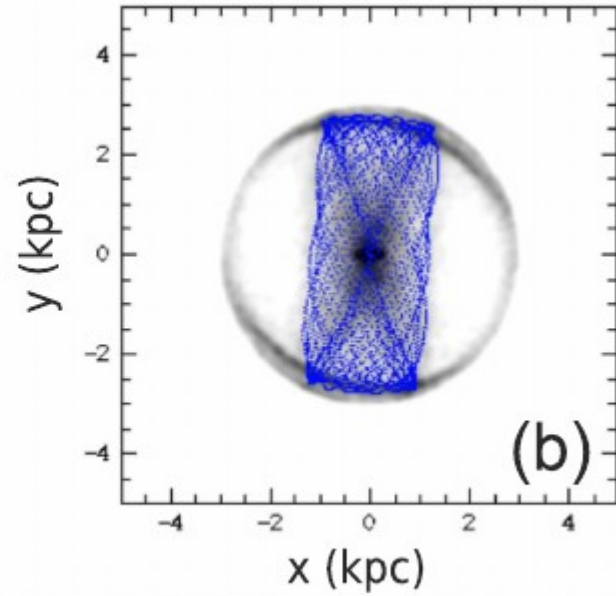
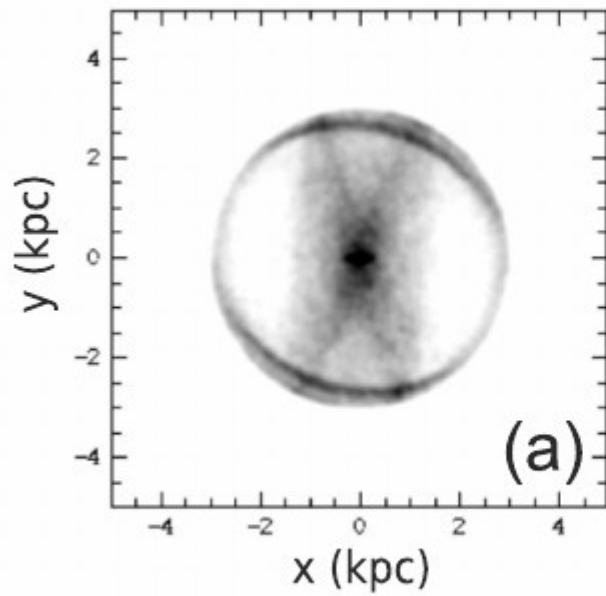
# face-on profiles



# sticky chaotic orbits behind boxy barred features?









# Summary

- **Inner boxiness** observed in face-on bars can be supported by **chaotic orbits sticky to  $x_1$** .
- The presence of **inner boxy isophotes** in face-on views of bars is a strong indication for the **participation of chaos** in the building of the bar

# Summary

- There is a **direct relation** between **inner boxy face-on** and **inner boxy edge-on** features.

Both are determined by the dominance of the  **$x1v1 - x1v1'$  tori** in 4D cross sections.

- The internal structure of a peanut depends on the amount of non-periodic orbits populated in the phase space of the v/r-ILR region.

Thank you for your  
attention

